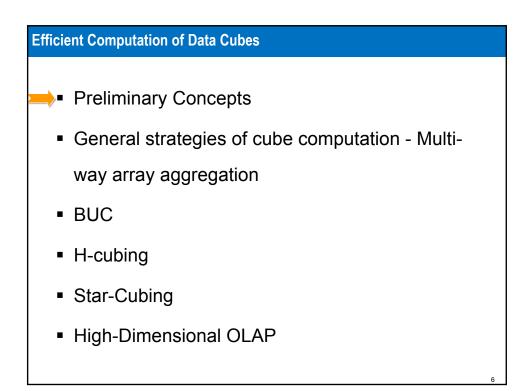


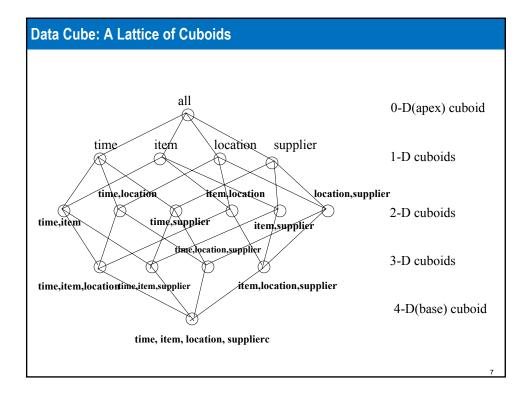
# Data Cube Technology in Brief

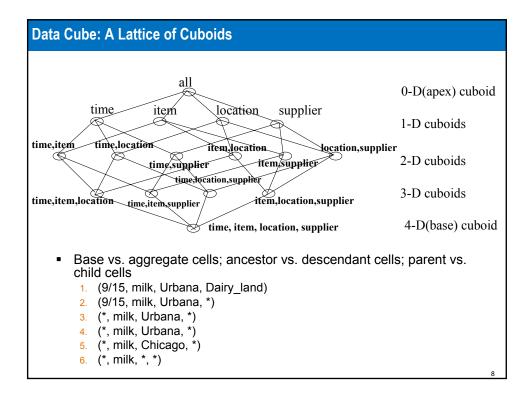
- Efficient Methods for Data Cube Computation
- Data Cubes for Advanced Applications
- Knowledge Discovery with Data Cubes
- Summary

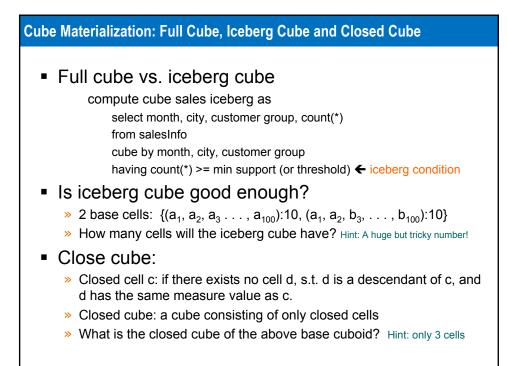


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	1	Session Overview	and the second se	
	2	Data Cube Technology	ALCONTRACT, AND ALCONT	
	3	Summary and Conclusion	and the second se	
				5



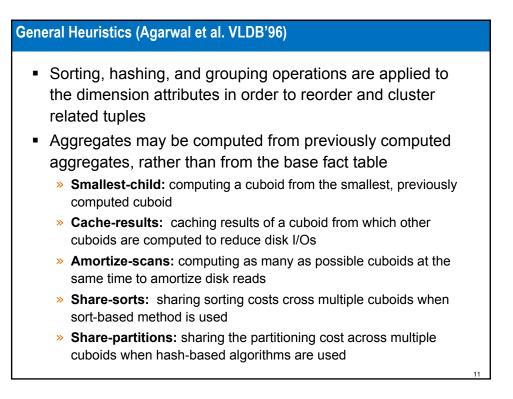






#### **Roadmap for Efficient Computation**

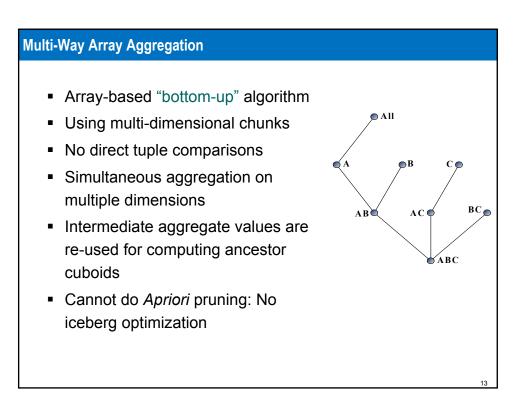
- General cube computation heuristics (Agarwal et al.'96)
- Computing full/iceberg cubes: 3 methodologies
  - » Bottom-Up: Multi-Way array aggregation (Zhao, Deshpande & Naughton, SIGMOD'97)
  - » Top-down:
    - BUC (Beyer & Ramarkrishnan, SIGMOD'99)
    - H-cubing technique (Han, Pei, Dong & Wang: SIGMOD'01)
  - » Integrating Top-Down and Bottom-Up:
    - Star-cubing algorithm (Xin, Han, Li & Wah: VLDB'03)
- High-dimensional OLAP: A Minimal Cubing Approach (Li, et al. VLDB'04)
- Computing alternative kinds of cubes:
  - » Partial cube, closed cube, approximate cube, etc.

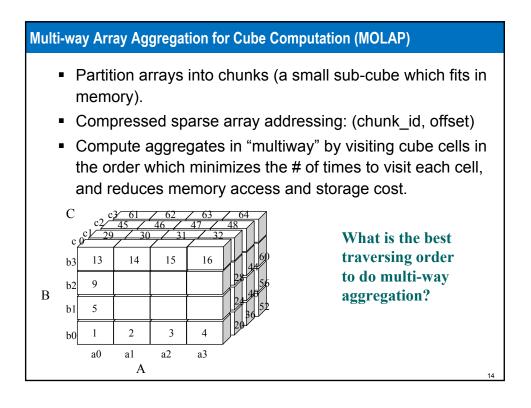


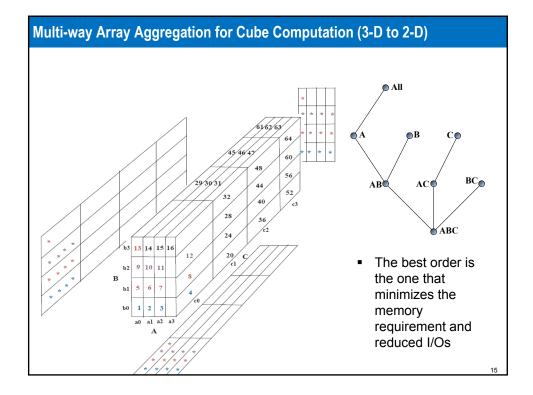
- Preliminary Concepts
- General strategies of cube computation Multi-

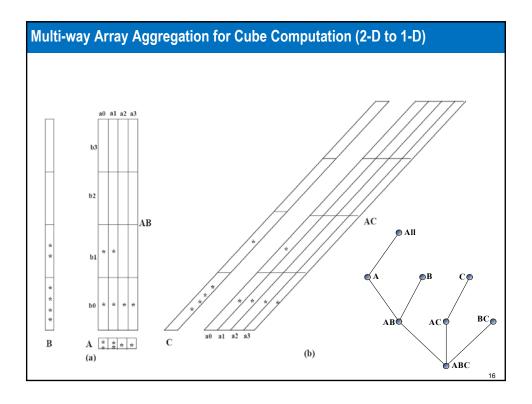
way array aggregation

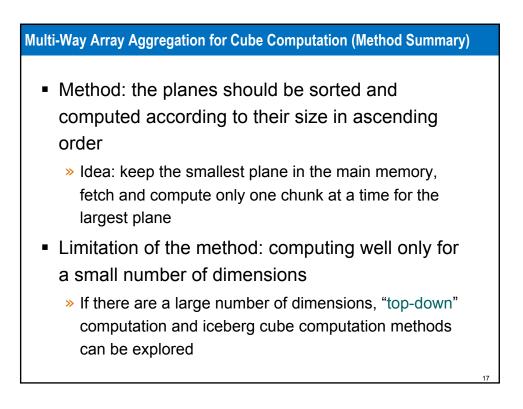
- BUC
- H-cubing
- Star-Cubing
- High-Dimensional OLAP









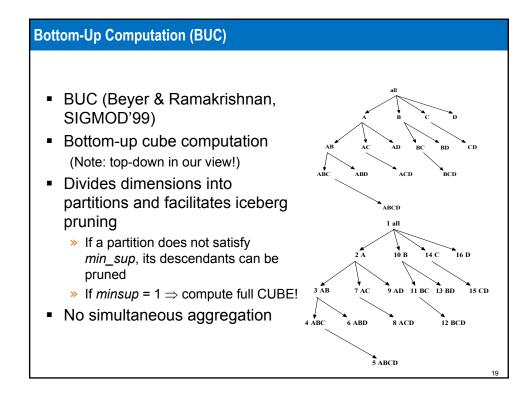


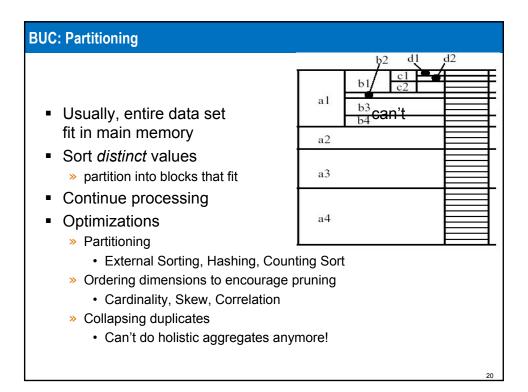
- Preliminary Concepts
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way array aggregation

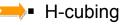
븢 BUC

- H-cubing
- Star-Cubing
- High-Dimensional OLAP

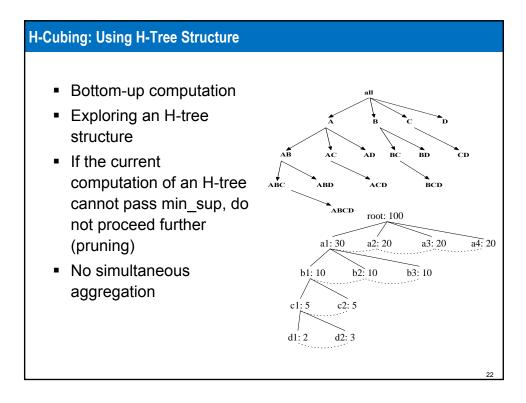


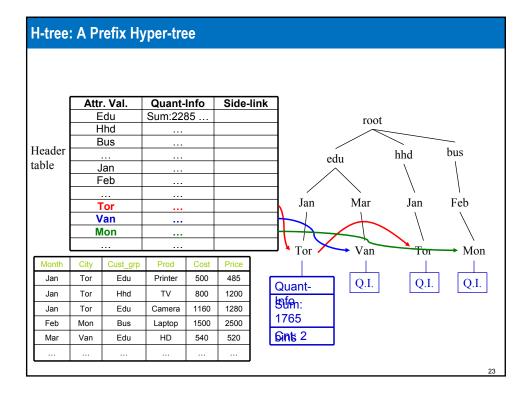


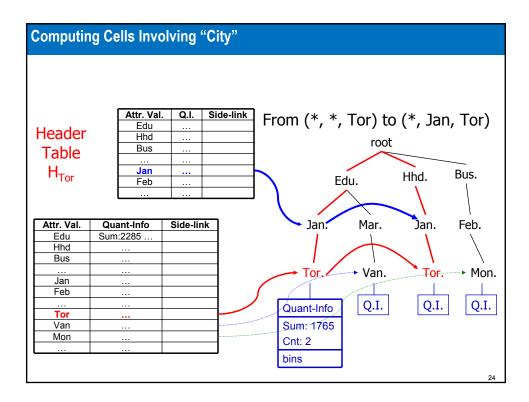
- Preliminary Concepts
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- BUC



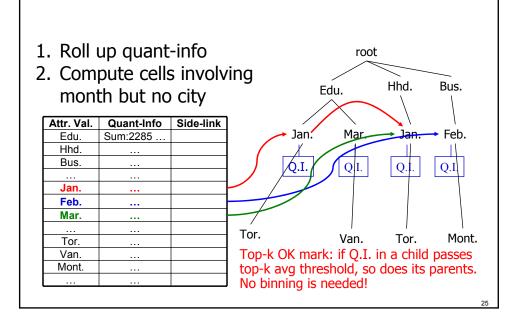
- Star-Cubing
- High-Dimensional OLAP

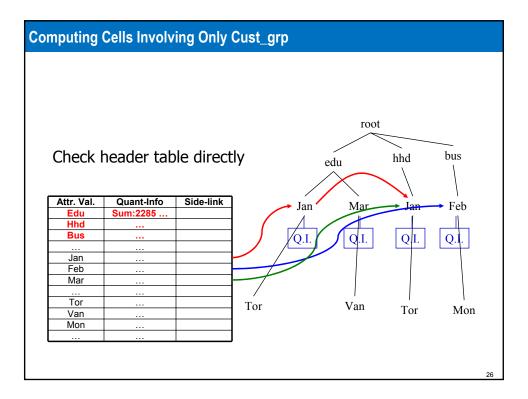




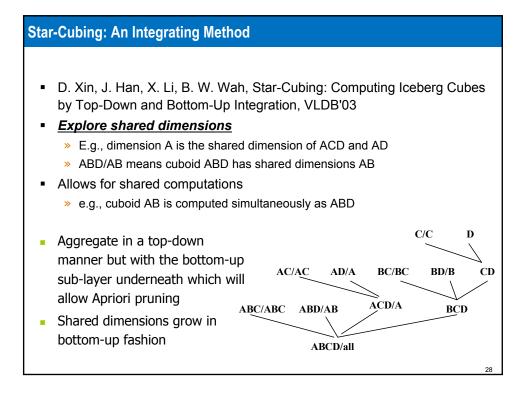


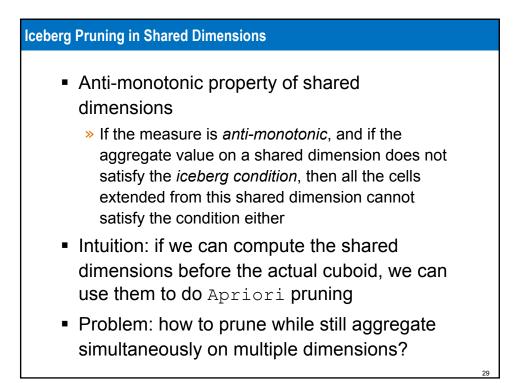






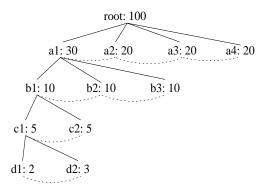
- Preliminary Concepts
- General strategies of cube computation Multiway array aggregation
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- Star-Cubing
  - High-Dimensional OLAP





# **Cell Trees**

- Use a tree structure similar to H-tree to represent cuboids
- Collapses common prefixes to save memory
- Keep count at node
- Traverse the tree to retrieve a particular tuple



#### **Star Attributes and Star Nodes**

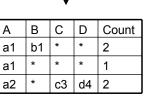
- Intuition: If a singledimensional aggregate on an attribute value *p* does not satisfy the iceberg condition, it is useless to distinguish them during the iceberg computation
   » E.g., b<sub>2</sub>, b<sub>3</sub>, b<sub>4</sub>, c<sub>1</sub>, c<sub>2</sub>, c<sub>4</sub>, d<sub>1</sub>, d<sub>2</sub>, d<sub>3</sub>
- Solution: Replace such attributes by a \*. Such attributes are <u>star attributes</u>, and the corresponding nodes in the cell tree are <u>star nodes</u>

А	В	С	D	Count
a1	b1	c1	d1	1
a1	b1	c4	d3	1
a1	b2	c2	d2	1
a2	b3	c3	d4	1
a2	b4	c3	d4	1

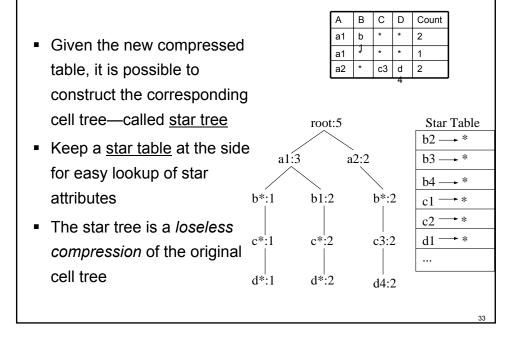
#### **Example: Star Reduction**

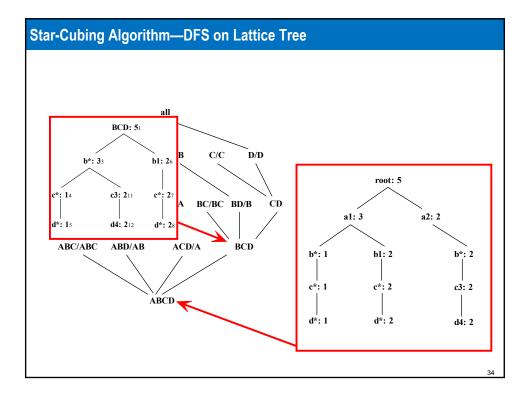
- Suppose minsup = 2
- Perform one-dimensional aggregation. Replace attribute values whose count < 2 with \*. And collapse all \*'s together
- Resulting table has all such attributes replaced with the star-attribute
- With regards to the iceberg computation, this new table is a *loseless compression* of the original table

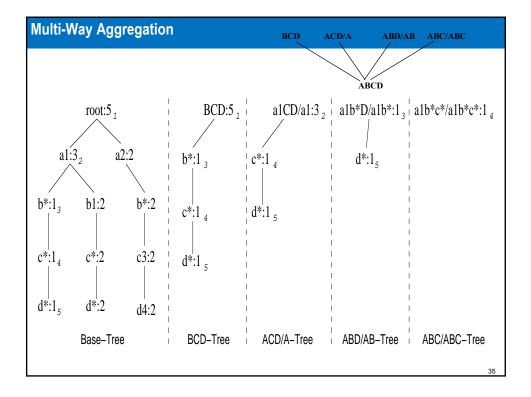
А	В	С	D	Count
a1	b1	*	*	1
a1	b1	*	*	1
a1	*	*	*	1
a2	*	c3	d4	1
a2	*	c3	d4	1

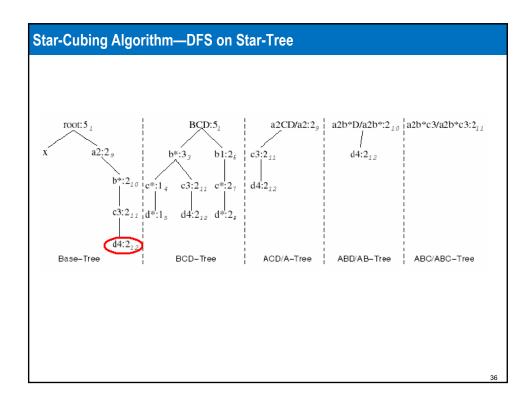


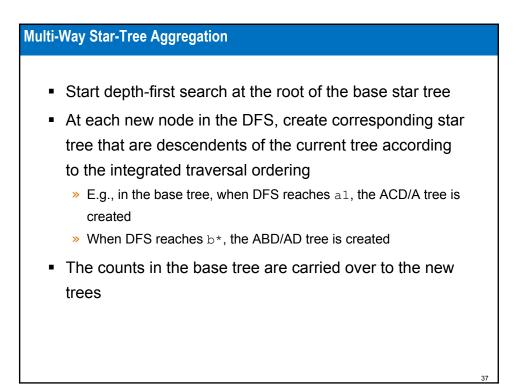
#### **Star Tree**

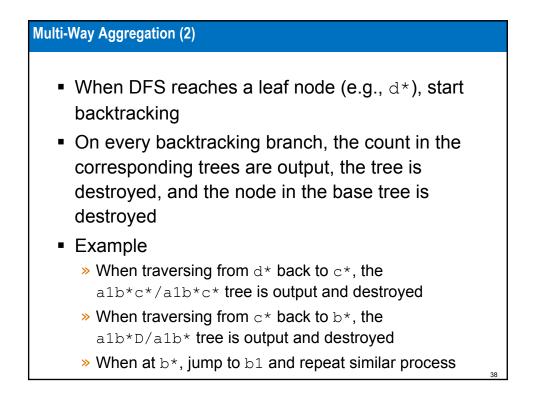




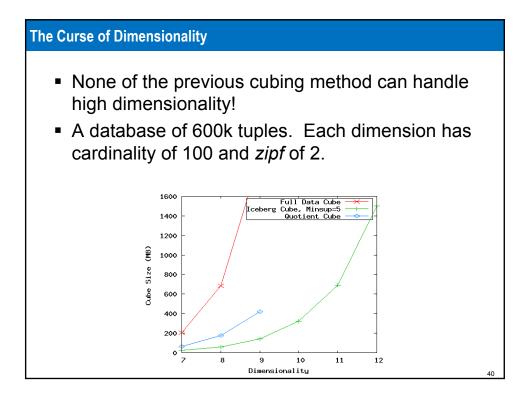


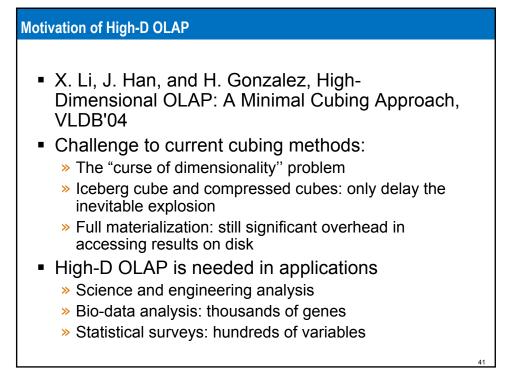




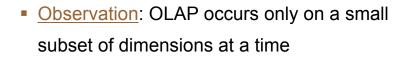


- Preliminary Concepts
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- Star-Cubing
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### Fast High-D OLAP with Minimal Cubing



- Semi-Online Computational Model
  - 1. Partition the set of dimensions into shell fragments
  - 2. Compute data cubes for each shell fragment while retaining **inverted indices** or **value-list indices**
  - 3. Given the pre-computed **fragment cubes**, dynamically compute cube cells of the highdimensional data cube *online*

### **Properties of Proposed Method**

- Partitions the data vertically
- Reduces high-dimensional cube into a set of lower dimensional cubes
- Online re-construction of original highdimensional space
- Lossless reduction
- Offers tradeoffs between the amount of preprocessing and the speed of online computation

### **Example Computation**

Let the cube aggregation function be count

tid	A	в	С	D	Е
1	a1	b1	c1	d1	e1
2	a1	b2	c1	d2	e1
3	a1	b2	c1	d1	e2
4	a2	b1	c1	d1	e2
5	a2	b1	c1	d1	e3

Divide the 5 dimensions into 2 shell fragments:

» (A, B, C) and (D, E)

### **1-D Inverted Indices**

# Build traditional invert index or RID list

Attribute Value	TID List	List Size
al	123	3
a2	4 5	2
b1	145	3
b2	2 3	2
c1	12345	5
d1	1345	4
d2	2	1
e1	12	2
e2	34	2
e3	5	1

#### Shell Fragment Cubes: Ideas

- Generalize the 1-D inverted indices to multi-dimensional ones in the data cube sense
- Compute all cuboids for data cubes ABC and DE while retaining the inverted indices
- For example, shell fragment cube ABC contains 7 cuboids:
  - » A, B, C
  - » AB, AC, BC
  - » ABC

Cell	Intersection	TID List	List Size
al bl	123 ∩145	1	1
al b2	1 2 3 ∩2 3	2 3	2
a2 b1	45∩145	4 5	2
a2 b2	4 5 ∩ 2 3	$\otimes$	0

 This completes the offline computation stage

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 Given a database of T tuples, D dimensions, and F shell fragment size, the fragment cubes' space requirement is:

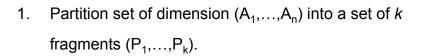
» For F < 5, the growth is sub-linear

$$O\left(T\left[\frac{D}{F}\right](2^F-1)\right)$$

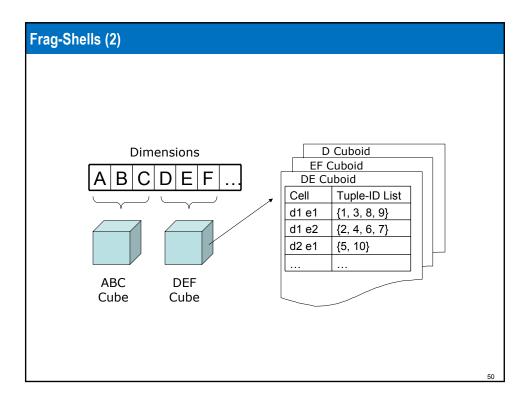
- Shell fragments do not have to be disjoint
- Fragment groupings can be arbitrary to allow for maximum online performance
  - » Known common combinations (e.g.,<city, state>) should be grouped together.
- Shell fragment sizes can be adjusted for optimal balance between offline and online computation

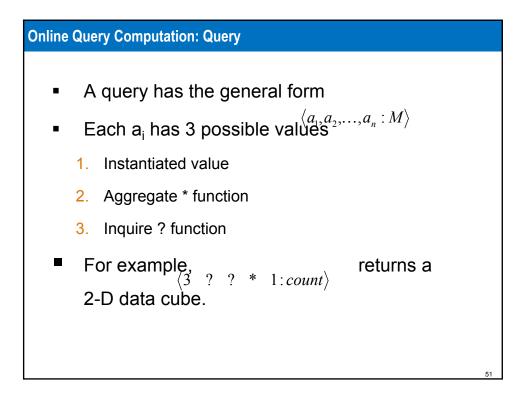
ID_Measure Table					
	easure tal	than coun ble separat	•	-	
	tid	count	sum		
	1	5	70		
	2	3	10		
	3	8	20		
	4	5	40		
	5	2	30		
				48	

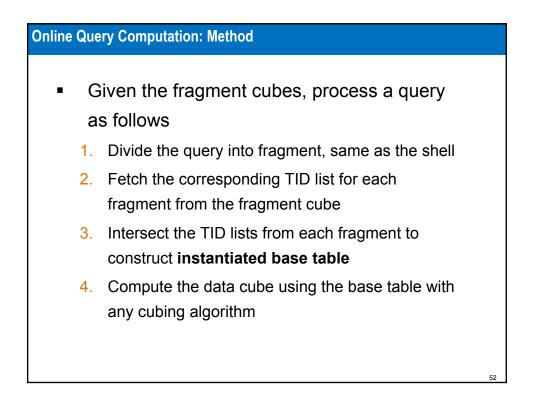
# The Frag-Shells Algorithm

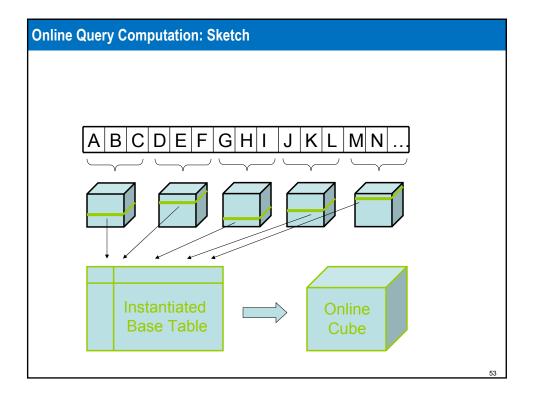


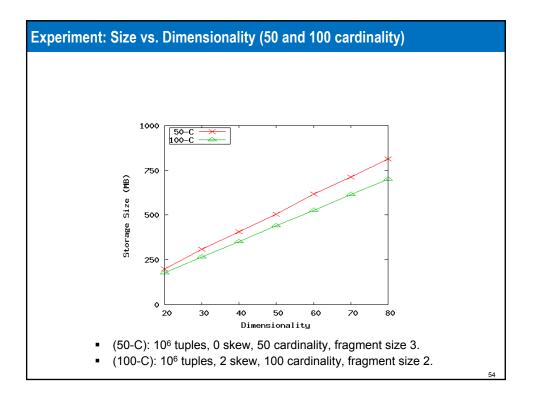
- 2. Scan base table once and do the following
- 3. insert <tid, measure> into ID\_measure table.
- 4. for each attribute value a<sub>i</sub> of each dimension A<sub>i</sub>
- 5. build inverted index entry <a<sub>i</sub>, tidlist>
- 6. For each fragment partition P<sub>i</sub>
- build local fragment cube S<sub>i</sub> by intersecting tid-lists in bottom- up fashion.

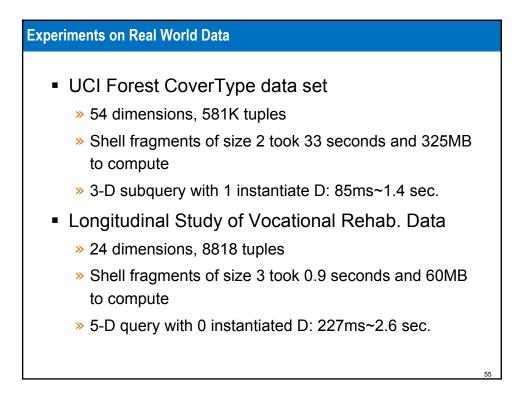


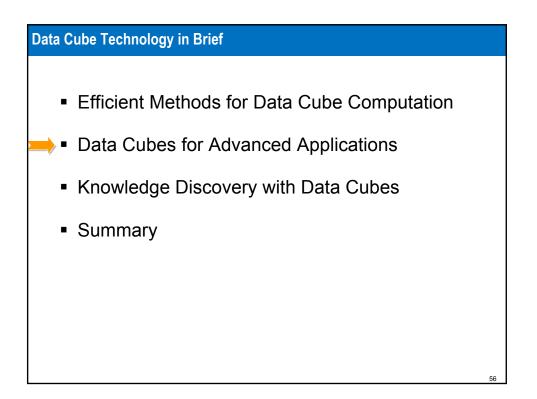






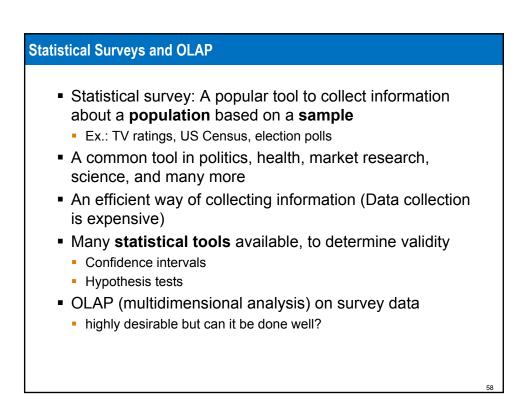




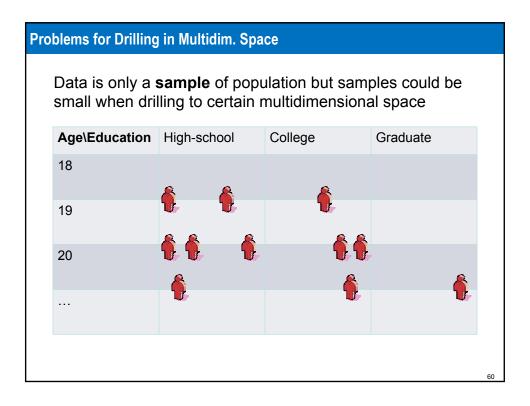


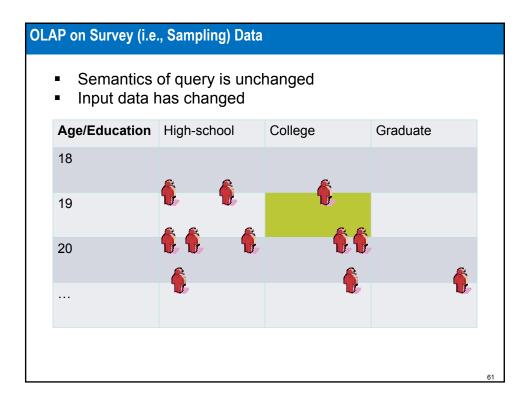
#### Data Cubes for Advanced Applications

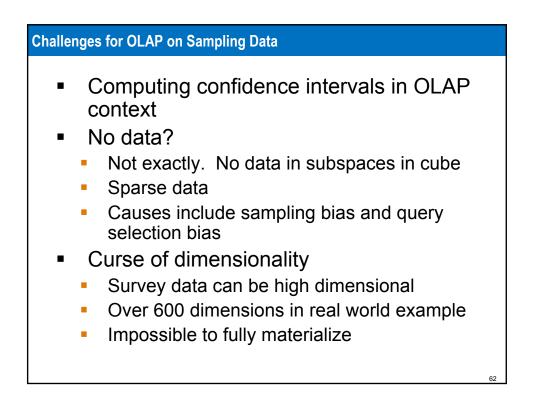
- Data cubes have been developed for sophisticated data sets and advanced applications
- Sophisticated data sets
  - » Stream cube, spatial cube, multimedia cube, text cube, RFID cube, etc. to be studied in volume 2
- Data Cubes for Advanced Applications
  - » Sampling Cube
    - X. Li, J. Han, Z. Yin, J.-G. Lee, Y. Sun, "Sampling Cube: A Framework for Statistical OLAP over Sampling Data", SIGMOD'08
  - » Ranking Cube
    - D. Xin, J. Han, H. Cheng, and X. Li. Answering top-k queries with multi-dimensional selections: The ranking cube approach. VLDB'06

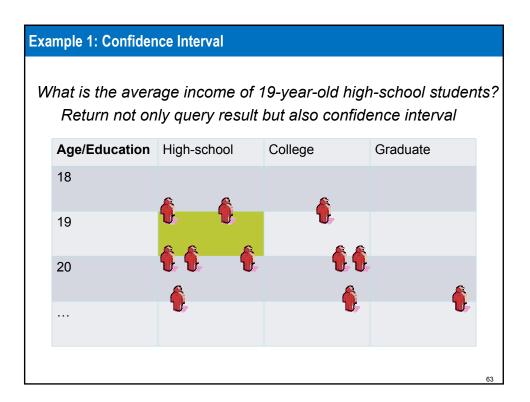


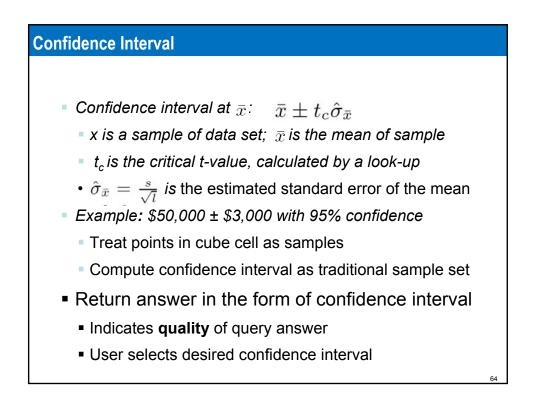
rveys: Sample vs. Whole Population						
Data is only a s	sample of <b>pop</b> u	ulation				
Age\Education		College	Graduate			
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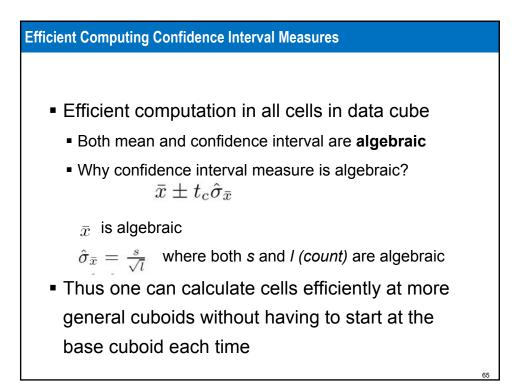


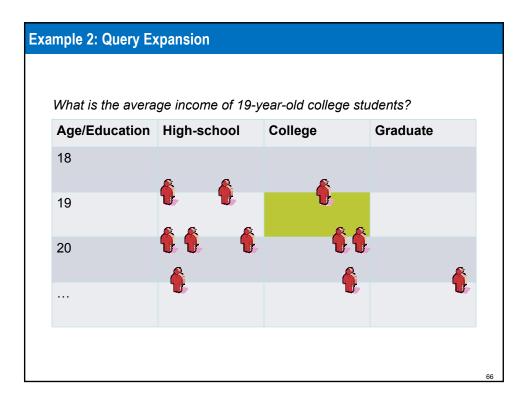


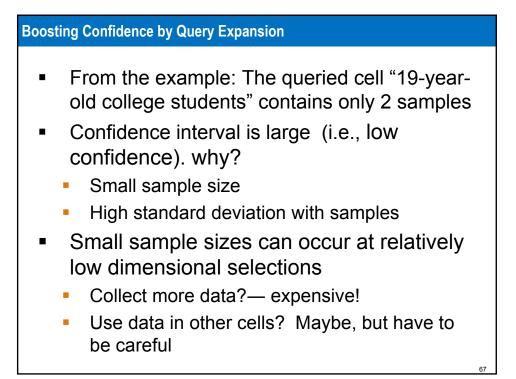


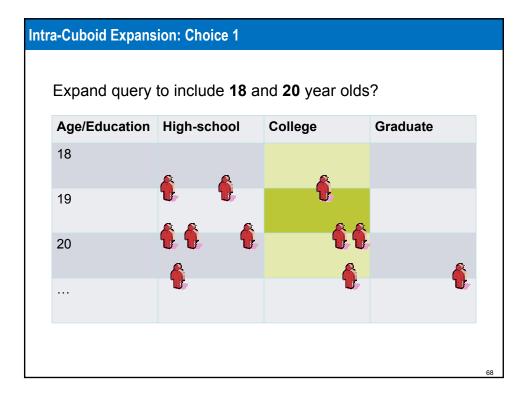


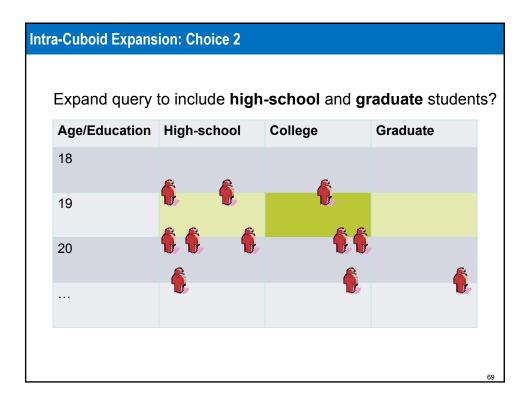


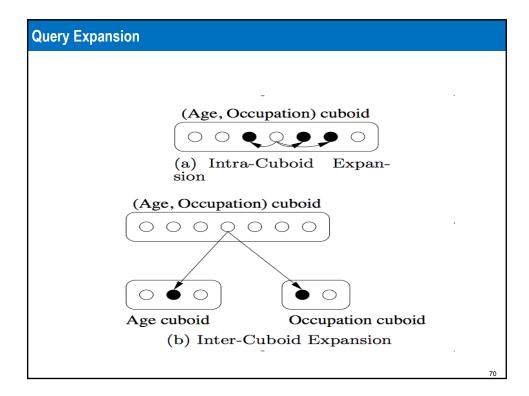


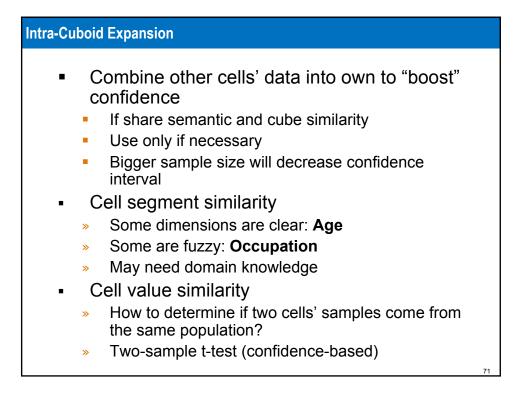






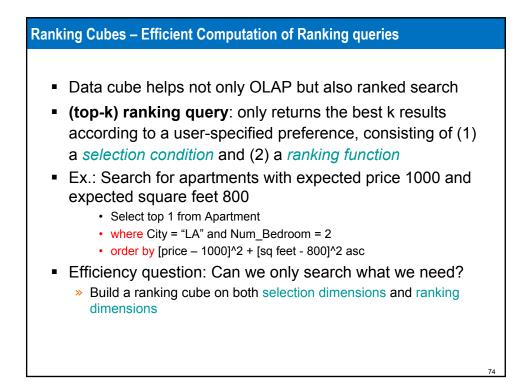


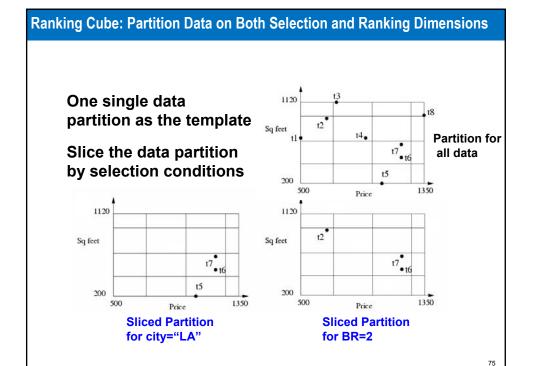


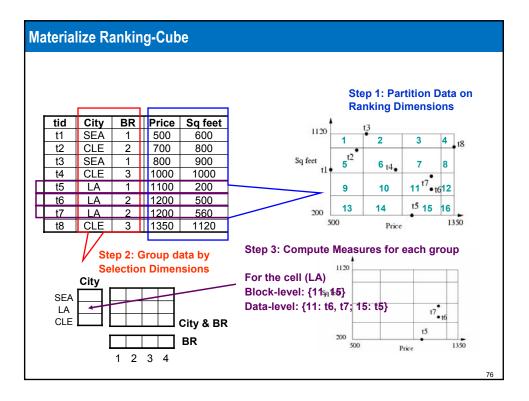


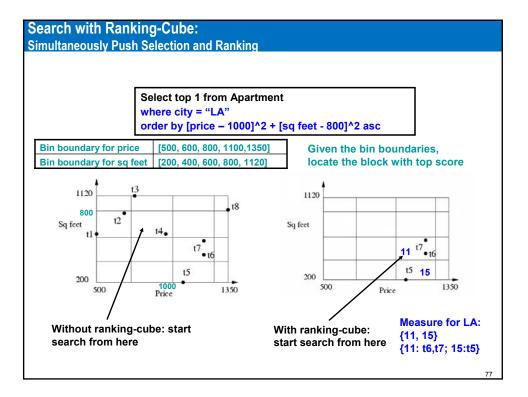
Inter-Cuboid Expansion	
<ul> <li>If a query dimension is</li> <li>Not correlated with cube value</li> <li>But is causing small sample size by drilling down too much</li> <li>Remove dimension (i.e., generalize to *) and</li> </ul>	
<ul> <li>move to a more general cuboid</li> <li>Can use two-sample t-test to determine similarity between two cells across cuboids</li> </ul>	
<ul> <li>Can also use a different method to be shown later</li> </ul>	
	72

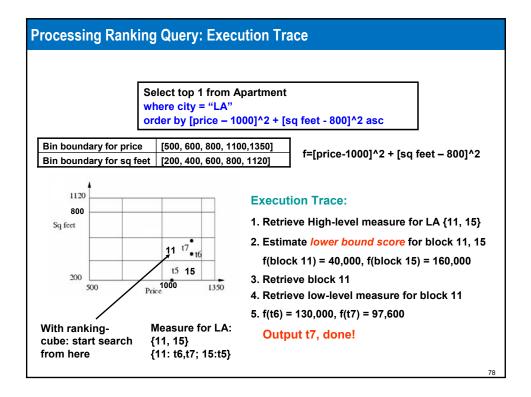
Query Expansion Experiments												
<ul> <li>Real world sample data: 600 dimensions and 750,000 tuples</li> <li>0.05% to simulate "sample" (allows error checking)</li> </ul>												
	uery		Query Ans	9	Sampling Sizes							
Gender	Marital	No Expand	Expand	% Improve	Population	Sample	Expanded					
FEMALE	MARRIED	0.48	0.32	33%	2473.0	2.2	28.3					
FEMALE	SINGLE	0.31	0.21	30%	612.6	0.6	6.4					
FEMALE	DIVORCED	0.49	0.43	11%	321.1	0.3	3.4					
MALE	MARRIED	0.42	0.21	49%	4296.8	4.4	37.6					
MALE	SINGLE	0.26	0.21	16%	571.8	0.5	3.6					
MALE	DIVORCED	0.33	0.27	19%	224.7	0.2	1.2					
	Average	0.38	0.27	26%	1416.7	1.4	13.4					
							73					

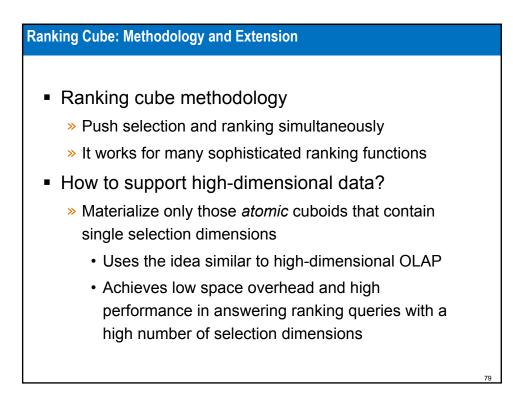


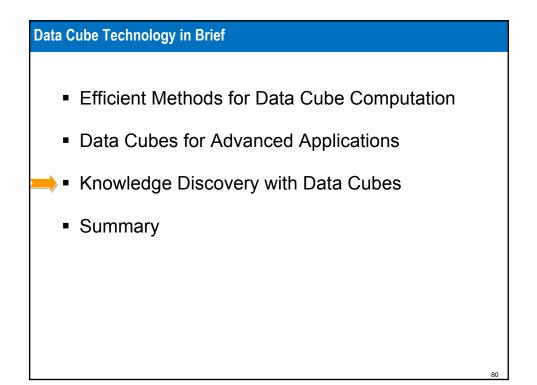




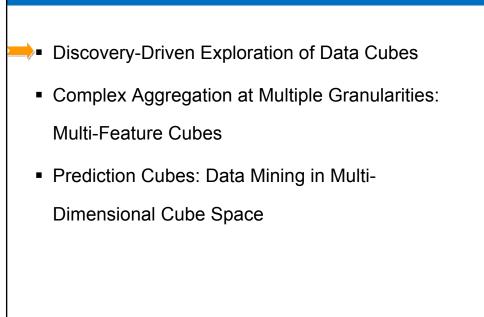


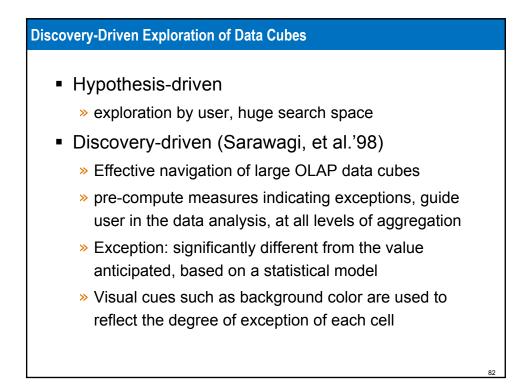


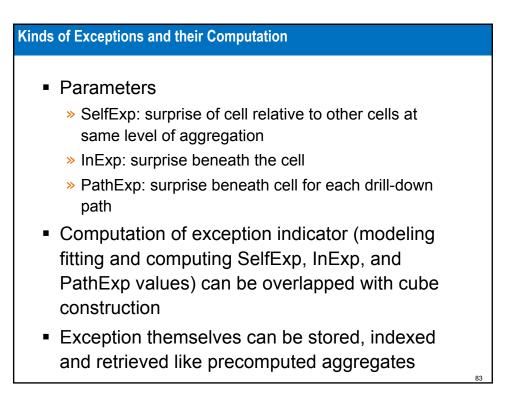




# Knowledge Discovery with Data Cubes

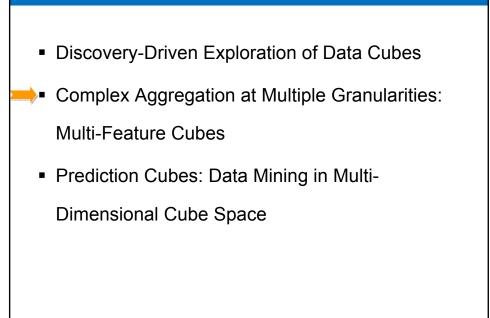




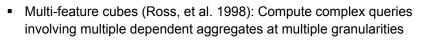


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1	Fotal		19	6 -1%	0%	1%	3%	6	- 1	-9%	6 -19	% 29	%	-4%	3%
Avg sale	s	m	nth												
item		Ja	Feb	Mar	Apr	May	Jun	Jul	ł	Aug	Sep	Oct	Nov	De	с
Sony b/w printer			9%	-8%	2%	-5%	14%	49	6 C	<b>)%</b>	41%	-13%	-159	% -11'	0%
Sony color printer			0%	0%	3%	2%	4%	-10	% -	13%	0%	4%	-6%	4%	
HP b/w printer			-2%	1%	2%	3%	8%	0%		12%	-9%	3%	-3%		
HP color printer IBM home computer		-	0% 1%	0% -2%	-2% -1%	1% -1%	0% 3%	-19		7% 1 <b>0</b> %	-2% 4%	1% 1%	-5% -4%		
IBM laptop computer			0%	0%	-1% -1%	-1% 3%	4%	2%		10%	-2%	0%	-9%		
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Toshiba laptop computer		outer	1%	0%	3%	0%	-2%	-29		5%	3%	2%	-1%		
Logitech mouse			3%	-2%	-1%	0%	4%	6%			2%	1%	-4%		
Ergo-way mouse			0%	0%	2%	3%	1%	-29	6 -	2%	-5%	0%	-5%	8%	·
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		1.07	200	100	0/7		~	4.07		7/1	100		~	0.07	200
North		-1% -1%	-3% 1%	-1%	0%			4%		7%	1%	09		-3% 1%	-3% 7%
South East		-1% -1%	-2%	2%	-39			39%		9% 2%	-34%		% 96	1% -2%	-1%
±ast West		-1% 4%	0%	-1%	-39			18%		18%	8%	59		-2% -8%	1%
v est		+70	0%	1 -1%0	-3%	v   2%	~	1.20	-	18%0	0%0	1 29	~	-8%	1 1.20

### Knowledge Discovery with Data Cubes



### **Complex Aggregation at Multiple Granularities: Multi-Feature Cubes**



 Ex. Grouping by all subsets of {item, region, month}, find the maximum price in 1997 for each group, and the total sales among all maximum price tuples

select item, region, month, max(price), sum(R.sales)

from purchases

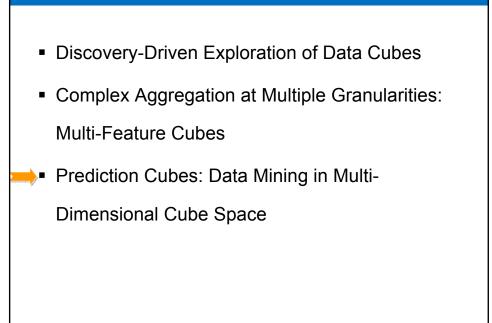
```
where year = 1997
```

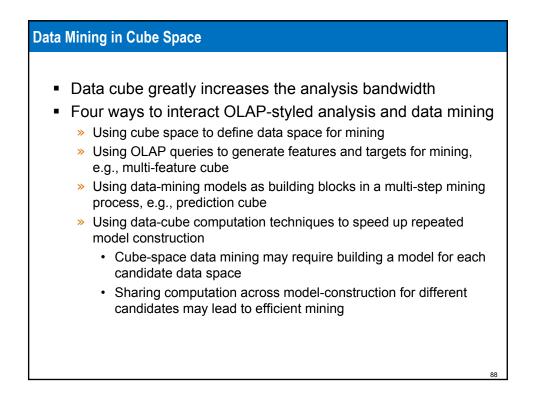
cube by item, region, month: R

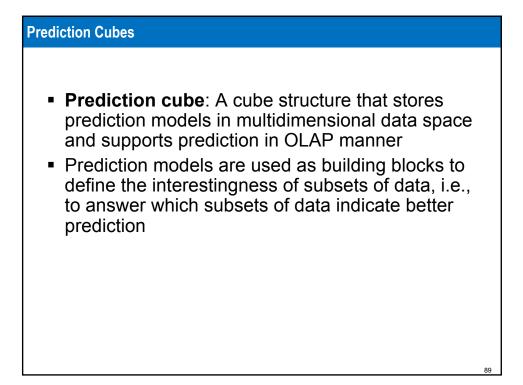
such that R.price = max(price)

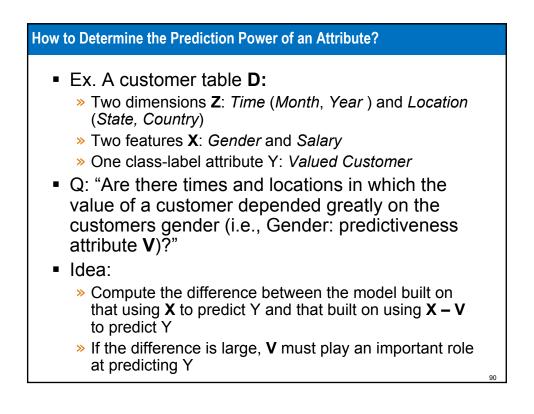
 Continuing the last example, among the max price tuples, find the min and max shelf live, and find the fraction of the total sales due to tuple that have min shelf life within the set of all max price tuples

# Knowledge Discovery with Data Cubes



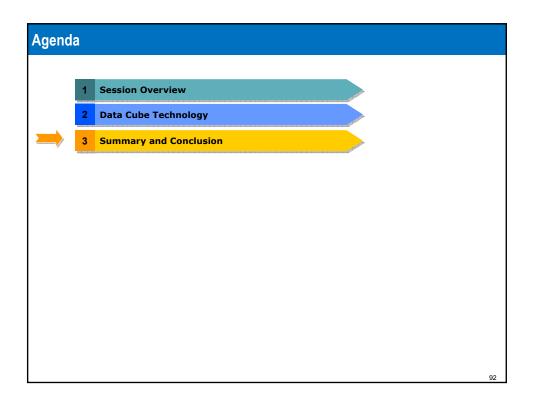






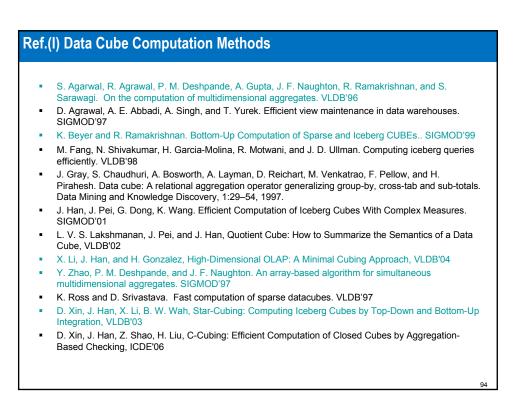


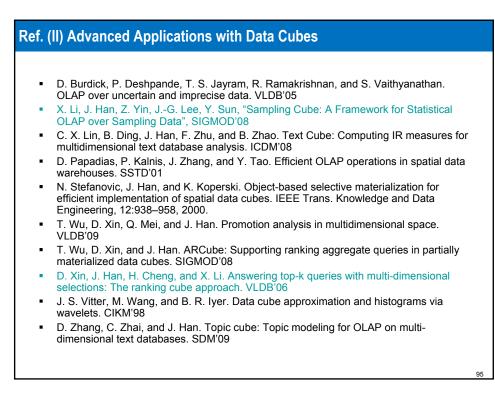
- Naïve method: Fully materialize the prediction cube, i.e., exhaustively build models and evaluate them for each cell and for each granularity
- Better approach: explore score function decomposition that reduces prediction cube computation to data cube computation



#### Data Cube Technology: Summary

- Efficient Methods for Data Cube Computation
  - MultiWay Array Aggregation
  - BUC
  - H-cubing
  - Star-Cubing
  - High-Dimensional OLAP with Shell-Fragments
- Data Cubes for Advanced Applications
  - Sampling Cubes
  - Ranking Cubes
- Knowledge Discovery with Data Cubes
  - Discovery-Driven Exploration of Data Cubes
  - Multi-feature Cubes
  - Prediction Cubes
- Much more to be studied on mining in cube space





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<ul> <li>Y. Chen, G. Dong, J. Han, B. W. Wah, and J. Wang, Multi-Dimensional Regression Analysis of Time-Series Data Streams, VLDB'02</li> </ul>	
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