

### Abstract

Static software analysis has known brilliant successes in the small, by proving complex program properties of programs of a few dozen or hundreds of lines, either by systematic exploration of the state space or by interactive deductive methods. To scale up is a definite problem. Very few static analyzers are able to scale up to millions of lines without sacrificing soundness and/or precision. Unsound static analysis may be useful for bug finding but is less useless in safety critical applications where the absence of bugs, at least of some categories of common bugs, should be formally verified.

After recalling the basic principles of abstract interpretation including the notions of abstraction, approximation, soundness, completeness, false alarm, etc., we introduce the domainspecific static analyzer ASTRÉE (www.astree.ens.fr) for proving the absence of runtime errors in safety critical real time embedded synchronous software in the large. The talk emphasizes soundness (no runtime error is ever omitted), parametrization (the ability to refine abstractions by options and analysis directives), extensibility (the easy incorporation of new abstractions to refine the approximation), precision (few or no false alarms for programs in the considered application domain) and scalability (the analyzer scales to millions of lines).

In conclusion, present-day software engineering methodology, which is based on the control of the design, coding and testing processes should evolve in the near future, to incorporate a systematic control of final software product thanks to domain-specific analyzers that scale up

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\_ 2 \_

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All Computer Scientists Have Experienced Bugs





Ariane 5.01 failure Patriot failure (overflow)

(float rounding)

Mars orbiter loss (unit error)

It is preferable to verify that mission/safety-critical programs do not go wrong before running them.

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— 4 —

# Principle of program verification

- Define a semantics of the language (that is the effect of executing programs of the language)
- Define a specification (example: absence of runtime errors such as division by zero, arithmetic overflow, etc)
- Make a formal proof that the semantics satisfies the specification
- Use a computer to automate the proof
- By undecidability<sup>(1)</sup>, some form of approximation is inevitable!

#### Abstract Interpretation 2.

\_\_\_\_ Reference

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[1] P. Cousot. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes. Thèse d'État ès sciences mathématiques. Université scientifique et médicale de Grenoble. 1978.

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## The Theory of Abstract Interpretation

- A theory of sound approximation of mathematical structures, in particular those involved in the description of the behavior of computer systems
- Systematic derivation of sound methods and algorithms for approximating undecidable or highly complex problems in various areas of computer science
- Main practical application is on the safety and security of complex hardware and software computer systems
- Abstraction: extracting information from a system description that is relevant to proving a property

— 7 —

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#### Applications of Abstract Interpretation

- Static Program Analysis [CC77], [CH78], [CC79] including Dataflow Analysis; [CC79], [CC00], Set-based Analysis [CC95], Predicate Abstraction [Cou03], ...
- Grammar Analysis and Parsing [CC03];
- Hierarchies of Semantics and Proof Methods [CC92b], [Cou02];
- Typing & Type Inference [Cou97];
- (Abstract) Model Checking [CC00];
- Program Transformation (including program optimization, partial evaluation, etc) [CC02];

\_ 8 \_

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<sup>(1)</sup> there are infinitely many programs for which a computer cannot prove them in finite time even with an infinite memory. — 5 —









# Example 1: CBMC

- CBMC is a Bounded Model Checker for ANSI-C programs (started at CMU in 1999).
- Allows verifying array bounds (buffer overflows), pointer safety, exceptions and user-specified assertions.
- Aimed for embedded software, also supports recursion and dynamic memory allocation using malloc.
- Done by unwinding the loops in the program and passing the resulting equation to a SAT solver.
- Problem (a.o.): does not scale up!



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— 25 —

- Coverity Prevent<sup>™</sup> Static Analysis offers (dixit) "the most precise static source code analysis solution available today" (started at Stanford by Dawson Engler around 2000).
- "Average false positive (FP) rate of about 15%, with some users reporting FP rates of as low as 5%."
- Integers overflows, arrays & pointer errors, memory leaks, deadlocks, race conditions, etc.
- Bug finding by local pattern matching, condition checking by SAT solver, and showing up the most probable errors.
- Problem (a.o.): not sound, imprecise and endless! MPI. 8/26/2008

- 26 -

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# Example 3: ASTRÉE

- ASTRÉE is an abstract interpretation-based static analyzer for ANSI-C programs (started at ENS in 2001).
- Allows verifying array bounds (buffer overflows), pointer safety, exceptions and user-specified assertions.
- Aimed for embedded software, does not support recursion and dynamic memory allocation.

— 27 —

- Done by abstracting the reachability fixpoint equations for the program operational semantics.
- Advantage (a.o.): sound, precise, and does scale up but domain-specific!



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5. Precision

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# **Required** Precision

- Coverity Prevent<sup>™</sup> Static Analyzer has "an average FP rate of about 15%, with some users reporting FP rates of as low as 5%" [www.coverity.com/html/prevent-for-c-features.html]
- Consider a 1.000.000 LOCS control/command safety critical program, with 1 potential error per line (often much more)
- -5% FP = 5.000 false positives
- In safety critical software, false alarms must be justified for certification
- False/true alarms can take hours to days to be solved  $\implies$  the cost is several man  $\times$  years!

— 29 —

Scaling up

— 30 —

6.

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# Undecidability and complexity

- The mathematical proof problem is undecidable
- Even assuming finite states, the complexity is much too high for combinatorial exploration to succeed
- Example: 1.000.000 lines  $\times$  50.000 variables  $\times$  64 bits  $\simeq 10^{27}$  states
- Exploring  $10^{15}$  states per seconde, one would need  $10^{12}$  s > 300 centuries (and a lot of memory)!

— 31 —

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# A typical small control/command program ...

	1 typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
	2 BOOLEAN INIT; float P, X;
	3 void filter () {
	4 static float E[2], S[2];
	5 if (INIT) { S[0] = X; P = X; E[0] = X; }
	6 else { $P = (((((0.5 * X) - (E[0] * 0.7)) + (E[1] * 0.4)))$
	7 + $(S[0] * 1.5)) - (S[1] * 0.7)); \}$
	8 $E[1] = E[0]; E[0] = X; S[1] = S[0]; S[0] = P;$
	9 /* P in [-1325.4522, 1325.4522] */
	10 }
	11 int main () {
	12 int i = 1; X = 5.0; INIT = TRUE;
	13 while (i < 3600000) {/* simulated 10ms clock tick for 10 hours */
	14 X = 0.9 * X + 35; /* simulated filter input */
	15 filter (); INIT = FALSE; i++; }
	16 }
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# ... Analysis with CBMC

Script started on Tue Jul 29 23:44:00 2008 % time ./cbmc filter.c

Starting Bounded Model Checking Unwinding loop 1 iteration 1 Unwinding loop 1 iteration 2

Unwinding loop 1 iteration 95479 cbmc(34799) malloc: \*\*\* mmap(size=2097152) failed (error code=12) \*\*\* error: can't allocate region \*\*\* set a breakpoint in malloc\_error\_break to debug terminate called after throwing an instance of 'std::bad\_alloc' what(): St9bad alloc

# Abort

29668.051u 101.916s 8:20:41.88 99.0% 0+0k 1+10io 2680pf+0w % ^Dexit Script20cone on Wed Jul 30 09:08:5832008

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### The difficulty of scaling up

- The abstraction must be coarse enough to be effectively computable with reasonable resources
- The abstraction must be precise enough to avoid false alarms
- Abstractions to infinite domains with widenings are more expressive than abstractions to finite domains<sup>(3)</sup> (when considering the analysis of a programming language) [CC92a]
- Abstractions are ultimately incomplete (even intrinsically for some semantics and specifications [CC00])

(3) e.g. predicate abstraction which always abstract to a finite domain MPI. 8/26/2008 — 35 —

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# ... Analysis with ASTRÉE

% diff -U1 filter.c filter-a.c -- filter.c 2008-07-30 11:33:13.000000000 +0200 +++ filter-a.c 2008-07-30 12:22:26.000000000 +0200 @@ -8.2 +8.3 @@ E[1] = E[0]; E[0] = X; S[1] = S[0]; S[0] = P;+ \_\_ASTREE\_log\_vars((P)); /\* P in [-1325.4522, 1325.4522] \*/

Fast:

% (time astree -exec-fn main filter-a.c) |& egrep "WARN|pf+" 0.710u 0.085s 0:01.47 53.7% 0+0k 7+7io 840pf+0w

#### %

- Precise:

% astree -exec-fn main filter-a.c |& grep "P in" | tail -n1 direct = <float-interval: P in [-1325.4522, 1325.4522] >

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## A common believe on static analyzers

"The properties that can be proved by static analyzers are often simple" [2]

Like in mathematics:

- May be simple to state (no overflow)
- But harder to discover  $(P \in [-1325.4522, 1325.4522])$
- And difficult to prove (since it requires finding a non trivial non-linear invariant for second order filters with complex roots [Fer04], which can hardly be found by exhaustive enumeration)

\_\_\_\_ Reference \_

<sup>[2]</sup> Vijay D'Silva, Daniel Kroening, and Georg Weissenbacher. A Survey of Automated Techniques for Formal Software Verification. IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems, Vol. 27, No. 7, July 2008. 

7. Soundness	8. Abstraction Completion / Refinement
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Is the virtue of soundness a myth? Why bother about soundness since automatic static an cannot prove total correctness anyway? Finding as man	Abstraction completion - Completion is the process of refining an abstraction of a seman-
<ul> <li>as possible is the most direct approximation! [3]</li> <li>We can focus on a well-defined category of bugs (e.g. r errors, time overrun, etc)</li> </ul>	runtime - In theory, always possible by an infinite fixpoint computation in the concrete! [Cou00, GRS00] - In complicated cases, the most abstract complete refined ab-
<ul> <li>And ensure <u>no</u> bug is left in this category</li> <li>And, more importantly, know when the verification she stopped for that category of bugs (contrary to unsound ods like testing/bug finding)</li> </ul>	.ould be .d meth- .d meth- .d meth- .counter-example-guided abstraction refinement [CGJ <sup>+</sup> 00] .fixpoint abstraction refinement [CGR07]



### Analysis by Astrée

```
% cat modulo-a.c
int main () {
    float m, M, x, y;
M = 4095.0; m = -M;
x = 4094.9997558593750; /* largest float strictly less than M */
    y = x - (int) ((x-m)/(M-m))*(M-m);
__ASTREE_log_vars((y));
}
% astree -exec-fn main -print-float-digits 25 modulo-a.c |& grep "y in"
direct = <float-interval: y in [-4095.000244140625, 4094.999755859375] >
%
```

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— 45 —

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#### Analysis by ASTRÉE

```
% cat -n unpreditable-a.c
1 const int false = 0;
2 int main () { int n, T[1], x;
3 n = 1;
4 x = T[n];
5 ___ASTREE_assert((false));
6 }
% astree -exec-fn main unpreditable-a.c |& grep "WARN"
unpreditable-a.c:4.4-8::[call#main@2:]: WARN: invalid dereference: dereferencing
4 byte(s) at offset(s) [4;4] may overflow the variable T of byte-size 4
%
No alarm on assert(false) because execution is assumed to stop after a definite
runtime error with unpredictable results<sup>(4)</sup>.
```

(4) Equivalent semantics if no alarm.

```
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```

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## The Semantics of C is Hard (Ex. 2: Runtime Errors)

What is the effect of out-of-bounds array indexing?

```
% cat unpredictable.c
#include <stdio.h>
int main () { int n, T[1];
    n = 2147483647;
    printf("n = %i, T[n] = %i\n", n, T[n]);
}
```

#### Yields different results on different machines:

```
n = 2147483647, T[n] = 2147483647 Macintosh PPC
n = 2147483647, T[n] = -1208492044 Macintosh Intel
n = 2147483647, T[n] = -135294988 PC Intel 32 bits
Bus error PC Intel 64 bits
```

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— 46 —

## Different Classes of Run-time Errors

— 47 —

- 1. Errors terminating the execution <sup>(5)</sup>. ASTRÉE warns and continues by taking into account only the executions that did not trigger the error.
- Errors not terminating the execution with predictable outcome<sup>(6)</sup>. ASTRÉE warns and continues with worst-case assumptions.
- 3. Errors not terminating the execution with <u>unpredictable</u> outcome<sup>(7)</sup>. ASTRÉE warns and continues by taking into account only the executions that did not trigger the error.

 $\Rightarrow$  ASTRÉE is sound with respect to C standard, unsound with respect to C implementation, unless no false alarm of type 3.

\_\_\_\_ 48 \_\_\_\_

```
(5) floating-point exceptions e.g. (invalid operations, overflows, etc.) when traps are activated
```

(6) e.g. overflows over signed integers resulting in some signed integer.

(7) e.g. memory corruptionss.

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10. Specification	11. The design of ASTRÉE for soundness, precision, scalability, and refinability		
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Implicit Specification: Absence of Runtime Errors	Modular refinable abstraction		
The static analyzer should definitely guarantee the absence of - violations of the norm of C (e.g. array index out of bounds, division by zero, nil/dangling pointer dereferencing)	<ul> <li>The abstract semantics is decomposed into:</li> <li>A structural fixpoint iterator (by composition on the program syntax)</li> <li>A collection of parametric abstract domains with: <ul> <li>parameters to adjust the expressivity of the abstraction</li> <li>parametric convergence acceleration (parameters to adjust the frequence and precision of widenings/narrowings)</li> <li>analysis directives (to locally adjust the choice of abstractions)</li> <li>A reduction performing the conjunction of the abstractions</li> </ul> </li> </ul>		
<ul> <li>implementation-specific undefined behaviors (e.g. maximum short integer is 32767, NaN)</li> <li>violations of the programming guidelines (e.g. no modulo arithmetics for signed integers)</li> <li>violations of the programmer assertions (must all be statically verified).</li> <li>for all reachable states during any execution <sup>(8)</sup></li> </ul>	<ul> <li>- parametric convergence acceleration (parameters to adjust the frequence and precision of widenings/narrowings)</li> <li>- analysis directives (to locally adjust the choice of abstractions)</li> <li>- A reduction performing the conjunction of the abstractions</li> <li>⇒ Easily refinable by parameter/directive adjustment and ex-</li> </ul>		

12. Iterator	13. General Abstract Domains		
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<ul> <li>Characterization of the iterator</li> <li>structural (by induction on the program syntax)</li> <li>flow sensitive (the execution order of statements is taken into account)</li> <li>path sensitive (distinguishes between feasible paths through a program)</li> <li>context sensitive (function calls are analyzed differently for each call site)</li> <li>interprocedural (function bodies are analyzed in the context of each respective call site)</li> </ul>	Semantics x(t) f f f f f f f f f f		
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#### Parameterized abstractions - Parameterize the cost / precision ratio of abstractions in the static analyzer - Examples: - array smashing: --smash-threshold n (400 by default) $\rightarrow$ smash elements of arrays of size > n, otherwise individu-18. Refinement by Analysis Directives alize array elements (each handled as a simple variable). - packing in octogons: (to determine which groups of variables are related by octagons and where) · --fewer-oct: no packs at the function level, · --max-array-size-in-octagons n: unsmashed array elements of size > n don't go to octagons packs © P. Cousot MPI. 8/26/2008 — 71 — MPI. 8/26/2008 — 73 — © P. Cousot Analysis directives Parameterized widenings - Parameterize the rate and level of precision of widenings in the - Require a local refinement of an abstract domain static analyzer - Example: - Examples: - delayed widenings: --forced-union-iterations-at-beginning n (2) % cat repeat1.c typedef enum {FALSE=0,TRUE=1} BOOL; by default) int main () { - enforced widenings: --forced-widening-iterations-after n (250) int x = 100; BOOL b = TRUE; by default) while (b) { - thresholds for widening (e.g. for integers): x = x - 1;b = (x > 0);3 let widening\_sequence = 3 [ of\_int 0; of\_int 1; of\_int 2; of\_int 3; of\_int 4; of\_int 5; % astree -exec-fn main repeat1.c |& egrep "WARN" of\_int 32767; of\_int 32768; of\_int 65535; of\_int 65536; repeat1.c:5.8-13::[call#main@2:loop@4>=4:]: WARN: signed int arithmetic of\_string "2147483647"; of\_string "2147483648"; range [-2147483649, 2147483646] not included in [-2147483648, 2147483647] of\_string "4294967295" ] % MPI. 8/26/2008 — 72 — MPI. 8/26/2008 \_ 74 \_ (c) P. Cousot © P. Cousot



# Example of abstract domain introduced in ASTRÉE Adding new abstract domains - Design the mathematical abstract domain Overapproximation with an arithmetico-geometric series: - Specify the concretization, and f(k) - Implement: max I f(k) $k \le \max k$ - the representation of the (parameterized) abstract properties - the abstract property transformers for language primitives - (parameterized) widening max k - reduction with other abstractions - Examples : ellipsoids for filters [Fer05b], exponentials for accumulation of small rounding errors [Fer05a], quaternions, ... © P. Cousot MPI. 8/26/2008 — 79 — © P. Cousot MPI. 8/26/2008 - 81 -Arithmetico-geometric series<sup>(12)</sup> [Fer05a] - Abstract domain: $(R^+)^5$ - Concretization: $\gamma \in (R^+)^5 \longmapsto \wp(N \mapsto R)$ $\gamma(M,a,b,a',b') =$ 20. Refinement by Extension $\{f \mid orall k \in N: |f(k)| \leq \left(oldsymbol{\lambda} x \cdot ax + b \circ (oldsymbol{\lambda} x \cdot a'x + b')^k ight)(M)\}$ i.e. any function bounded by the arithmetic-geometric progression. [4] J. Feret. The arithmetic-geometric progression abstract domain. In VMCAI'05, Paris, LNCS 3385, pp. 42-58, Springer, 2005. (12) here in R but must be implemented in the floats by appropriate roundings! MPI, 8/26/2008 - 80 -© P. Cousot MPI. 8/26/2008 — 82 — © P. Cousot



	22. Conclusion		THE END Thank you for your attention		
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<ul> <li>Static analysis domain-specific</li> <li>In consequence in the near fut</li> <li>From the prea the design, co</li> <li>To a product control of the</li> </ul>	Conclusion by abstract interpretation industrial software , software engineering method ure: sent-day process-based metho oding and testing processes -based methodology incorpor e final software product by st	does scale up for ology should evolve dology controlling ating a systematic atic analyzers.		23. Bibliography	
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MPI, 8/26/2008

— 93 —

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MPI, 8/26/2008

— 94 —

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#### MPI, 8/26/2008

— 96 —

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