

```
*****  
*****  
***  
*** Demonstration of the Astree static analyzer ***  
*** http://www.astree.ens.fr/ ***  
***  
*****  
*****
```

```
*****  
* Astree is SOUND hence reports ALL potential *  
* runtime errors *  
*****
```

*** example [CC76]:

```
cat -n dichotomy-error.c  
1 /* dichotomy-error.c */  
2 int main () {  
3     int lwb, upb, m, R[100], X;  
4     lwb = 1; upb = 100;  
5     while (lwb <= upb) {  
6         m = (upb + lwb) / 2;  
7         if (X == R[m]) {  
8             upb = m; lwb = m+1; }  
9         else if (X < R[m]) {  
10            upb = m - 1; }  
11        else {  
12            lwb = m + 1; }  
13    }  
14    __ASTREE_log_vars((m));  
15 }
```

*** static analysis by Astree:

```
/* Analyzer launched at 2006/ 7/12 06:47:19  
dichotomy-error.c:7.15-19::[call#main@2:loop@5>=4:]: WARN: invalid dereference: dereferencing  
dichotomy-error.c:7.15-19::[call#main@2:loop@5>=4:]: WARN: invalid dereference: dereferencing  
dichotomy-error.c:9.19-23::[call#main@2:loop@5>=4:]: WARN: invalid dereference: dereferencing  
dichotomy-error.c:9.19-23::[call#main@2:loop@5>=4:]: WARN: invalid dereference: dereferencing  
%
```

*** (the two errors are reported two times
each because of partitioning.)

```
*****  
* Astree is INCOMPLETE hence may report false alarms *  
*****
```

*** example:

```

cat -n fausse-alarme.c
 1  /* fausse-alarme.c */
 2  void main()
 3  {
 4      int x, y;
 5      if ((-4681 < y) && (y < 4681) && (x < 32767) && (-32767 < x) && ((7*y*y - 1) ==
 6          y = 1 / x;
 7      });
 8  }

```

*** static analysis by Astree:

```

astree --exec-fn main --no-relational fausse-alarme.c |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:47:23
fausse-alarme.c:6.9-14::[call#main@2:]: WARN: integer division by zero ([-32766, 32766] and
%
```

```

*****
* Astree is based upon classical abstract domains *
* such as intervals.. *
*****

```

*** example:

```

cat -n dichotomy.c
 1  /* dichotomy.c */
 2  int main () {
 3      int lwb, upb, m, R[100], X;
 4      lwb = 0; upb = 99;
 5      while (lwb <= upb) {
 6          m = (upb + lwb) / 2;
 7          if (X == R[m]) {
 8              upb = m; lwb = m+1; }
 9          else if (X < R[m]) {
10              upb = m - 1; }
11          else {
12              lwb = m + 1; }
13      }
14      __ASTREE_log_vars((m));
15  }

```

*** correction (difference with the erroneous version):

```

1c1
< /* dichotomy-error.c */
---
> /* dichotomy.c */
4c4
<     lwb = 1; upb = 100;
---
>     lwb = 0; upb = 99;

```

*** static analysis by Astree:

```

astree --exec-fn main --no-relational dichotomy.c |& egrep "(launched)|(m in )"
/* Analyzer launched at 2006/ 7/12 06:47:28
<interval: <m in [0, 99]> <> > <modulo: >

```

%

*** (pay attention to the case of many global variables!)

```
*****
* Astree uses weakly relational abstract *
* domains such as octagons...          *
*****
```

*** example:

```
cat -n octagon.c
 1  /* octagon.c */
 2  void main()
 3  {
 4      int X, Y, Z;
 5      X = 10;
 6      Y = 100;
 7      while (X >= 0) {
 8          X--;
 9          Y--;
10     };
11     __ASTREE_assert((X <= Y));
12 }
```

*** static analysis by Astree (1 -- WITHOUT octagons):

```
astree octagon.c --no-octagon --exec-fn main |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:47:31
octagon.c:9.4-7::[call#main@2:loop@7>=4:]: WARN: signed int arithmetic range [-2147483649,
octagon.c:11.19-25::[call#main@2:]: WARN: assert failure
%
```

*** static analysis by Astree (2 -- WITH octagons):

```
astree octagon.c --exec-fn main |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:47:33
%
```

*** (does not scale up for too many variables!)

```
*****
* Astree uses weakly relational abstract *
* domains such as boolean decision trees... *
*****
```

*** example:

```
cat -n boolean.c
 1  /* boolean.c */
 2  typedef enum {F=0,T=1} BOOL;
 3  BOOL B;
 4  void main () {
```

```

5     unsigned int X, Y;
6     while (1) {
7         /* ... */
8         B = (X == 0);
9         /* ... */
10        if (!B) {
11            Y = 1 / X;
12        }
13        /* ... */
14    }
15 }

```

*** static analysis by Astree (1 -- WITHOUT decision trees):

```

astree boolean.c --no-relational --exec-fn main |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:47:36
boolean.c:11.13-18::[call#main@4:loop@6=1:]: WARN: integer division by zero ([0, 4294967295
boolean.c:11.13-18::[call#main@4:loop@6=2:]: WARN: integer division by zero ([0, 4294967295
boolean.c:11.13-18::[call#main@4:loop@6=3:]: WARN: integer division by zero ([0, 4294967295
boolean.c:11.13-18::[call#main@4:loop@6>=4:]: WARN: integer division by zero ([0, 429496729
%

```

*** static analysis by Astree (2 -- WITH decision trees):

```

astree boolean.c --exec-fn main |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:47:38
%

```

```

*****
* Astree uses computation trace abstractions *
* (describing sequences of states) not only *
* invariants (describing sets of states) *
*****

```

*** example:

```

cat -n trace-partitioning.c
1  /* trace-partitioning.c */
2  void main() {
3      float t[5] = {-10.0, -10.0, 0.0, 10.0, 10.0};
4      float c[4] = {0.0, 2.0, 2.0, 0.0};
5      float d[4] = {-20.0, -20.0, 0.0, 20.0};
6      float x, r;
7      int i = 0;
8      __ASTREE_known_fact((( -100.0 <= x) && (x <= 100.0)));
9      while ((i < 3) && (x >= t[i+1])) {
10         i = i + 1;
11     }
12     r = (x - t[i]) * c[i] + d[i];
13     __ASTREE_log_vars((r));
14 }

```

*** static analysis by Astree (1 -- WITH partitioning):

```
astree --exec-fn main --no-trace --no-relational trace-partitioning.c |& egrep "(launched)
/* Analyzer launched at 2006/ 7/12 06:47:41
   <interval: <> <r in [-20, 20]> > <modulo: >
%
```

```
*** static analysis by Astree (2 -- WITHOUT
    partitioning):
```

```
astree --exec-fn main --no-partition --no-trace --no-relational trace-partitioning.c |& eg
/* Analyzer launched at 2006/ 7/12 06:47:42
   <interval: <> <r in [-240, 240]> > <modulo: >
%
```

```
*****
* Astree handles floats, not reals or *
* fixed point arithmetics           *
*****
```

```
*** example of computation error in floats:
*** (x+a)-(x-a) <> 2a! with float
```

```
cat -n float-float.c
1  /* float-float.c */
2  int main () {
3  float x; float a, y, z, r1, r2;
4  a = 1.0;
5  x = 1125899973951488.0;
6  y = (x + a);
7  z = (x - a);
8  r1 = y - z;
9  r2 = 2 * a;
10 printf("(x + a) - (x - a) = %f\n", r1);
11 printf("2a                = %f\n", r2);
12 }
```

```
*** compilation:
```

```
float-float.c: In function 'main':
float-float.c:10: warning: incompatible implicit declaration of built-in function 'printf'
```

```
*** execution:
```

```
(x + a) - (x - a) = 0.000000
2a                = 2.000000
```

```
*** more precision can be better...
*** (x+a)-(x-a) <> 2a! with double
```

```
cat -n double-double.c
1  /* double-double.c */
2  int main () {
3  double x; double a, y, z, r1, r2;
4  a = 1.0;
5  x = 1125899973951488.0;
6  y = (x + a);
7  z = (x - a);
8  r1 = y - z;
```

```

9   r2 = 2 * a;
10  printf("(x + a) - (x - a) = %f\n", r1);
11  printf("2a          = %f\n", r2);
12  }

```

*** compilation:

```

double-double.c: In function 'main':
double-double.c:10: warning: incompatible implicit declaration of built-in function 'print

```

*** execution:

```

(x + a) - (x - a) = 2.000000
2a          = 2.000000

```

```

*** computations with different precisions...
*** can be really catastrophic!
*** (x+a)-(x-a) <> 2a! with double+float

```

```

cat -n double-float.c
1  /* double-float.c */
2  int main () {
3  double x; float a, y, z, r1, r2;
4  a = 1.0;
5  x = 1125899973951488.0;
6  y = (x + a);
7  z = (x - a);
8  r1 = y - z;
9  r2 = 2 * a;
10 printf("(x + a) - (x - a) = %f\n", r1);
11 printf("2a          = %f\n", r2);
12 }

```

*** compilation:

```

double-float.c: In function 'main':
double-float.c:10: warning: incompatible implicit declaration of built-in function 'printf

```

*** execution:

```

(x + a) - (x - a) = 134217728.000000
2a          = 2.000000

```

```

*** testing is unlikely to make it!
*** (x+a)-(x-a) <> 2a! with double+float

```

```

cat -n double-float2.c
1  /* double-float2.c */
2  int main () {
3  double x; float a, y, z, r1, r2;
4  a = 1.0;
5  x = 1125899973951487.0;
6  y = (x + a);
7  z = (x - a);
8  r1 = y - z;
9  r2 = 2 * a;
10 printf("(x + a) - (x - a) = %f\n", r1);

```

```
11 printf("2a          = %f\n", r2);
12 }
```

*** only one digit difference:

```
1c1
< /* double-float2.c */
---
> /* double-float.c */
5c5
< x = 1125899973951487.0;
---
> x = 1125899973951488.0;
```

*** compilation:

```
double-float2.c: In function 'main':
double-float2.c:10: warning: incompatible implicit declaration of built-in function 'print
```

*** execution:

```
(x + a) - (x - a) = 0.000000
2a                = 2.000000
```

```
*****
* Astree takes rounding errors into account... *
*****
```

*** example $((x+a)-(x-a)) \leftrightarrow 2a!$ in double+float):

```
cat -n double-float-analyze.c
1  /* double-float-analyze.c */
2  int main () {
3  double x; float a, y, z, r1, r2;
4  a = 1.0;
5  x = 1125899973951488.0;
6  y = (x + a);
7  z = (x - a);
8  r1 = y - z;
9  r2 = 2 * a;
10 __ASTREE_log_vars((r1, r2));
11 }
```

*** static analysis by Astree:

```
astree --exec-fn main double-float-analyze.c |& egrep "(launched)|(r2 in )|(r1 in)"
/* Analyzer launched at 2006/ 7/12 06:47:58
<interval: <> <r2 in {2}, r1 in [-1.34218e+08, 1.34218e+08]> > <symbolic: >
%
```

```
*****
* Astree takes into account the potential accumulation *
* of rounding errors over very long periods of time... *
*****
```

*** example:

```
cat -n bary.c
 1  /* bary.c */
 2  typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
 3  float INIT,C1,I;
 4  float RANDOM_INPUT;
 5  __ASTREE_volatile_input((RANDOM_INPUT [-1.,1.]));
 6
 7  void bary () {
 8      static float X,Y,Z;
 9      if (C1>0.)
10          {Z = Y;Y = X;}
11      if (INIT>0.)
12          {
13              X=I;
14              Y=I;
15              Z=I;
16          }
17      else
18          {X = 0.50000001 * X + 0.30000001*Y + 0.20000001*Z  ;};
19      __ASTREE_log_vars((X,Y,Z));
20
21  }
22
23  void main () {
24      INIT = 1.;
25      C1 = RANDOM_INPUT;
26      I = RANDOM_INPUT;
27      while (1) {
28          bary();
29          INIT = RANDOM_INPUT;
30          C1 = RANDOM_INPUT;
31          I = RANDOM_INPUT;
32          __ASTREE_wait_for_clock();
33      }
34  }
```

*** configuration file (10 hours at 1/100th s):

```
cat -n bary10.config
 1  __ASTREE_max_clock((3600000));
```

*** static analysis by Astree:

```
astree --exec-fn main --config-sem bary10.config bary.c |& tail -n 75 | egrep --after-cont
<interval: <> <Z in [-1.71113, 1.71113], Y in [-1.71113, 1.71113],
X in [-1.71113, 1.71113]> > <symbolic: >
%
```

*** configuration file (100 hours at 1/100th s):

```
cat -n bary100.config
 1  __ASTREE_max_clock((36000000));
```

*** static analysis by Astree:

```
astree --exec-fn main --config-sem bary100.config bary.c |& tail -n 75 | egrep --after-cor
<interval: <> <Z in [-215.193, 215.193], Y in [-215.193, 215.193],
```

```

X in [-215.193, 215.193]> > <symbolic: >
%

*** configuration file (1000 hours at 1/100th s):

cat -n bary1000.config
  1  __ASTREE_max_clock((360000000));

*** static analysis by Astree:

astree --exec-fn main --config-sem bary1000.config bary.c |& tail -n 50 | egrep --after-cc
<interval: <> <Z in [-2.1295e+23, 2.1295e+23],
  Y in [-2.1295e+23, 2.1295e+23], X in [-2.1295e+23, 2.1295e+23]> >
%

*** (note that the analysis time is independent
    of the execution time.)

```

```

*****
* Astree knows about basic numerical computations... *
*****

```

```

*** example (rounding computations):

```

```

cat -n moda_dur_3.c
  1  /* entree */
  2  double X;
  3  __ASTREE_volatile_input((X [-186.,186.]));
  4
  5  /* sortie */
  6  double RESULTAT;
  7
  8  void N()
  9  {
 10     int tronc_entier;
 11     double entree,diametre,min,rapport,troncature,plancher,multiple_inf,reste,rest
 12     int BPO;
 13     min = 0;
 14     diametre = 1.;
 15
 16     /* au choix: nouvelle entree ou retroaction */
 17     if (BPO) entree = X;
 18     else     entree = RESULTAT;
 19
 20     /* calcul du rapport de entree - min / diametre, puis de sa troncature */
 21     min = 0;
 22     diametre = 1.;
 23     rapport = (entree - min) / diametre;
 24     tronc_entier = (int) rapport;
 25     troncature = (double) tronc_entier;
 26
 27     /* calcul de la valeur plancher de ce rapport */
 28     if (rapport<0) plancher = troncature - 1;
 29     else          plancher = troncature;
 30
 31     /* calcul du reste de l'entree */
 32     reste = entree - (diametre * plancher);
 33

```

```

34      /* calcul du multiple inferieur a l'entree*/
35      multiple_inf = entree - reste;
36
37      /* calcul du multiple superieur a l'entree*/
38      multiple_sup = multiple_inf + diametre;
39
40
41      /* calcul du multiple le plus proche */
42      if (reste < 0) reste_abs = -reste;
43      else           reste_abs = reste;
44      if (reste_abs <= 0.5*diametre) plus_proche = multiple_inf;
45      else                           plus_proche = multiple_sup;
46
47
48      /* resultat */
49      RESULTAT = plus_proche;
50      __ASTREE_log_vars((entree,RESULTAT;mod,inter));
51  }
52
53
54  void main()
55  {
56      while (1) {
57          N();
58          __ASTREE_wait_for_clock();
59      }
60  }

```

*** static analysis by Astree (1 - WITHOUT abstract domain for truncations):

```

astree moda_dur_3.c --exec-fn main --no-nod |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:48:07

```

```

moda_dur_3.c:24.17-30::[call#main@54:loop@56>=4:call#N@57:]: WARN: double->signed int conver
%

```

*** static analysis by Astree (2 - WITH abstract domain for truncations):

```

astree moda_dur_3.c --exec-fn main --mod |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:48:09

```

%

*** truncation information derived by Astree:

```

astree moda_dur_3.c --exec-fn main --mod |& egrep --after-context 18 "(launched)|(WARN)|(c
<interval: <> <entree in [-186.1, 186.1], RESULTAT in [-186.1, 186.1]> >
<modulo:
  there exists an integer i in ((entree) - 0.)/1. + [-0.;0.5]
such that: RESULTAT = 1.*i + [-3.33733041202e-13;3.33733041202e-13]
>
<modulo:
  tronc_entier = Arr_0(((entree) - 0.)/1. + [-0.;0.]) + [-0.;0.]
there exists an integer i in ((entree) - 0.)/1. + [-0.5;0.5]
such that: plus_proche = 1.*i + [-3.33733041202e-13;3.33733041202e-13]
there exists an integer i in ((entree) - 0.)/1. + [-1.;8.26450019531e-14]
such that: reste=entree - 1.*i + [-1.66111568944e-13;1.66111568944e-13]
there exists an integer i in ((entree) - 0.)/1. + [-1.;8.26450019531e-14]
such that: plancher = i + [-4.17443857259e-14;4.17443857259e-14]
troncature = Arr_0(((entree) - 0.)/1. + [-0.;0.]) + [-0.;0.]
rapport=((entree) - 0.)/1. + [-8.26450019531e-14;8.26450019531e-14]

```

there exists an integer i in $((\text{entree}) - 0.) / 1. + [-0.5; 0.5]$
such that: $\text{RESULTAT} = 1.*.i + [-3.33733041202e-13; 3.33733041202e-13]$

>
%

```
*****  
* Astree knows about synchronous programming... *  
*****
```

*** incorrect example:

```
cat -n clock-error.c  
1  /* clock-error.c */  
2  int R, T, n = 10;  
3  void main()  
4  { volatile int I;  
5    R = 0;  
6    while (1) {  
7      if (I)  
8        { R = R+1; }  
9      else  
10     { R = 0; }  
11     T = (R>=n);  
12    /* __ASTREE_wait_for_clock(); */  
13  }}
```

*** configuration file:

```
cat -n clock-error.config  
1  /* clock-error.config */  
2  __ASTREE_volatile_input((I [0,1]));
```

*** analysis of the incorrect example by Astree:

```
astree --exec-fn main --config-sem clock-error.config clock-error.c |& egrep "(launched)|(  
/* Analyzer launched at 2006/ 7/12 06:48:14  
clock-error.c:8.12-15::[call#main@3:loop@6>=4:]": WARN: signed int arithmetic range [-214748  
%
```

*** correct example:

```
cat -n clock.c  
1  /* clock.c */  
2  int R, T, n = 10;  
3  void main()  
4  { volatile int I;  
5    R = 0;  
6    while (1) {  
7      if (I)  
8        { R = R+1; }  
9      else  
10     { R = 0; }  
11     T = (R>=n);  
12     __ASTREE_wait_for_clock();  
13  }}
```

*** correction (difference with the incorrect program):

```

1c1
< /* clock-error.c */
---
> /* clock.c */
12c12
< /* __ASTREE_wait_for_clock(); */
---
> __ASTREE_wait_for_clock();

```

*** configuration file:

```

cat -n clock.config
1 /* clock.config */
2 __ASTREE_volatile_input((I [0,1]));
3 __ASTREE_max_clock((3600000));

```

*** analysis of the correct example by Astree:

```

astree --exec-fn main --config-sem clock.config clock.c |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:48:17
%

```

```

*****
* Astree knows about control/command theory... *
*****

```

*** filter example:

```

cat -n filtre.c
1 typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
2 BOOLEAN INIT;
3 float P, X;
4 volatile float RANDOM_INPUT;
5 __ASTREE_volatile_input((RANDOM_INPUT [-10.0,10.0]));
6
7 void filtre2 () {
8     static float E[2], S[2];
9     if (INIT) {
10         S[0] = X;
11         P = X;
12         E[0] = X;
13     } else {
14         P = (((((0.4677826 * X) - (E[0] * 0.7700725)) + (E[1] * 0.4344376)) + (S[0]
15     }
16     E[1] = E[0];
17     E[0] = X;
18     S[1] = S[0];
19     S[0] = P;
20 }
21
22 void main () {
23     X = RANDOM_INPUT;
24     INIT = TRUE;
25     while (TRUE) {
26         X = RANDOM_INPUT;
27         filtre2 ();
28         INIT = FALSE;
29     }
30 }

```

```
*** static analysis by Astree (1 -- WITH 2nd order
    filter domain):
```

```
astree filtre.c --dump-invariants --exec-fn main |& egrep "(launched)|(WARN)|(P in)"
/* Analyzer launched at 2006/ 7/12 06:48:19
```

```
    X in [-10, 10], P in [-13.3881, 13.3881], RANDOM_INPUT in [-10, 10]> >
%
```

```
*** static analysis by Astree (2 -- WITHOUT 2nd order
    filter domain):
```

```
astree filtre.c --exec-fn main --no-filtre2 --dump-invariants |& egrep "(launched)|(WARN)|
/* Analyzer launched at 2006/ 7/12 06:48:21
filtre.c:14.6-114.::[call#main@22:loop@25>=4:call#filtre2@27:]: WARN: double->float conversio
    X in [-10, 10], P in [-3.40282e+38, 3.40282e+38],
```

```
%
```

```
*****
* Astree can analyze low level memory operations *
*****
```

```
*** example 1 (pointer casts):
```

```
cat -n memcpy.c
1  /* memcpy.c (polymorphic memcpy) */
2
3  /* byte per byte copy of src into dst */
4  void memcpy(char* dst, const char* src, unsigned size)
5  {
6      int i;
7      for (i=0;i<size;i++) dst[i] = src[i];
8  }
9
10 void main()
11 {
12     float x = 10.0, y;
13     int zero = 0;
14     /* copy of x into y (well-typed) */
15     memcpy(&y,&x,sizeof(y));
16     __ASTREE_assert((y==10.0));
17     /* copy of zero into y (not well-typed but allowed in C) */
18     memcpy(&y,&zero,sizeof(y));
19     __ASTREE_assert((y==0.0));
20 }
```

```
*** static analysis by Astree:
```

```
astree --exec-fn main --unroll 5 memcpy.c |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:48:23
%
```

```
*** example 2 (unions):
```

```
cat -n union.c
1  /* union.c (union type) */
```

```

2
3 union {
4     int type;
5     struct { int type; int data; } A;
6     struct { int type; char data[3]; } B;
7 } u;
8
9 void main()
10 {
11     /* no assert failure */
12     u.type = 12;
13     __ASTREE_assert((u.A.type==12));
14     __ASTREE_assert((u.B.type==12));
15
16     /* assert failure because the modification of u.B.data also modifies u.A.data */
17     u.A.data = 0;
18     u.B.data[0] = 12;
19     __ASTREE_assert((u.A.data==0));
20 }

```

*** static analysis by Astree:

```

astree --exec-fn main --full-memory-model union.c |& egrep "(launched)|(WARN)"
/* Analyzer launched at 2006/ 7/12 06:48:25
union.c:19.19-30::[call#main@9:]: WARN: assert failure
%

```

```

*****
* Astree has a graphic interface under X11... *
*****

```

tcsh: /bin/rm: No match.

*** static analysis by Astree

```

astree filtre.c --dump-invariants --exec-fn main --export-invariant-stat --export-file fil
%

```

*** visualization of the results:

```

visu --text-size 14 --text-font CMTT filtre.inv >& /dev/null &
[1] 13075
%

```

*** (scaling up with GTK+ (library to build graphical user interfaces (GUIs) originally for X Window!))

```

*****
*** The end, thank you for your attention ***
*****

```

Publications/2006-Dagstuhl-06281/Cousot-Dagstuhl-06281_demonstration % ^Dexit

Script done on Wed Jul 12 08:48:32 2006