Abstract Interpretation

SAVE 2016, Changsha, 10 December 2016



This is an abstract interpretation

Universités **Colloquium d'Informatique** Abstract interpretation **Patrick Cousot** New York University Amphi 15 4, place Jussieu 75005 Paris **Metro Jussieu** Sorbonne 29 Septembre 2016 à 18h00 The complexity of large programs grows faster than the intellectual ability of programmers in charge of their development and maintenance. The direct consequence is a lot of errors and bugs in programs mostly debugged by their end-users. Programmers are not responsible for these bugs. They are not required to produce provably safe and secure programs. This is because professionals are only required to apply state of the art techniques, that is testing on finitely many cases. This state of the art is changing rapidly and so will irresponsibility, as in other manufacturing disciples. e l'UPMC Scalable and cost-effective tools have appeared recently that can avoid bugs with possible dramatic consequences for example in transportation, banks, privacy of social networks, etc. Entirely automatic, they are able to capture all bugs involving the violation of software healthiness rules such as the use of operations with arguments for which they are undefined. These tools are formally founded on abstract interpretation. They are based on a definition of the semantics of programming languages specifying all possible executions of the programs of a language. Program properties of interest are abstractions of these semantics abstracting away all aspects of the semantics not relevant to a particular reasoning on programs. This yields proof methods. Full automation is more difficult because of undecidability: programs cannot always prove programs correct in finite time and memory. Further abstractions are therefore necessary for automation, which introduce imprecision. Bugs may be signalled that are impossible in any execution (but still none is forgotten). This has an economic cost, much less than testing. Moreover, the best static analysis tools are able to reduce these false alarms to almost zero. A time-consuming and error-prone task which is too difficult, if not impossible for programmers, without tools. Patrick Cousot received the Doctor Engineer degree in Computer Science and the Doctor ès Sciences degree in Mathematics from the University Joseph Fourier of Grenoble, France. He was a Research Scientist at the French National Center for Scientific Research at the University Joseph Fourier of Grenoble, France, then professor at the University of Metz, the École Polytechnique, the École Normale Supérieure, Paris, France. He is Silver Professor of Computer Science at the Courant Institute of Mathematical Sciences, New York University, USA. Patrick Cousot is the inventor, with Radhia Cousot, of Abstract Interpretation. SOPRONNE UNIVERSITÉ

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Scientific research

Scientific research

• In Mathematics/Physics:

trend towards unification and synthesis through universal principles

• In Computer science:

trend towards dispersion and parcellation through a ever-growing collection of local ad-hoc techniques for specific applications

An exponential process, will stop!

Example: reasoning on computational structures

WCET Operational Security protocole Systems biology semantics Axiomatic verification analysis semantics Abstraction Model Dataflow Database refinement Confidentiality checking analysis query analysis Туре Partial Obfuscation Dependence inference Program evaluation analysis synthesis Separation Denotational Effect logic CEGAR Grammar semantics systems Termination analysis Program Theories Trace proof combination Statistical transformation semantics model-checking Shape Interpolants Abstract Code analysis Invariance model Symbolic Integrity contracts proof checking execution Malware analysis detection **Probabilistic** Quantum entanglement **Bisimulation** Code verification detection **SMT** solvers refactoring Type theory Steganography Parsing Tautology testers

Example: reasoning on computational structures

(WCET Security protocole Systems biology Operational
	Axiomatic vanification 0/sterns biolog/ semantics
	semantics Abstraction
	Confidentiality Dataflow Model Database refinement
	analysis Partial Obfuscation Dependence information
	Program evaluation Obfuscation Dependence inference
	synthesis Effect Denotational analysis Separation
I	Grammar systems semantics CEGAR logic
	analysis – Theories Program Termination
	Statistical Trace combination transformation Proof
	model-checking semantics Code Interpolants Abstract Shape
	Invariance Symbolic contracts Integrity model analysis
	proof execution analysis checking Malware
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Example: reasoning on computational structures

Abstract interpretation

WCET Operational Security protocole Systems biology semantics Axiomatic verification analysis semantics Abstraction Model Dataflow Database refinement Confidentiality checking analysis query analysis Туре Partial **Obfuscation** Dependence inference Program evaluation analysis Separation synthesis Denotational Effect logic CEGAR Grammar semantics systems Termination analysis Theories Program Trace proof Statistical combination transformation semantics model-checking Shape Interpolants Abstract Code analysis Invariance model Symbolic Integrity contracts proof checking Malware execution analysis detection **Probabilistic** Quantum entanglement **Bisimulation** Code verification detection SMT solvers Type theory Steganography Tautology testers refactoring Parsing

Intuition I

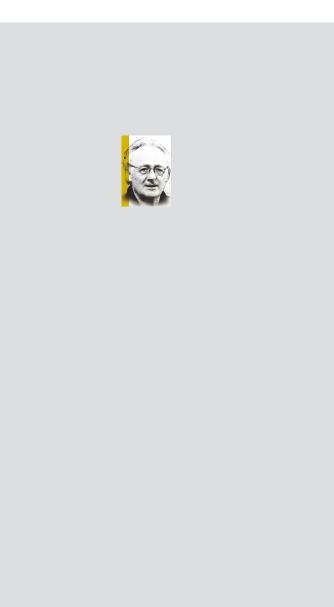




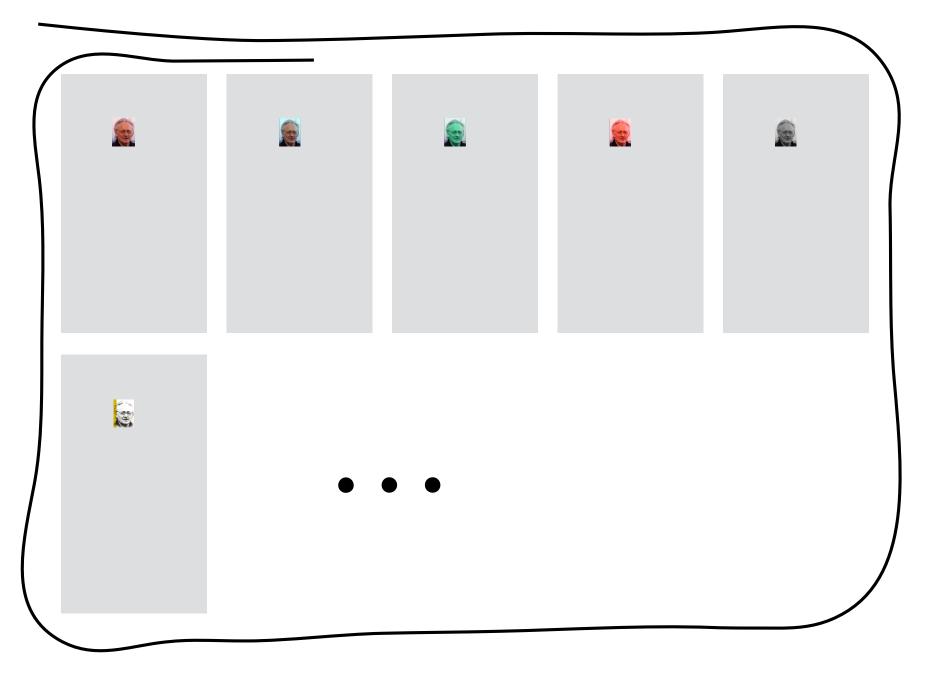
Abstraction I



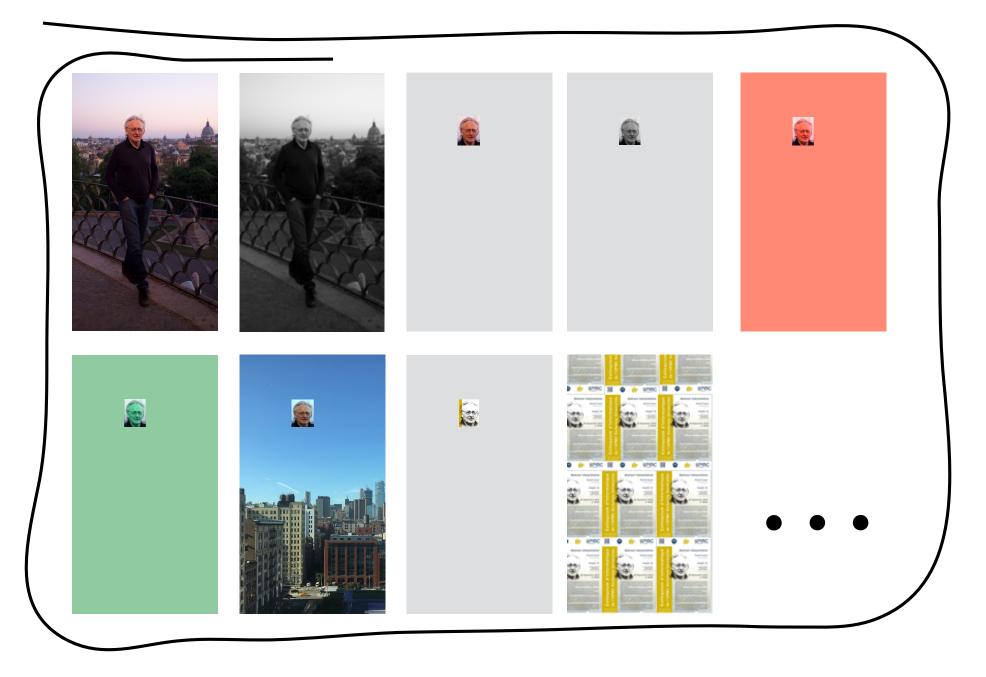
Abstraction 2



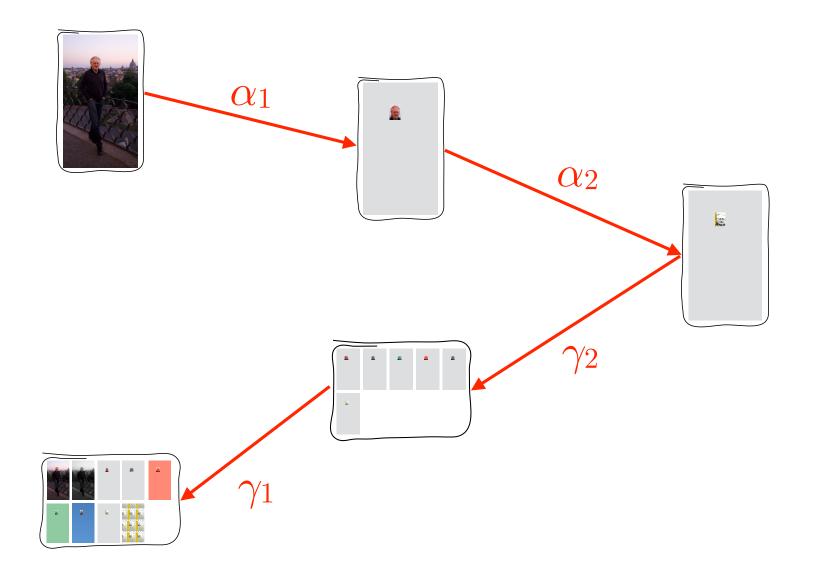
Concretization 2



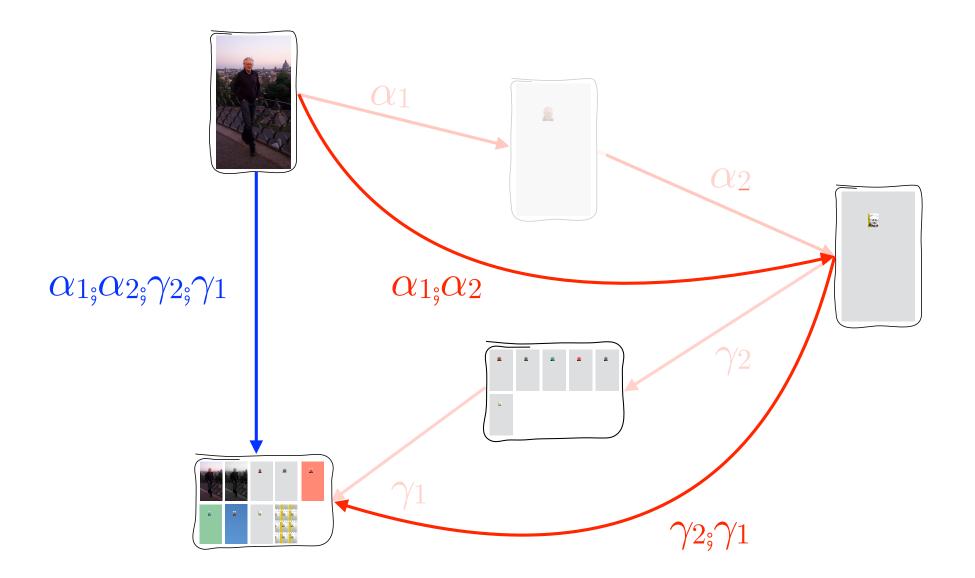
Concretization I



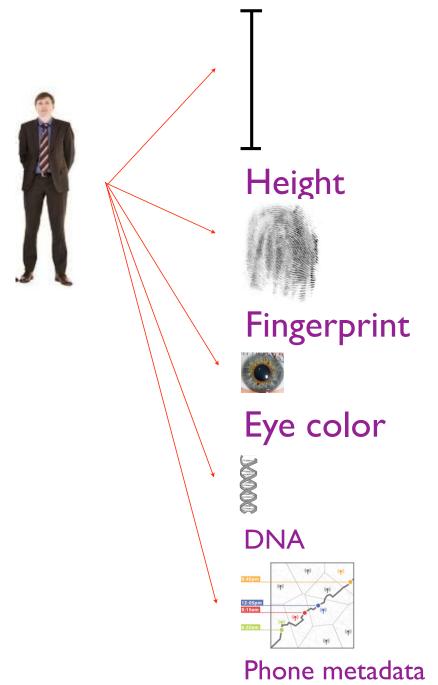
Abstract interpretations

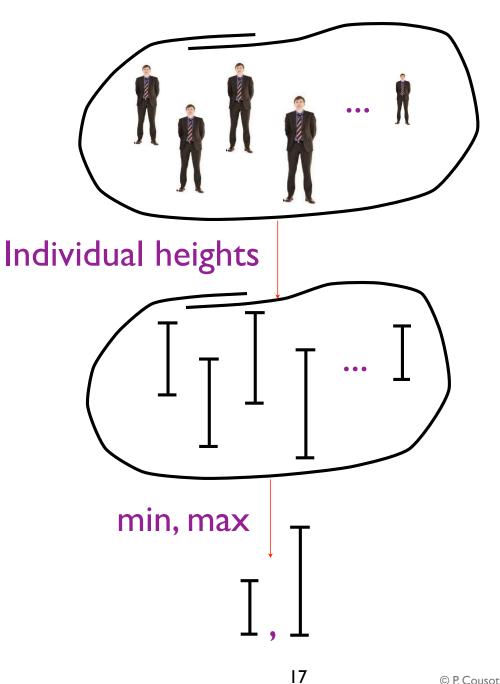


Abstract interpretations



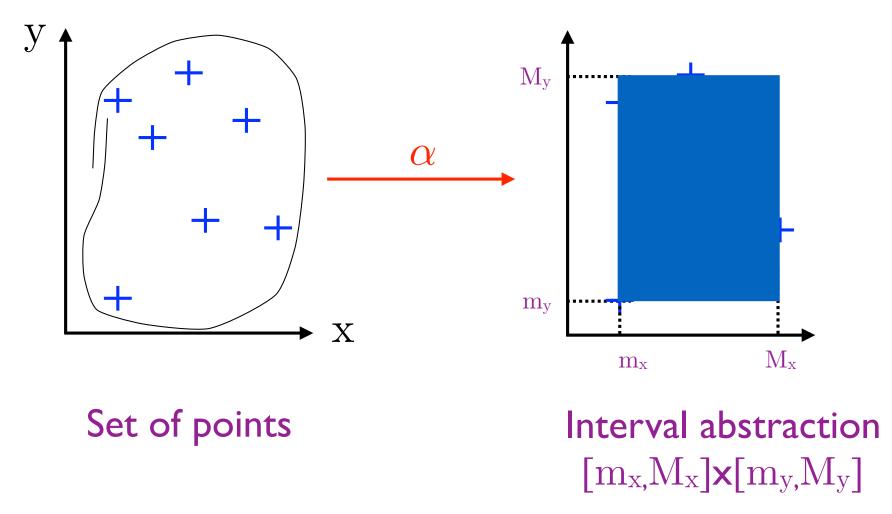
Intuition 2





Interval abstraction

 Example: interval abstraction (also called box abstraction)

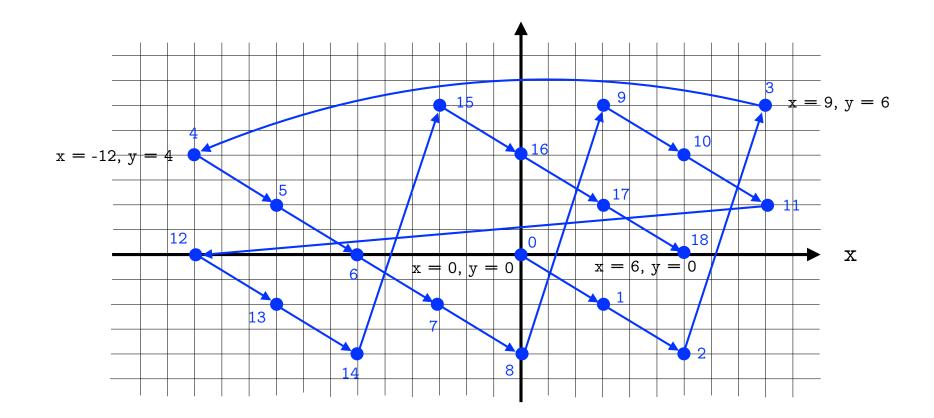


Intuition 3

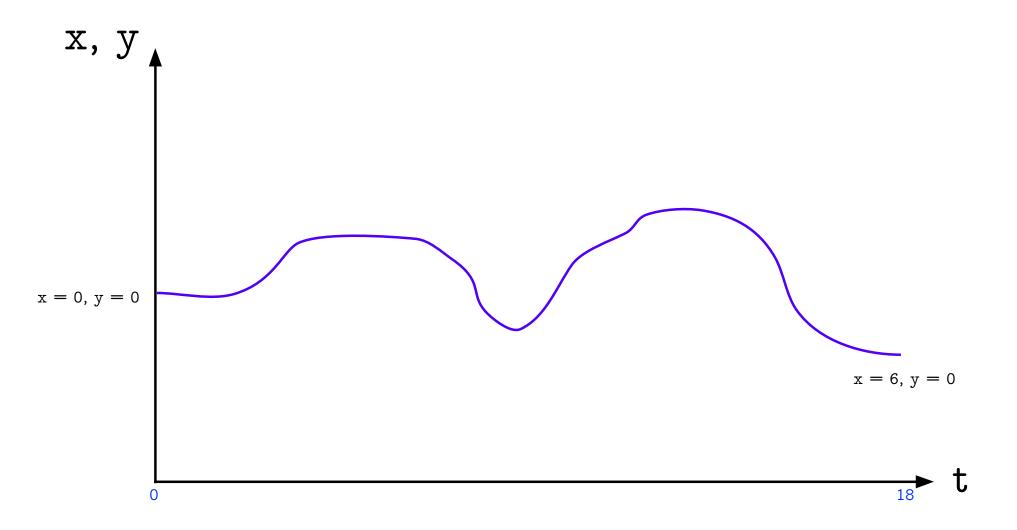
A C program and one of its executions

Enter two integers: $x = 0, y = 0$
x = 3, y = -2
x = 6, y = -4
x = 9, y = 6
x = -12, y = 4
x = -9, y = 2
x = -6, y = 0
x = -3, y = -2
x = 0, y = -4
x = 3, y = 6
x = 6, y = 4
x = 9, y = 2
x = -12, y = 0
x = -9, y = -2
x = -6, y = -4
x = -3, y = 6
x = 0, y = 4
x = 3, y = 2
x = 6, y = 0

Graphical representation of the execution (I)

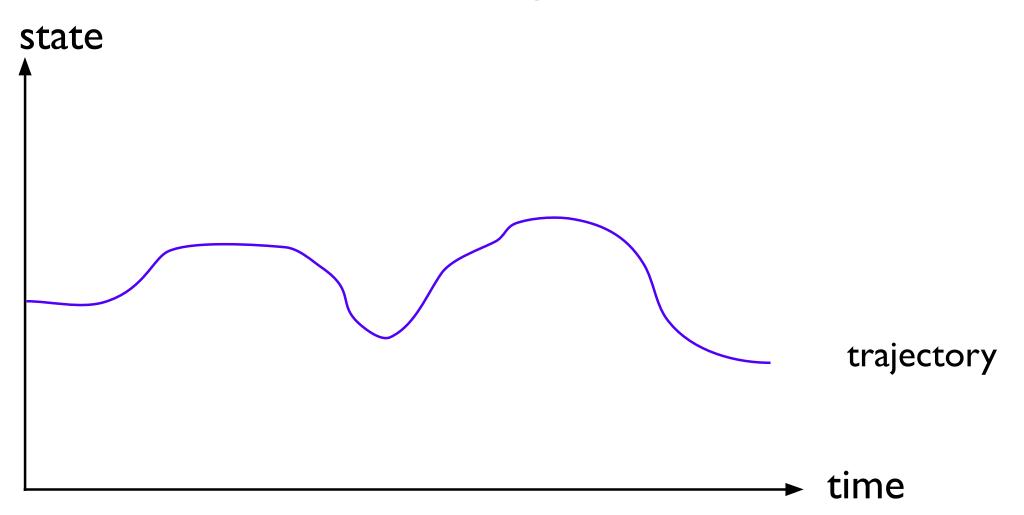


Graphical representation of the execution (2)



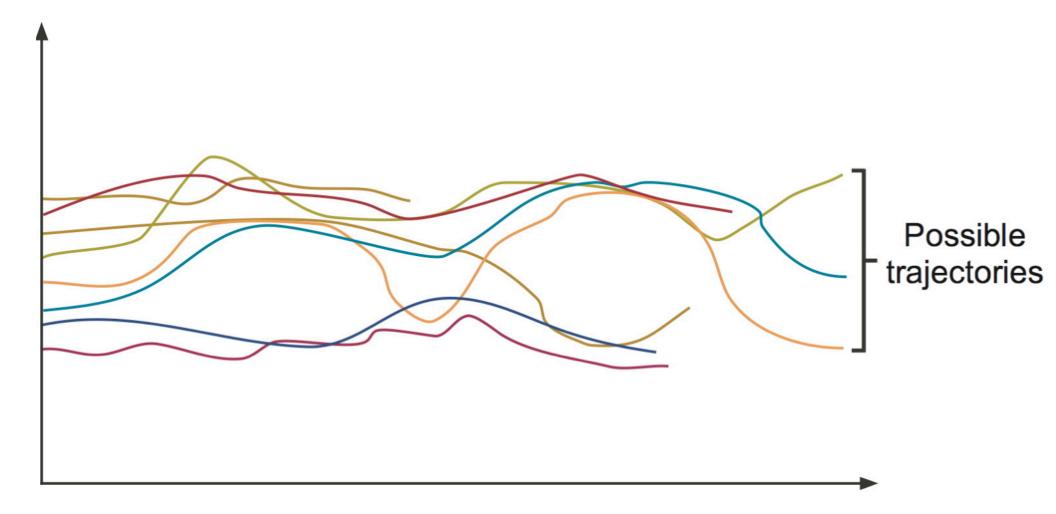
Semantics

Formalize what it means to run a program



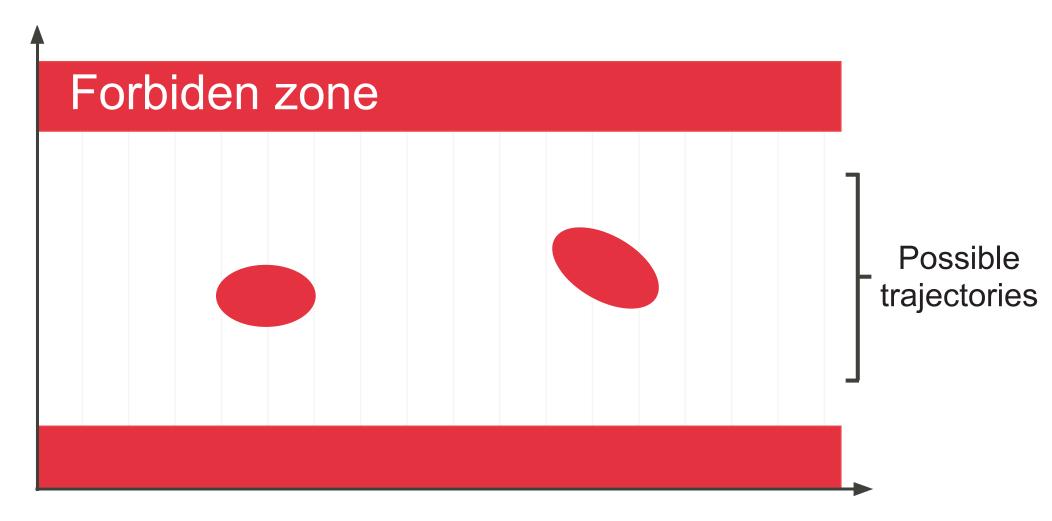
Properties (Collecting semantics)

Formalize what you are interested to **know** about program behaviors



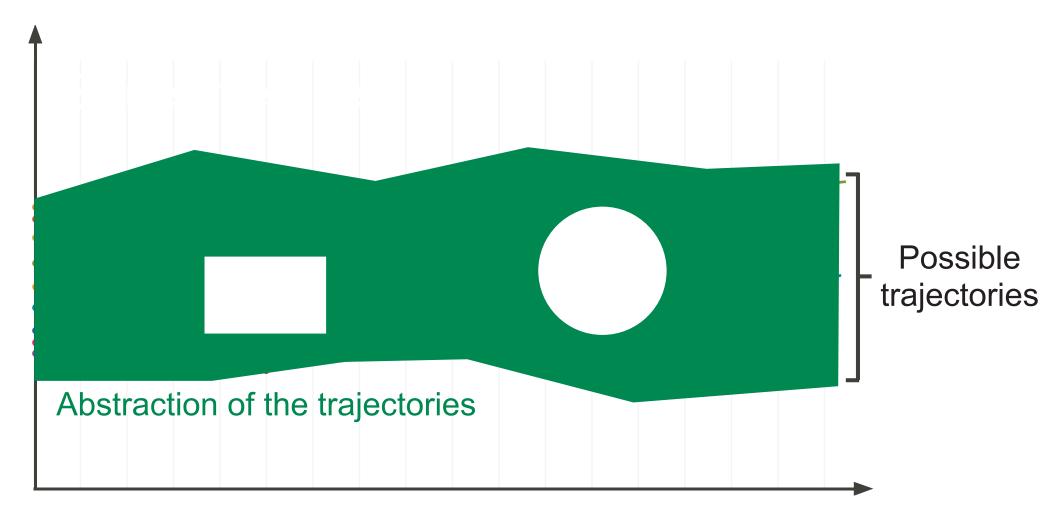
Specification

Formalize what you are interested to **prove** about program behaviors



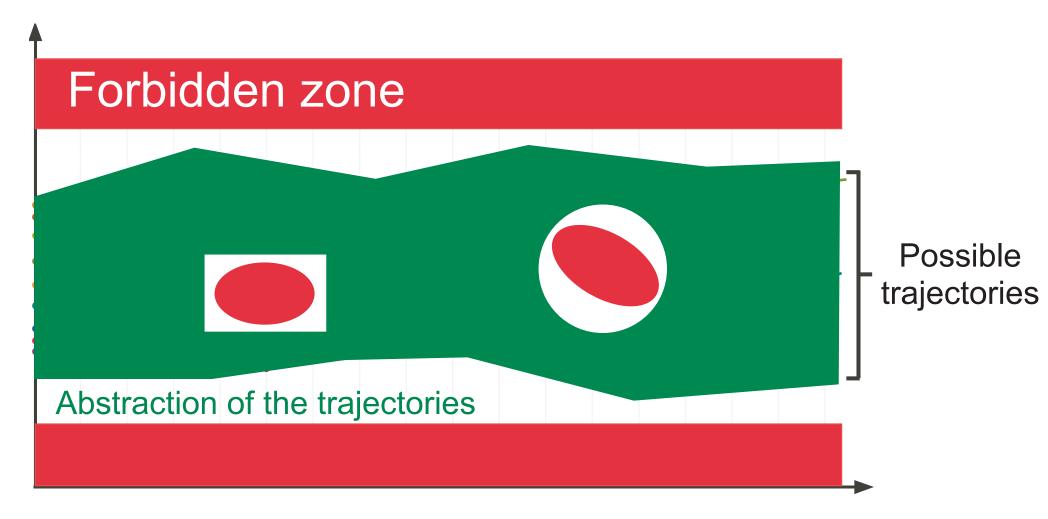
Abstraction

Abstract away all information on program behaviors irrelevant to the proof



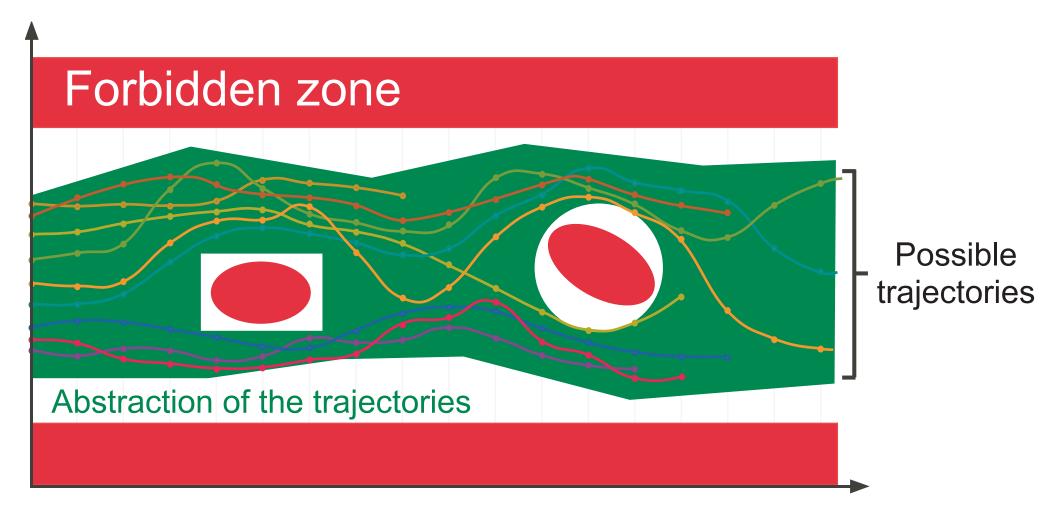
Verification

The proof is fully **automatic**



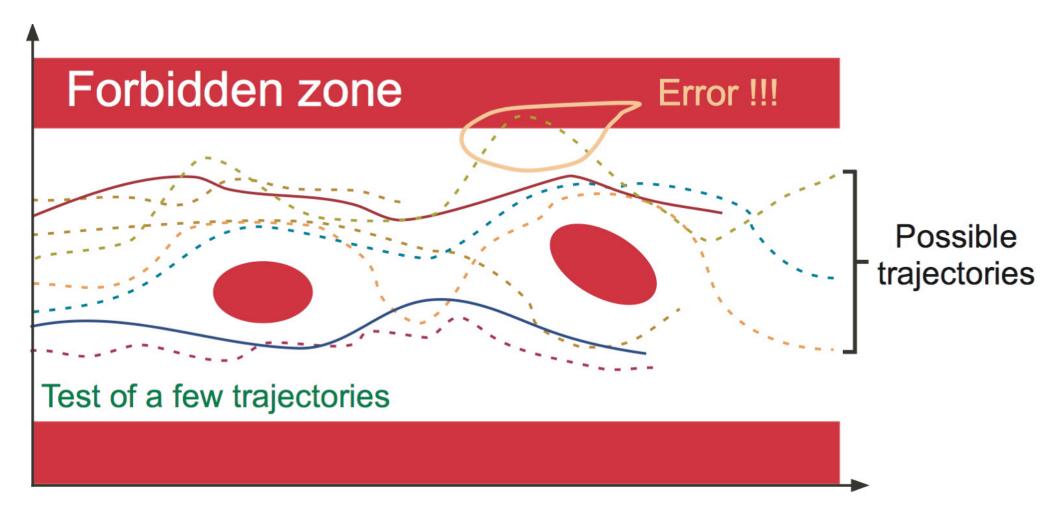
Soundness

Never forget any possible case so the **abstract proof is correct in the concrete**



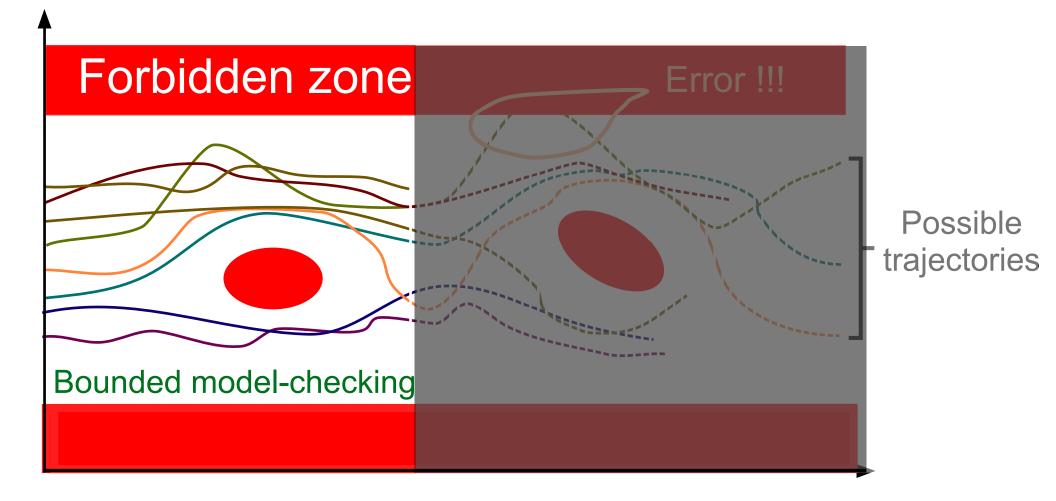
Unsound methods: testing

Try a few cases



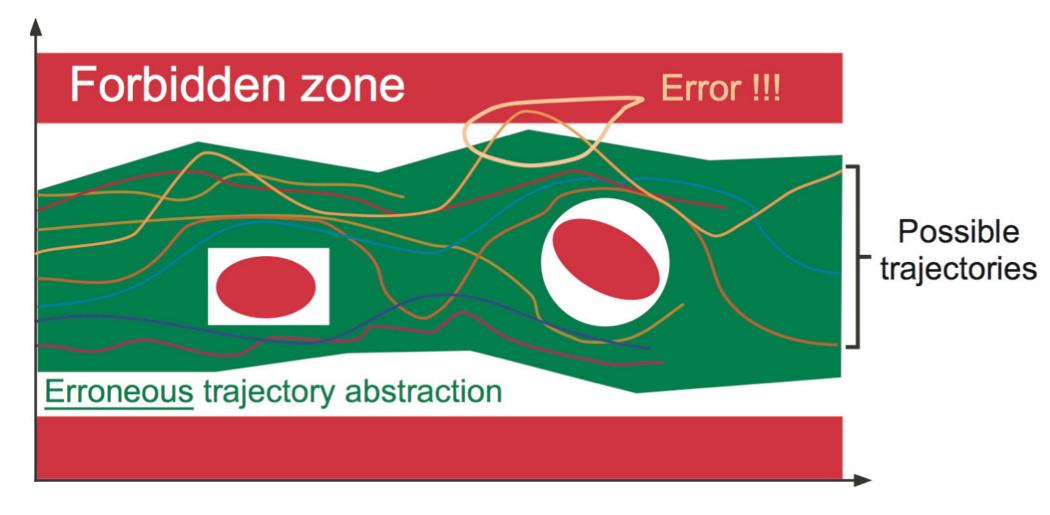
Unsound methods: bounded model checking

Simulate the beginning of all executions (so called bounded model-checking)



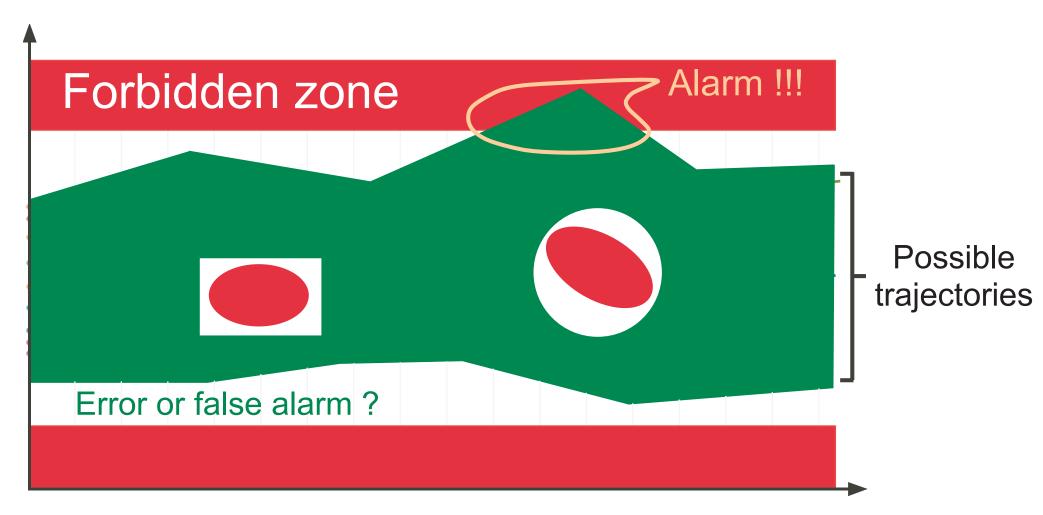
Unsound methods: soundiness

Many static analysis tools are **unsound** (e.g. Coverity, etc.) so inconclusive



Alarms

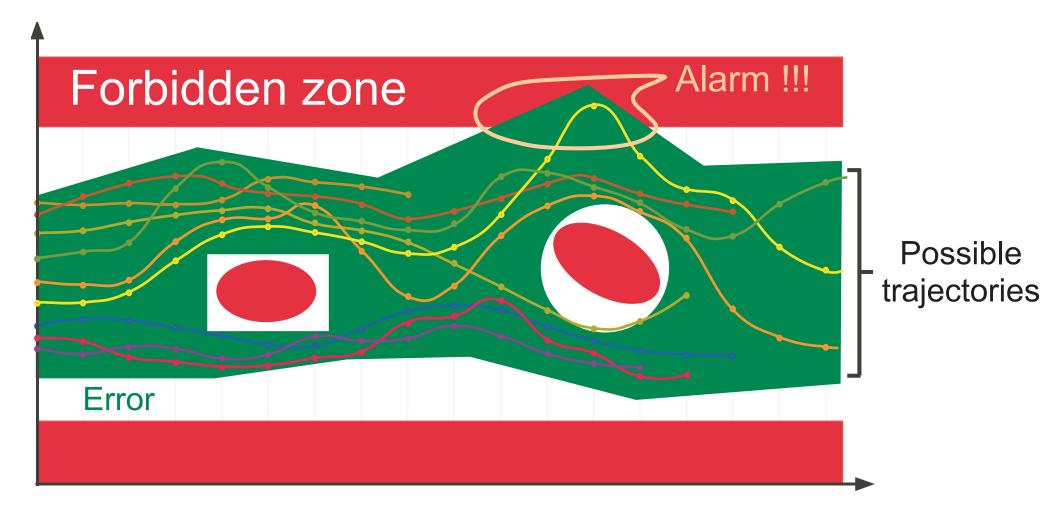
When abstract proofs may fail while concrete proofs would succeed



By soundness an alarm must be raised for this over-approximation!

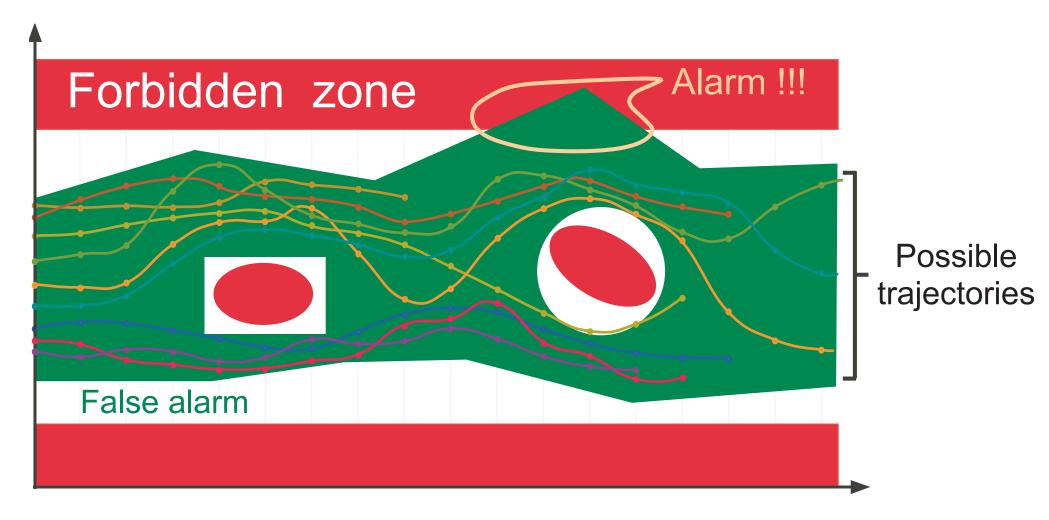
True alarm

The abstract alarm may correspond to a concrete error



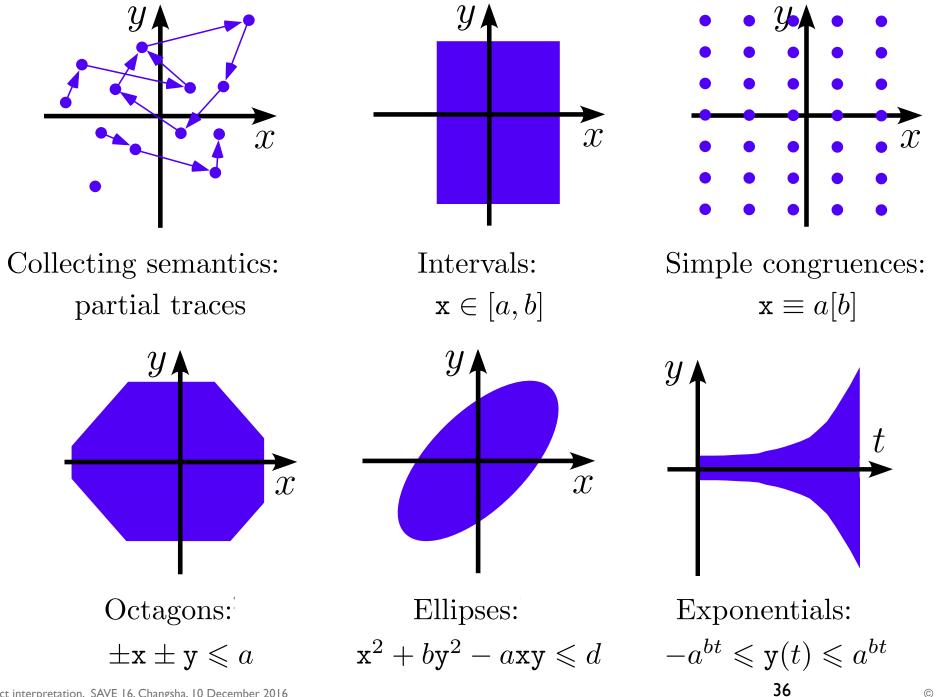
False alarm

The abstract alarm may correspond to no concrete error (false negative)



What to do in presence of false alarms

- False alarms are ultimately unavoidable (<u>Gödel's</u> incompleteness)
- Consider finite cases or decidable cases only (modelchecking, does not scale)
- Ask for human help by providing information on the program behavior (theorem provers, SMT solvers), program specific and labor costly
- Have specialists refine the abstract interpretation (e.g. Astrée, <u>http://www.absint.com/astree/index.htm</u>), shared cost

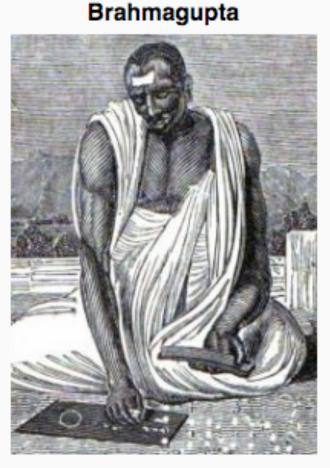


Abstract interpretation, SAVE 16, Changsha, 10 December 2016

The very first static analysis

Brahmagupta

Brahmagupta (Sanskrit: ब्रह्मगुप्त; (598–c.670 CE) was an Indian mathematician and astronomer who wrote two important works on Mathematics and Astronomy: the Brāhmasphuṭasiddhānta (Extensive Treatise of Brahma) (628), a theoretical treatise, and the Khaṇḍakhādyaka, a more practical text.



Born	598 CE
Died	c.670 CE
Fields	Mathematics, Astronomy
Known for	Zero, modern Number system

18.30. [The sum] of two positives is positives, of two negatives negative;

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• The abstraction is that you do not (always) need to known the absolute value of the arguments to know the sign of the result;

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- Useful in practice (if you know what to do when you don't know the sign)

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- Sometimes imprecise (don't know the sign of the sum of a positive and a negative)
- Useful in practice (if you know what to do when you don't know the sign)
- e.g. in compilation: do not optimize (a division by 2 into a shift when positive^(*))

(*) Unless processor uses 2's complement and can shift the sign.

18.30. [The sum] of two positives is positives, of two negatives negative;[...]

18.32. A negative minus zero is negative, a positive [minus zero] positive; zero [minus zero] is zero. When a positive is to be subtracted from a negative or a negative from a positive, then it is to be added.

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18.33. The product of a negative and a positive is negative, of two negatives positive, and of positives positive; the product of zero and a negative, of zero and a positive, or of two zeros is zero.

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negative, of zero and a positive, or of two zeros is zero.

18.34. A positive divided by a positive or a negative divided by a negative is positive; a zero divided by a zero is zero; a positive divided by a negative is negative; a negative divided by a positive is [also] negative.

The rule of signs by Michel Sintzoff (1972)

For example, a×a+b×b yields the value 25 when a is 3 and b is -4, and when + and × are the arithmetic multiplication and addition. But axa+bxb yields always the object "pos" when a and b are the objects "pos" or "neg", and when the valuation is defined as follows : pos×pos=pos pos+pos=pos pos+neg=pos,neg pos×neg=neg neg+pos=pos,neg neg×pos=neg neg×neg=pos neg+neg=neg $V(p \times q) = V(p) \times V(q)$ V(p+q)=V(p)+V(q)V(0) = V(1) = ... = posV(-1) = V(-2) = ... = negThe valuation of a×a+b×b yields "pos" by the following computations : V(a)=pos,neg V(b)=pos,neg V(a×a)=pos×pos,neg×neg V(b×b)=pos×pos,neg×neg **≠**pos.pos=pos =pos,pos=pos $V(a \times a + b \times b) = V(a \times a) + V(b \times b) = pos + pos = pos$ This valuation proves that the result of a×a+b×b is always positive and hence allows to compute its square root without any preliminary dynamic test on its sign. On the other hand, the

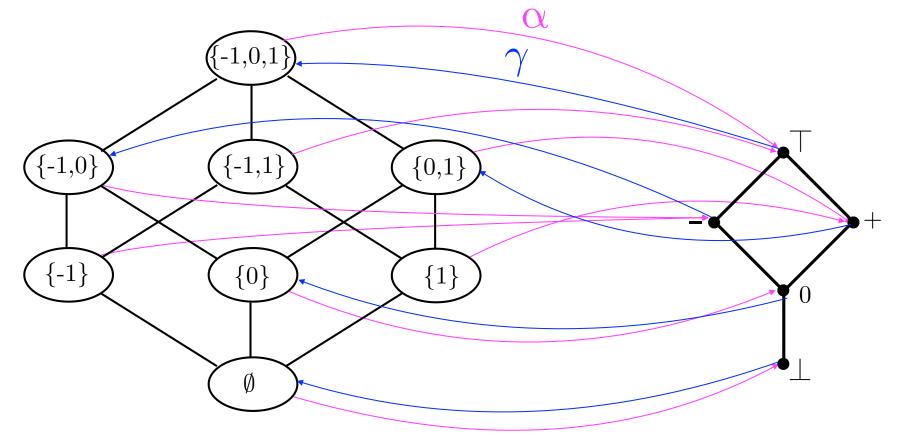
The rule of signs by Michel Sintzoff (1972)

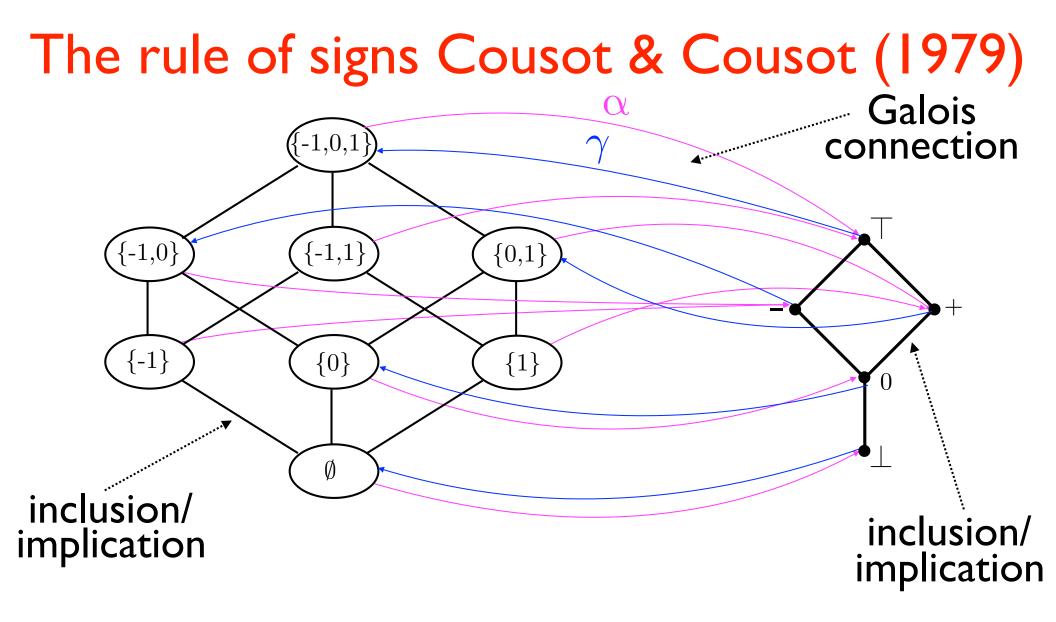
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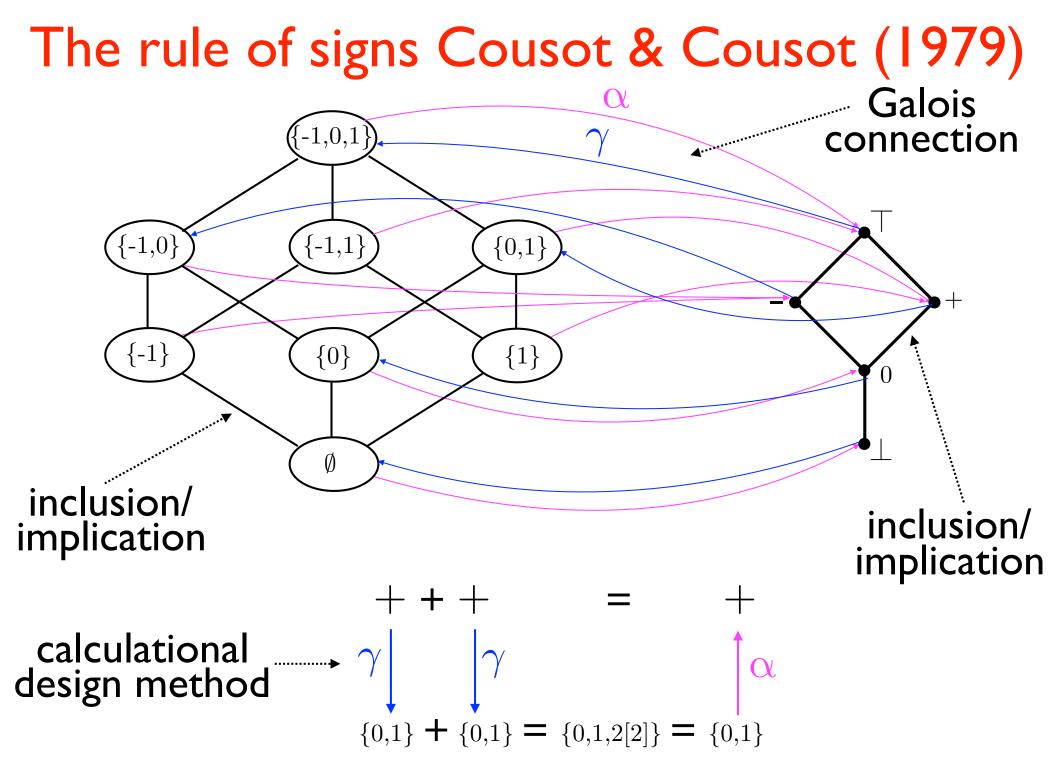
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But axa+bxb yields always the object "pos" when
a and b are the objects "pos" or "neg", and when
the valuation is defined as follows :
                             pos×pos=pos
pos+pos=pos
                                                      wrong
pos+neg=pos,neg
                             pos×neg=neg
neg+pos=pos,neg
                             neg×pos=neg
                                                       0 \in pos x - l \in neg
                             neg×neg=pos
neg+neg=neg
V(p+q)=V(p)+V(q)
                             V(p \times q) = V(p) \times V(q)
                                                    = 0∉neg
V(0) = V(1) = ... = pos
V(-1) = V(-2) = ... = neg
The valuation of a×a+b×b yields "pos" by the
following computations :
V(a)=pos,neg
                           V(b)=pos,neg
V(a×a)=pos×pos,neg×neg V(b×b)=pos×pos,neg×neg
      zpos,poszpos
                                  =pos,pos=pos
V(a \times a + b \times b) = V(a \times a) + V(b \times b) = pos + pos = pos
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a×a+b×b is always positive and hence allows to
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The rule of signs Cousot & Cousot (1979)







Application of abstract interpretation to static analysis

All computer scientists have experienced bugs









Ariane 5.01 failure (overflow) (float rounding) (unit error)

Patriot failure

Mars orbiter loss

Heartbleed (buffer overrun)

- Checking the presence of bugs by debugging is great
- Proving their absence by static analysis is even better!

Static analysis

- Check program properties (automatically, using the program text only, without running the program)
- Difficulties:
 - Undecidability / complexity:
 - Precision
 - Scalability
 - Soundness (correctness)
 - Induction: widening/narrowing

Fixpoint

 $\{y \geqslant 0\} \leftarrow ext{hypothesis}$ $\mathbf{X} = \mathbf{V}$ $\{I(x,y)\} \leftarrow \text{loop invariant}$ while (x > 0) { x = x - 1;}

Floyd-Naur-Hoare verification conditions:

 $(y \geqslant 0 \wedge x = y) \Longrightarrow I(x,y)$ $(I(x,y)\wedge x>0\wedge x'=x-1)\Longrightarrow I(x',y)$

Equivalent fixpoint equation:

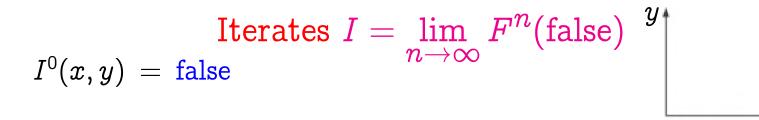
 $I(x,y) = x \geqslant 0 \land (x = y \lor I(x+1,y))$

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(5)We look for the most precise invariant I, implying all others, that is $Ifp^{\Longrightarrow} F$.

Fixpoint equation

(i.e.
$$I = F(I)^{(5)}$$
)

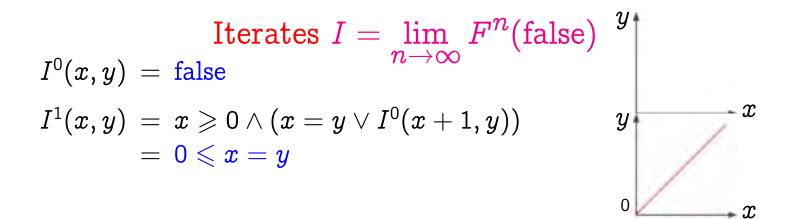


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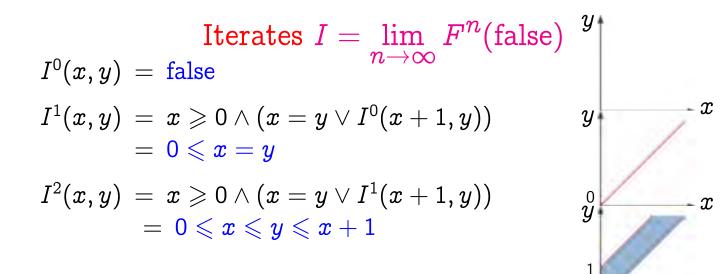
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 \mathcal{I}



CSE, SNU, Seoul, 09/30/2008

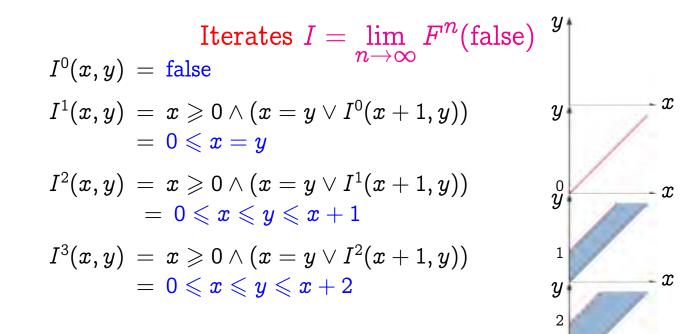
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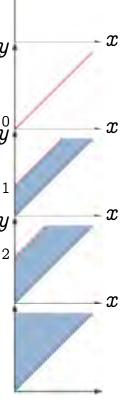
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x

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Convergence acceleration: widening

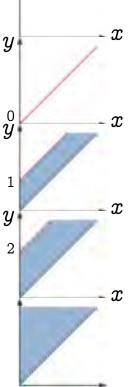
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Fixed point

$$\begin{array}{l} \text{Accelerated Iterates }I=\lim_{n\to\infty}F^n(\text{false}) \begin{array}{l} y\\ I^0(x,y)=\text{false} \end{array} \\ I^1(x,y)=x\geqslant 0\wedge (x=y\vee I^0(x+1,y)) \qquad y\\ = 0\leqslant x=y \end{array} \\ I^2(x,y)=x\geqslant 0\wedge (x=y\vee I^1(x+1,y)) \qquad y\\ = 0\leqslant x\leqslant y\leqslant x+1 \end{array} \\ I^3(x,y)=x\geqslant 0\wedge (x=y\vee I^2(x+1,y)) \qquad 1\\ = 0\leqslant x\leqslant y\leqslant x+2 \qquad y\\ I^4(x,y)=I^2(x,y) \bigtriangledown I^3(x,y)\leftarrow \text{widening} \qquad 2\\ = 0\leqslant x\leqslant y \end{aligned} \\ I^5(x,y)=x\geqslant 0\wedge (x=y\vee I^4(x+1,y)) \\ = I^4(x,y) \quad \text{fixed point!} \end{aligned}$$

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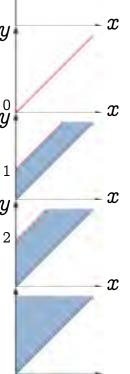


Octagons

$$\begin{array}{l} \text{Accelerated Iterates }I=\lim_{n\to\infty}F^n(\text{false}) \begin{array}{l} y\\ I^0(x,y)=\text{false} \end{array} \\ I^1(x,y)=x\geqslant 0\wedge (x=y\vee I^0(x+1,y)) \qquad y\\ = 0\leqslant x=y \end{array} \\ I^2(x,y)=x\geqslant 0\wedge (x=y\vee I^1(x+1,y)) \qquad g\\ = 0\leqslant x\leqslant y\leqslant x+1 \end{array} \\ I^3(x,y)=x\geqslant 0\wedge (x=y\vee I^2(x+1,y)) \qquad 1\\ = 0\leqslant x\leqslant y\leqslant x+2 \qquad y\\ I^4(x,y)=I^2(x,y) \bigtriangledown I^3(x,y)\leftarrow \text{widening} \qquad 2\\ = 0\leqslant x\leqslant y \end{array} \\ I^5(x,y)=x\geqslant 0\wedge (x=y\vee I^4(x+1,y)) \\ = I^4(x,y) \quad \text{fixed point!} \end{array}$$

The invariants are computer representable with octagons!

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Industrialisation: Development in cooperation with Airbus France

 Automatic proofs of absence of runtime errors in Electric Flight Control Software:



- A340/600: 132.000 lines of C, 40mn on a PC 2.8 GHz, 300 Mb (Nov. 2003)
- A380: 1.000.000 lines of C, 34h, 8 Gb (Nov. 2005) no false alarm, World premières !
- Automatic proofs of absence of runtime errors in the ATV software⁽²⁾:

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C version of the automatic docking software: 102.000 lines of C, 23s on a Quad-Core AMD Opteron[™] processor, 16 Gb (Apr. 2008)

(iii)

⁽²⁾ the Jules Vernes Automated Transfer Vehicle (ATV) enabling ESA to transport payloads to the International Space Station.

Application of abstract interpretation to program proof methods

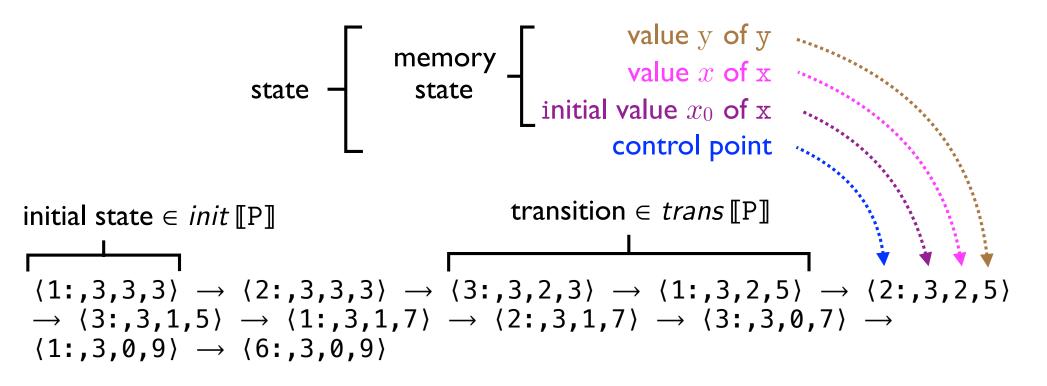
Maximal execution trace

#include ·	<stdio.h></stdio.h>	Enter an integer: 3	Enter an integer: –1
int main() {	x = 3, y = 3	x = -1, y = -1
	<pre>int x,y;</pre>	x = 2, y = 5	x = -2, y = 1
	<pre>printf("Enter an integer: ");</pre>	x = 1, y = 7	x = -3, y = 3
	scanf("%d",&x);	x = 0, y = 9	x = -4, $y = 5$
/* 1: */	while (x != 0) {		
	printf("x = %d, y = %d\n",x,y);		x = -738245, y = 1476487
/* 2: */	x = x - 1;		
/* 3: */	y = y + 2;		
	}		
/* 4: */	printf("x = %d, y = %d\n",x,y);		

 $\begin{array}{l} \langle 1:,3,3,3\rangle \rightarrow \langle 2:,3,3,3\rangle \rightarrow \langle 3:,3,2,3\rangle \rightarrow \langle 1:,3,2,5\rangle \rightarrow \langle 2:,3,2,5\rangle \\ \rightarrow \langle 3:,3,1,5\rangle \rightarrow \langle 1:,3,1,7\rangle \rightarrow \langle 2:,3,1,7\rangle \rightarrow \langle 3:,3,0,7\rangle \rightarrow \\ \langle 1:,3,0,9\rangle \rightarrow \langle 6:,3,0,9\rangle \end{array}$

Maximal execution trace

<pre>#include int main(</pre>		Enter an integer: 3 x = 3, y = 3	Enter an integer: $-1 \times = -1$, $y = -1$
	<pre>int x,y; printf("Enter on integers ");</pre>	x = 2, y = 5	x = -2, y = 1
	•		x = -3, y = 3
/* 1• */	<pre>scanf("%d",&x); y = x; while (x != 0) {</pre>	x = 0, y = 9	x = -4, y = 5
/☆ ⊥• ☆/	<pre>printf("x = %d, y = %d\n",x,y);</pre>		x = -738245, y = 1476487
/* 2: */	x = x - 1;		
/* 3: */	y = y + 2;		
	}		
/* 4: */	printf("x = %d, y = %d\n",x,y);		



Maximal trace semantics

- The trace semantics of a program is the set of all possible maximal finite or infinite execution traces for that program
- The trace semantics of a programing language maps programs to their trace semantics

Inductive definition

• Partial traces:

- A trace with one initial state is a partial trace
- A partial trace extended by a transition is a partial trace

• Maximal traces:

- Finite traces with no extension by a transition
- Infinite traces which prefixes are all partial traces

Fixpoint partial trace semantics

- initial states of program P: *init* [P]
- transitions of programs P: $trans \llbracket P \rrbracket$
- $\operatorname{Ft}[\![\mathbf{P}]\!]X = \{ s \mid s \in init[\![\mathbf{P}]\!] \} \cup \{ \sigma ss' \mid \sigma s \in X \land ss' \in trans[\![\mathbf{P}]\!] \} \}$
- $S^t[\![P]\!] = \mathsf{lfp}^{\subseteq} F^t[\![P]\!]$

Invariance abstraction

- Collect at each control point the possible values of variables when execution reaches that control point
- $\alpha(X)c = \{m \mid \exists \sigma, \sigma'. \sigma \langle c, m \rangle \sigma' \in X\}$
- Invariance semantics: $S^{i}\llbracket P \rrbracket = \alpha(S^{t}\llbracket P \rrbracket)$

Invariance abstraction

- Collect at each control point the possible values of variables when execution reaches that control point
- $S^{i}\llbracket P \rrbracket = \alpha(S^{t}\llbracket P \rrbracket)c = \{m \mid \exists \sigma, \sigma'. \ \sigma \langle c, m \rangle \sigma' \in S^{t}\llbracket P \rrbracket\}$

Calculations design of the verification conditions

- $\alpha(\operatorname{Ft}[\![\mathbf{P}]\!]X)$ = $\lambda c.\{m \mid \exists \sigma, \sigma'. \sigma \langle c, m \rangle \sigma' \in X\}$ = ...
 - $= \mathrm{F^i}[\![\mathbf{P}]\!](\alpha(X))$
 - where $\mathrm{F}^i[\![\mathrm{P}]\!]$ are the Turing/Floyd/Naur/Hoare verification conditions
- It follows that $S^i \llbracket P \rrbracket = \mathsf{lfp}^{\dot{c}} F^i \llbracket P \rrbracket$
- The proof method is then by fixpoint induction (Tarski 1955)

Application to the semantics of programming languages



• All known semantics are abstractions of a most precise semantics

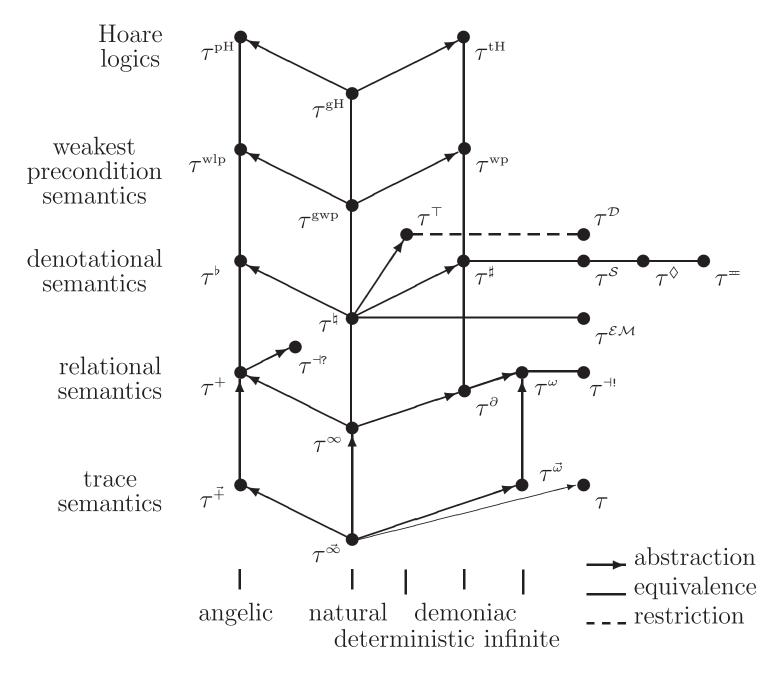
Abstraction to denotational semantics

- The maximal trace semantics ${\rm S^m}[\![P]\!]$ (maximal finite and infinite execution traces
- Denotational semantics abstraction:
 - $\bullet \ \operatorname{Sd}[\![\mathbf{P}]\!] = \alpha(\operatorname{Sm}[\![\mathbf{P}]\!])$

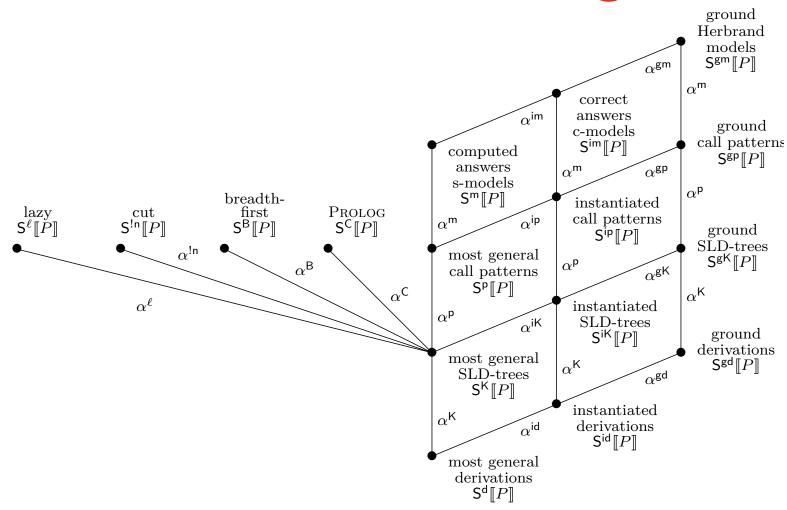
•
$$\alpha(X) = \lambda s.\{s' \mid \exists \sigma. s\sigma s' \in X\} \cup \{\bot \mid \exists \sigma. s\sigma ... \in X\}$$

i.e. a map of initial states to the set of final states plus \perp in case of non-termination

Hierarchy of abstractions



idem for Prolog



all semantics are abstractions of S^d [[P]]

Conclusion

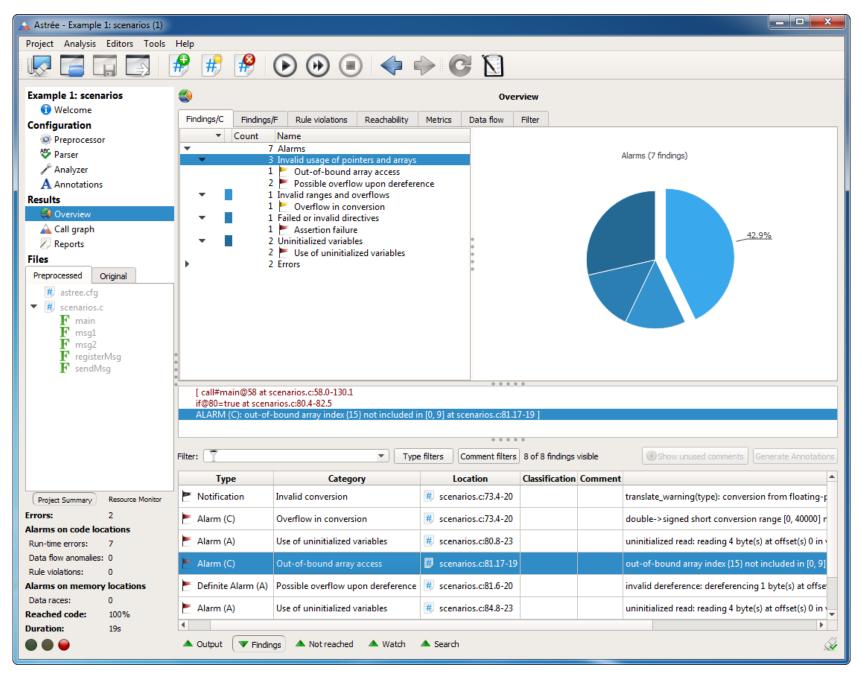
Abstract interpretation

- A well-developed theory, still in progress
- Active research e.g.
 - abstract domains to handle e.g. complex data structures
 - abstraction of parallelism with weak memory models
 - applications to biology, ...
- Industrial-quality static analyzers

Industrialisation: Astrée

Astrée - Example 1: scenarios (1)										
Project Analysis Editors Edit Tools Help										
Example 1: scenarios	#	Analyzed f	ile: db/invalid/path/scenarios.c		C	Origina	source: src/	scenarios.c	2	
1 Welcome	70	/*				/*		63		
Configuration	71 72	* Type cast ca */	using overflow.		67 68	* Type cast */	causing ov	ertlow.		
Preprocessor Parser	73 II 74					69 s = SPEED_SENSOR; 70				
Analyzer	75	/*		71 /*						
Annotations	76					72 * Precise handling of pointer arithmetics. 73 */				
Results	78	<pre>78</pre>				74 ptr = &ArrayBlock[0]; 75				
Overview	80	<pre>80 if (uninitialized_1) {</pre>				<pre>if (uninitialized_1) {</pre>				
A Call graph	81 82	<pre>81 ArrayBlock[15] = 0x15; // easy case 82 }</pre>				77 ArrayBlock[15] = 0x15; // easy case				
Reports	83	83 79								
Files	85					*(ptr + 15)		// hard case		
Preprocessed Original	86 87	}			82 83	}			_	
# astree.cfg	88	/*		-	84	/*				
▼ ₩ scenarios.c	89 90		lling of compute-through-overt by default, alarms on explicit		85 86			compute-through-over t, alarms on explici		
F main	91 92	* deactivated */	(see Options->General tab).		87 88	* deactivate */	ed (see Opt	ions->General tab).		
F msg1 F msg2	93	z = (short)((ur	signed short)vx + (unsigned s	short)vy	89	z = (short)((hort)vx + (unsigned	short)vy	
registerMsg	94 95	ASTREE_asser	t((-2<=z && z<=2));		90 91	ASTREE_asse	ert((-2<=z	&& z<=2));		
F sendMsg	<u>्</u>	/*				/*			▼ 	
	0	Line 81, column 7 Line 77, column 1								
	[call#main@58 at scenarios.c:58.0-130.1 if@80=true at scenarios.c:80.4-82.5									
	ALARM (A): invalid dereference: dereferencing 1 byte(s) at offset(s) 15 may overflow the variable ArrayBlock of byte-size 10 at scenarios.c:81.6-20]									
	ERROR: Definite runtime error during assignment in this context. Analysis stopped for this context.									
	0000									
	Filter: Type filters Comment filters 8 of 8 findings visible Show unused comments Generate Annotations									
Project Summary Resource Monitor	Order	Туре	Category	Lo	cation	Classification	Comment		A	
Errors: 2 Alarms on code locations	4	 Alarm (C) 	Out-of-bound array access	# scenar	ios.c:81.17-19		c	out-of-bound array index {	15} not incl	
Run-time errors: 7	5 🕨	• Definite Alarm (A)	Possible overflow upon dereference	🗰 scenar	ios.c:81.6-20		i	nvalid dereference: derefer	rencing 1 b	
Data flow anomalies: 0 Rule violations: 0	6 🕨	F Alarm (A)	Use of uninitialized variables	# scenarios.c:84.8-23			L	uninitialized read: reading 4	byte(s) at	
Alarms on memory locations	7	Definite Alarm (A)	Possible overflow upon dereference	# scenar	ios.c:85.6-17		i	nvalid dereference: derefer	rencing 1 b	
Data races: 0 Reached code: 100%	8	F Alarm (A)	Assertion failure	# scenar	ios.c:127.4-40		ā	assert failureASTREE_ass		
Duration: 20s	4									
	🔺 Outpu	t 🔍 🔻 Findings 🔺	Not reached 🔺 Watch 🔺 Search	1					<u>م</u>	

Industrialisation: Astrée



Many other static analyzers

- Julia (Java) http://www.juliasoft.com
- Ikos, NASA https://ti.arc.nasa.gov/opensource/ikos/
- Clousot for code contract, Microsoft, https:// github.com/Microsoft/CodeContracts
- Infer (Facebook) http://fbinfer.com
- Zoncolan (Facebook)
- Google

Static analysis for software development

• Users of Astrée:



• Why not all software developers use static analysis tools?

Irresponsibility

 Computer engineering is the only technology where developers are not responsible for their errors, even the trivial ones:

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The future

- Safety and security does matter to the general public
- Computer scientists will ultimately be held responsible for there errors
- At least the automatically discoverable ones
- Since this is now part of the state of the art
- Automatic static analysis, verification, etc has a brilliant future.

Francesco Logozzo, designer of the <u>Zoncolan</u> static analyzer at Facebook wrote me on 09/12/2016:

``Finding people who really know static analysis is very hard, you should tell your students that if they want a great job in a Silicon Valley company they should study abstract interpretation not JavaScript. Feel free to quote me on that ;-)"

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The End, Thank You