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N := 30 : for n from 1 to N do for m from 1 to n - 1 do f[n, n, m] := 0 od: f[n, n, n] := 1 : for k
from 1 to n do for m from n + 1 to N do f[n, k, m] := 0 od od: for k from 1 to n do for m
from 1 to k - 1 do f[n, k, m] := 0 od od od: for n from 2 to N do for k from n - 1 to 2 by -1
do for m from k + 1 to n do f[n, k, m] :=  $\frac{k}{2n - k} \cdot (f[n - 1, k - 1, m]) + \frac{(2n - 2k)}{2n - k} \cdot f[n, k + 1, m]$ :
f[n, k, k] :=  $\frac{k}{2n - k} \cdot \text{add}(f[n - 1, k - 1, mp], mp = 1..k) + \frac{(2n - 2k)}{2n - k} \cdot f[n, k + 1, k]$ 
od od : for m from 1 to n do f[n, 1, m] :=  $\frac{1}{2n - 1} \cdot f[n - 1, 1, m] + \frac{(2n - 2)}{2n - 1} \cdot f[n, 2, m]$ 
od od: for n from 1 to N do print("expected value", n, add(f[n, 1, m]·m, m = 1..n),
evalf(add(f[n, 1, m]·m, m = 1..n))) od:
#NOTE f[n,k,m] is the probability that the maximum number of socks on the bed from this point on
will be m, given that we currently have n pairs of socks in play and there are k socks on the bed now.

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"expected value", 1, 1, 1.
"expected value", 2,  $\frac{5}{3}$ , 1.666666667
"expected value", 3,  $\frac{7}{3}$ , 2.333333333
"expected value", 4,  $\frac{311}{105}$ , 2.961904762
"expected value", 5,  $\frac{3377}{945}$ , 3.573544974
"expected value", 6,  $\frac{3943}{945}$ , 4.172486772
"expected value", 7,  $\frac{18385}{3861}$ , 4.761719762
"expected value", 8,  $\frac{10831151}{2027025}$ , 5.343373170
"expected value", 9,  $\frac{203961377}{34459425}$ , 5.918885095
"expected value", 10,  $\frac{4248732053}{654729075}$ , 6.489297963
"expected value", 11,  $\frac{1021124893}{144729585}$ , 7.055398473
"expected value", 12,  $\frac{2409006894311}{316234143225}$ , 7.617795061
"expected value", 13,  $\frac{1319304498593}{161343950625}$ , 8.176969099
"expected value", 14,  $\frac{1864195055263613}{213458046676875}$ , 8.733308883

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- "expected value", 15, $\frac{499912897075649}{53828550901125}$, 9.287132734
- "expected value", 16, $\frac{65104674955222699}{6617199446983125}$, 9.838705252
- "expected value", 17, $\frac{65785247971229129537}{6332659870762850625}$, 10.38824906
- "expected value", 18, $\frac{10967776372033537513}{1002909934283709375}$, 10.93595347
- "expected value", 19, $\frac{818794491347250948689}{71311256805546883125}$, 11.48198094
- "expected value", 20, $\frac{226261084752832183400743}{18813587457228104165625}$, 12.02647211
- "expected value", 21, $\frac{1152625100577317466744319}{91699793410405514709375}$, 12.56954959
- "expected value", 22, $\frac{7392976092801737927394363533}{563862029680583509947946875}$, 13.11132104
- "expected value", 23, $\frac{9897142669769557951327009681}{724965466732178798504503125}$, 13.65188154
- "expected value", 24, $\frac{457408419333327691995322190243}{32231572777687408744321828125}$, 14.19131553
- "expected value", 25, $\frac{860742320784169391147790879059297}{58435841445947272053455474390625}$, 14.72969841
- "expected value", 26, $\frac{45499430980850068304217998123975093}{2980227913743310874726229193921875}$, 15.26709779
- "expected value", 27, $\frac{1226637574427356092419318919774641}{77617729448842985926530784903125}$, 15.80357456
- "expected value", 28, $\frac{141944443181242688207031345291907073351}{8687364368561751199826958100282265625}$, 16.33918380
- "expected value", 29, $\frac{1193664470287895135718041660658069961511}{70739967001145688341448087388012734375}$, 16.87397550
- "expected value", 30, $\frac{2505345492674107248078780684347543728951}{143919243209227434901566798479060390625}$, 17.40799518

(1)