N/D 3. Richard J. Morgen offers a math problem that stems from a quiz game show on TV in which three contestants get to spin a wheel. Each contestant can choose to spin one or two times. The wheel has 20 equal size segments, marked 5, 10, 15, 20, on up to 100. Each contestant can decide, in turn, whether to stop after one spin or spin again. Anyone who goes over 100 is out. A tie (which could be two way or three way) results in a one spin spinoff.

What is the best strategy? Specifically, what number should you stop on if you spin first? What if you spin second? (Obviously, if you are second, you take a second spin if your first spin does not match or exceed that achieved by the first spinner. But you need more strategy than that.) The third spinner only has to decide whether to stop if he or she ties someone.

Solution:

The first spinner should take a second spin if the first number is 65 or less. On best play, the overall odds of winning are 30.82% if this is done.

The second spinner should take a second spin if either (1) the first number is 50 or less, (2) the first number is less than the result from the first spinner, or (3) the first number ties the first spinner with that number being 65 or less. On best play, the overall odds of winning are 32.96% if this is done.

The third spinner should take a second spin if either (1) the first number is less than value needed to win, (2) the first spin ties both preceding spinners, if the tie is at 65 or less, or (3) the first spin ties only one previous spinner, if the tie is at 50 or less. (More precisely, if tied with only one previous spinner at 50, it makes no difference if a second spin is taken, or not. The odds of winning are 50/50 from that point either way.) On best play, the overall odds of winning are 36.22% if this is done.

Developing the strategy requires working backwards from the situation faced by Spinner 3. This spinner knows a value he must beat, and whether both previous spinners were tied at this value. The choices are whether to proceed or stop on a two-way or a three-way tie.

	Spinner	3, Spin 1	Sp	inner 3, Spir	n 2, Hold on '	Tie			Hold on Tie	
									Total	
	Chance	Chance	Chance to	Chance to	Chance to	Chance to	Total for	Chance to	Chance to	Chance to
To Beat	to Win	to Tie	Be Under	Win	Tie	Over 100	Spin 2	Win	Lose	Tie
0	1.00	0.00	0.0000	0.0000	0.0000	0.0000	0.0000	1.0000	0.0000	0.0000
5	0.95	0.05	0.0000	0.0000	0.0000	0.0000	0.0000	0.9500	0.0000	0.0500
10	0.90	0.05	0.0000	0.0450	0.0025	0.0025	0.0500	0.9450	0.0025	0.0525
15	0.85	0.05	0.0025	0.0850	0.0050	0.0075	0.1000	0.9350	0.0100	0.0550
20	0.80	0.05	0.0075	0.1200	0.0075	0.0150	0.1500	0.9200	0.0225	0.0575
25	0.75	0.05	0.0150	0.1500	0.0100	0.0250	0.2000	0.9000	0.0400	0.0600
30	0.70	0.05	0.0250	0.1750	0.0125	0.0375	0.2500	0.8750	0.0625	0.0625
35	0.65	0.05	0.0375	0.1950	0.0150	0.0525	0.3000	0.8450	0.0900	0.0650
40	0.60	0.05	0.0525	0.2100	0.0175	0.0700	0.3500	0.8100	0.1225	0.0675
45	0.55	0.05	0.0700	0.2200	0.0200	0.0900	0.4000	0.7700	0.1600	0.0700
50	0.50	0.05	0.0900	0.2250	0.0225	0.1125	0.4500	0.7250	0.2025	0.0725
55	0.45	0.05	0.1125	0.2250	0.0250	0.1375	0.5000	0.6750	0.2500	0.0750
60	0.40	0.05	0.1375	0.2200	0.0275	0.1650	0.5500	0.6200	0.3025	0.0775
65	0.35	0.05	0.1650	0.2100	0.0300	0.1950	0.6000	0.5600	0.3600	0.0800
70	0.30	0.05	0.1950	0.1950	0.0325	0.2275	0.6500	0.4950	0.4225	0.0825
75	0.25	0.05	0.2275	0.1750	0.0350	0.2625	0.7000	0.4250	0.4900	0.0850
80	0.20	0.05	0.2625	0.1500	0.0375	0.3000	0.7500	0.3500	0.5625	0.0875
85	0.15	0.05	0.3000	0.1200	0.0400	0.3400	0.8000	0.2700	0.6400	0.0900
90	0.10	0.05	0.3400	0.0850	0.0425	0.3825	0.8500	0.1850	0.7225	0.0925
95	0.05	0.05	0.3825	0.0450	0.0450	0.4275	0.9000	0.0950	0.8100	0.0950
100	0.00	0.05	0.4275	0.0000	0.0475	0.4750	0.9500	0.0000	0.9025	0.0975

We first analyze the case where Spinner 3 has a strategy to stop on a tie at Spin 1. Here, a second spin is made only if Spinner 3 hadn't yet won or tied on the first spin.

Alternatively, Spinner 3 can continue on a tie at Spin 1.

	Spinner	3, Spin 1	Spin	ner 3, Spin 2	, Continue o	n Tie		C	ontinue on T	ïe
									Total	
	Chance	Chance	Chance to	Chance to	Chance to	Chance to	Total for	Chance to	Chance to	Chance to
To Beat	to Win	to Tie	Be Under	Win	Tie	Over 100	Spin 2	Win	Lose	Tie
0	1.00	0.00	0.0000	0.0000	0.0000	0.0000	0.0000	1.0000	0.0000	0.0000
5	0.95	0.05	0.0000	0.0475	0.0000	0.0025	0.0500	0.9975	0.0025	0.0000
10	0.90	0.05	0.0000	0.0900	0.0025	0.0075	0.1000	0.9900	0.0075	0.0025
15	0.85	0.05	0.0025	0.1275	0.0050	0.0150	0.1500	0.9775	0.0175	0.0050
20	0.80	0.05	0.0075	0.1600	0.0075	0.0250	0.2000	0.9600	0.0325	0.0075
25	0.75	0.05	0.0150	0.1875	0.0100	0.0375	0.2500	0.9375	0.0525	0.0100
30	0.70	0.05	0.0250	0.2100	0.0125	0.0525	0.3000	0.9100	0.0775	0.0125
35	0.65	0.05	0.0375	0.2275	0.0150	0.0700	0.3500	0.8775	0.1075	0.0150
40	0.60	0.05	0.0525	0.2400	0.0175	0.0900	0.4000	0.8400	0.1425	0.0175
45	0.55	0.05	0.0700	0.2475	0.0200	0.1125	0.4500	0.7975	0.1825	0.0200
50	0.50	0.05	0.0900	0.2500	0.0225	0.1375	0.5000	0.7500	0.2275	0.0225
55	0.45	0.05	0.1125	0.2475	0.0250	0.1650	0.5500	0.6975	0.2775	0.0250
60	0.40	0.05	0.1375	0.2400	0.0275	0.1950	0.6000	0.6400	0.3325	0.0275
65	0.35	0.05	0.1650	0.2275	0.0300	0.2275	0.6500	0.5775	0.3925	0.0300
70	0.30	0.05	0.1950	0.2100	0.0325	0.2625	0.7000	0.5100	0.4575	0.0325
75	0.25	0.05	0.2275	0.1875	0.0350	0.3000	0.7500	0.4375	0.5275	0.0350
80	0.20	0.05	0.2625	0.1600	0.0375	0.3400	0.8000	0.3600	0.6025	0.0375
85	0.15	0.05	0.3000	0.1275	0.0400	0.3825	0.8500	0.2775	0.6825	0.0400
90	0.10	0.05	0.3400	0.0900	0.0425	0.4275	0.9000	0.1900	0.7675	0.0425
95	0.05	0.05	0.3825	0.0475	0.0450	0.4750	0.9500	0.0975	0.8575	0.0450
100	0.00	0.05	0.4275	0.0000	0.0475	0.5250	1.0000	0.0000	0.9525	0.0475

A tie leads to a tie breaker, where each spinner has 50 % odds (on a two-way tie), or 33 % odds (on a three-way tie). From this, we see the chance for eventually winning in both cases, for both strategies. (Optimal strategy in green.)

	Two-V	Vay Tie	Three-	Way Tie	Chance to	win with	Chance to	b Lose with
	(50% Win or	n Tie Breaker)	(33% Win or	n Tie Breaker)	Best S	trategy	Best S	trategy
	Chance to Win	Chance to Win	Chance to Win	Chance to Win		Three-Way	Two-Way	Three-Way
To Beat		on Cont Strategy		on Cont Strategy	Tie	Tie	Tie	Tie
0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.0000	0.0000
5	0.9750	0.9975	0.9667	0.9975	0.9975	0.9975	0.0025	0.0025
10	0.9713	0.9913	0.9625	0.9908	0.9913	0.9908	0.0088	0.0092
15	0.9625	0.9800	0.9533	0.9792	0.9800	0.9792	0.0200	0.0208
20	0.9488	0.9638	0.9392	0.9625	0.9638	0.9625	0.0362	0.0375
25	0.9300	0.9425	0.9200	0.9408	0.9425	0.9408	0.0575	0.0592
30	0.9063	0.9163	0.8958	0.9142	0.9163	0.9142	0.0838	0.0858
35	0.8775	0.8850	0.8667	0.8825	0.8850	0.8825	0.1150	0.1175
40	0.8438	0.8488	0.8325	0.8458	0.8488	0.8458	0.1513	0.1542
45	0.8050	0.8075	0.7933	0.8042	0.8075	0.8042	0.1925	0.1958
50	0.7613	0.7613	0.7492	0.7575	0.7613	0.7575	0.2388	0.2425
55	0.7125	0.7100	0.7000	0.7058	0.7125	0.7058	0.2875	0.2942
60	0.6588	0.6538	0.6458	0.6492	0.6588	0.6492	0.3413	0.3508
65	0.6000	0.5925	0.5867	0.5875	0.6000	0.5875	0.4000	0.4125
70	0.5363	0.5263	0.5225	0.5208	0.5363	0.5225	0.4638	0.4775
75	0.4675	0.4550	0.4533	0.4492	0.4675	0.4533	0.5325	0.5467
80	0.3938	0.3788	0.3792	0.3725	0.3938	0.3792	0.6063	0.6208
85	0.3150	0.2975	0.3000	0.2908	0.3150	0.3000	0.6850	0.7000
90	0.2313	0.2113	0.2158	0.2042	0.2313	0.2158	0.7688	0.7842
95	0.1425	0.1200	0.1267	0.1125	0.1425	0.1267	0.8575	0.8733
100	0.0488	0.0238	0.0325	0.0158	0.0488	0.0325	0.9513	0.9675

The third spinner should take an elective second spin on a two-way tie (if the first spin ties only one of the preceding spinners) if the tie is at 50 or less, and an elective second spin on a three-way tie (if the first spin ties both preceding spinners) if the tie is at 65 or less.

The second spinner must take a second spin if the first did not tie or exceed the score from the first spinner. However, when should he elect a second spin otherwise? If we assume for the moment that the first spin exceeded the previous score (which precludes the chance of a three-way tie), we know from the above the chance of Spinner 2 winning (which is the chance of Spinner 3 losing) for all outcomes of one and two spins.

	Chance					Spin 2, F	Probabili	ty to Wir	over Sp	inner 3 i	f Ahead	of Spinne	er 1 Afte	r 1 Spin	(Not Tie	d, and W	on't Tie)					Average
	to Win																					Chance
Spin 1	if Stop	5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100	to Win
5	0.0025	0.0088	0.0200	0.0362	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.3399
10	0.0088	0.0200	0.0362	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.3394
15	0.0200	0.0362	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.3384
20	0.0362	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.3366
25	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.3338
30	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.3296
35	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.3238
40	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.3163
45	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.3066
50	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2947
55	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2803
60	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2633
65	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2433
70	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2201
75	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1934
80	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1631
85	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1289
90	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0904
95	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0476
100	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000

The best strategy, highlighted in green, is to electively spin a second time if the first spin results in 50 or less.

When Spinner 2 ties with Spinner 1 after one spin, it is not enough to just win over Spinner 3. There is only a 50 % chance of ultimately winning over Spinner 1.

	Chance					Spin 2,	Probabili	ty to Wi	n over Sp	pinner 3	if Tied w	ith Spin	ner 1 Aft	er 1 Spir	(Not Tie	ed After	2 Spins)					Average
	to Win																					Chance
Spin 1	if Stop	5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100	to Win
5	0.0012	0.0088	0.0200	0.0362	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.3399
10	0.0046	0.0200	0.0362	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.3394
15	0.0104	0.0362	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.3384
20	0.0188	0.0575	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.3366
25	0.0296	0.0838	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.3338
30	0.0429	0.1150	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.3296
35	0.0588	0.1513	0.1925	0.2388	0.2875	0.3413	0.4000	0.4638	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.3238
40	0.0771			0.2875																		0.3163
45	0.0979			0.3413																		0.3066
50	0.1213			0.4000																		0.2947
55	0.1213			0.4638												0.0000						0.2803
60	0.1754	0.4000																	0.0000	0.0000		0.2633
65	0.2063			0.6063								0.0000				0.0000						0.2433
70	0.2388	0.5325	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2201
75	0.2733	0.6063	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1934
80	0.3104	0.6850	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1631
85	0.3500	0.7688	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1289
90	0.3921	0.8575	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0904
95	0.4367	0.9513	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0476
100	0.4838	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000					0.0000	0.0000	0.0000	0.0000

Here, the best strategy, highlighted in green, is to electively spin a second time if the first spin results in 65 or less.

Given these strategies, we can deduce the probabilities of the various possible Total Spin outcomes for Spinner 2, given the "To Beat" value known from Spinner 1.

						SPINNER	2, CHAN	ICES OF	SPIN OU	TCOME	(TOTAL	SPIN) W	HEN EMI	PLOYING	BEST ST	RATEGY	,				
										To Beat	(From S	oinner 1)									
Total Spin																					
Spinner 2	0	5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100
5	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
10	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025	0.0025
15	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050	0.0050
20	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075	0.0075
25	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100	0.0100
30	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125	0.0125
35	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150	0.0150
40	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175	0.0175
45	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200	0.0200
50	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225	0.0225
55	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0250	0.0250	0.0250	0.0250	0.0250	0.0250	0.0250	0.0250	0.0250	0.0250
60	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0275	0.0275	0.0275	0.0275	0.0275	0.0275	0.0275	0.0275	0.0275
65	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0300	0.0300	0.0300	0.0300	0.0300	0.0300	0.0300	0.0300
70	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0825	0.0825	0.0325	0.0325	0.0325	0.0325	0.0325	0.0325
75	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0825	0.0825	0.0850	0.0350	0.0350	0.0350	0.0350	0.0350
80	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0825	0.0825	0.0850	0.0875	0.0375	0.0375	0.0375	0.0375
85	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0825	0.0825	0.0850	0.0875	0.0900	0.0400	0.0400	0.0400
90	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0825	0.0825	0.0850	0.0875	0.0900	0.0925	0.0425	0.0425
95	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0825	0.0825	0.0850	0.0875	0.0900	0.0925	0.0950	0.0450
100	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0750	0.0775	0.0800	0.0825	0.0825	0.0850	0.0875	0.0900	0.0925	0.0950	0.0975
Over	0.1375	0.1375	0.1375	0.1375	0.1375	0.1375	0.1375	0.1375	0.1375	0.1375	0.1375	0.1650	0.1950	0.2275	0.2275	0.2625	0.3000	0.3400	0.3825	0.4275	0.4750
Total	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

For each of these combinations, we also know the chance that Spinner 2 will win, and hence we know the overall probability that Spinner 2 will win for each possible To Beat value from Spinner 1.

				c	HANCE C	OF SPINN	ER 2 WI	NNING,	FOR A G	IVEN TO	-BEAT (from SPI	NNER 1)	and SPI	N TOTAL	(from S	PINNER	2)			
										To Beat	(From S	pinner 1									
Total Spin																					
Spinner 2	0	5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100
5	0.0025	0.0012																			
10	0.0088	0.0088	0.0046																		
15	0.0200	0.0200	0.0200	0.0104																	
20	0.0362	0.0362	0.0362	0.0362	0.0188																
25	0.0575	0.0575	0.0575	0.0575	0.0575	0.0296															
30	0.0838	0.0838	0.0838	0.0838	0.0838	0.0838	0.0429														
35	0.1150	0.1150	0.1150	0.1150	0.1150	0.1150	0.1150	0.0588													
40	0.1513	0.1513	0.1513	0.1513	0.1513	0.1513	0.1513	0.1513	0.0771												
45	0.1925	0.1925	0.1925	0.1925	0.1925	0.1925	0.1925	0.1925	0.1925	0.0979											
50	0.2388	0.2388	0.2388	0.2388	0.2388	0.2388	0.2388	0.2388	0.2388	0.2388	0.1213										
55	0.2875	0.2875	0.2875	0.2875	0.2875	0.2875	0.2875	0.2875	0.2875	0.2875	0.2875	0.1471									
60	0.3413	0.3413	0.3413	0.3413	0.3413	0.3413	0.3413	0.3413	0.3413	0.3413	0.3413	0.3413	0.1754								
65	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.4000	0.2063							
70	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.4638	0.2388						
75	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.5325	0.2733					
80	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.6063	0.3104				
85	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.6850	0.3500			
90	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.7688	0.3921		
95	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.8575	0.4367	
100	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.9513	0.4838
Over																					
Spinner 2 Wins	0.4576	0.4576	0.4576	0.4576	0.4574	0.4570	0.4562	0.4548	0.4526	0.4494	0.4448	0.4382	0.4260	0.4076	0.3828	0.3521	0.3126	0.2635	0.2036	0.1319	0.0472

(The bottom-line totals are the dot product of the corresponding columns from the preceding two charts.)

Similarly, for each "To Beat" value from Spinner 1, we can compute the probability that Spinner 3 wins, and hence the probability that Spinner 1 wins.

				C	HANCE C	OF SPINN	ER 3 WI	NNING,	FOR A G	IVEN TO	BEAT (from SPI	NNER 1)	and SPI	N TOTAL	(from S	PINNER	2)			
										To Beat	(From S	pinner 1)									
Total Spin																					
Spinner 2	0	5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100
5	0.9975	0.9975	0.9913	0.9800	0.9638	0.9425	0.9163	0.8850	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
10	0.9913	0.9913	0.9908	0.9800	0.9638	0.9425	0.9163	0.8850	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
15	0.9800	0.9800	0.9800	0.9792	0.9638	0.9425	0.9163	0.8850	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
20	0.9638	0.9638	0.9638	0.9638	0.9625	0.9425	0.9163	0.8850	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
25	0.9425	0.9425	0.9425	0.9425	0.9425	0.9408	0.9163	0.8850	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
30	0.9163	0.9163	0.9163	0.9163	0.9163	0.9163	0.9142	0.8850	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
35	0.8850	0.8850	0.8850	0.8850	0.8850	0.8850	0.8850	0.8825	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
40	0.8488	0.8488	0.8488	0.8488	0.8488	0.8488	0.8488	0.8488	0.8458	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
45	0.8075	0.8075	0.8075	0.8075	0.8075	0.8075	0.8075	0.8075	0.8075	0.8042	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
50	0.7613	0.7613	0.7613	0.7613	0.7613	0.7613	0.7613	0.7613	0.7613	0.7613	0.7575	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
55	0.7125	0.7125	0.7125	0.7125	0.7125	0.7125	0.7125	0.7125	0.7125	0.7125	0.7125	0.7058	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
60	0.6588	0.6588	0.6588	0.6588	0.6588	0.6588	0.6588	0.6588	0.6588	0.6588	0.6588	0.6588	0.6492	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
65	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.6000	0.5875	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
70	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5363	0.5225	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
75	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4675	0.4533	0.3938	0.3150	0.2313	0.1425	0.0488
80	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3938	0.3792	0.3150	0.2313	0.1425	0.0488
85	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3150	0.3000	0.2313	0.1425	0.0488
90	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2313	0.2158	0.1425	0.0488
95	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1425	0.1267	0.0488
100	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0488	0.0325
Over	1.0000	0.9975	0.9913	0.9800	0.9638	0.9425	0.9163	0.8850	0.8488	0.8075	0.7613	0.7125	0.6588	0.6000	0.5363	0.4675	0.3938	0.3150	0.2313	0.1425	0.0488
Spinner 3 Wins	0.5424	0.5420	0.5412	0.5396	0.5372	0.5340	0.5297	0.5242	0.5173	0.5087	0.4982	0.4784	0.4557	0.4293	0.4016	0.3638	0.3192	0.2666	0.2047	0.1321	0.047
Spinner 1 Wins	0.0000	0.0003	0.0012	0.0029	0.0054	0.0091	0.0141	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.905

This allows Spinner 1 to decide on strategy.

	Chance								S	pinner 1	, Spin 2,	Probabil	ity to Wi	n								Average
	to Win																					Chance
Spin 1	if Stop	5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100	to Win
5	0.0003	0.0012	0.0029	0.0054	0.0091	0.0141	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.2059
10	0.0012	0.0029	0.0054	0.0091	0.0141	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.2059
15	0.0029	0.0054	0.0091	0.0141	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.2057
20	0.0054	0.0091	0.0141	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.2055
25	0.0091	0.0141	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.2050
30	0.0141	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2043
35	0.0210	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2033
40	0.0301	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.2018
45	0.0419	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1997
50	0.0570	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1968
55	0.0835	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1926
60	0.1183	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1867
65	0.1632	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1786
70	0.2156	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1678
75	0.2842	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1536
80	0.3682	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1352
85	0.4699	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.1117
90	0.5917	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0821
95	0.7361	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0453
100	0.9057	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000

The best strategy for Spinner 1 is to elect a second spin if the first is 65 or less.

Knowing that Spinner 1 will spin twice if the result of the first spin is 65 or less, we can compute the probabilities of each possible outcome from Spinner 1. Furthermore, we can compute the probability of each spinner winning.

Total Spin	Chance of	Chance of
Spinner 1	Occurring	Winning
0 (Over)	0.2275	0.0000
5	0.0000	0.0003
10	0.0025	0.0012
15	0.0050	0.0029
20	0.0075	0.0054
25	0.0100	0.0091
30	0.0125	0.0141
35	0.0150	0.0210
40	0.0175	0.0301
45	0.0200	0.0419
50	0.0225	0.0570
55	0.0250	0.0835
60	0.0275	0.1183
65	0.0300	0.1632
70	0.0825	0.2156
75	0.0825	0.2842
80	0.0825	0.3682
85	0.0825	0.4699
90	0.0825	0.5917
95	0.0825	0.7361
100	0.0825	0.9057
Total	1.0000	
Chance Sp	inner 1 Wins	0.3082
Chance Sp	inner 2 Wins	0.3296
Chance Sp	inner 3 Wins	0.3622
	Total	1.0000