Unsupervised Learning

Lecture 12

Motivation

- Goal: learn structure of data to yield generic representation, useful for many different tasks
- Supervised learning: given labels/targets for a particular task
 - Task strongly constrains objective function



- In unsupervised learning, where do labels/output targets come from?
 - What is the objective?

Motivation

• Most successes obtained with supervised models, e.g. Convnets



• Unsupervised learning methods less successful

• But likely to be very important in long-term

Different Perspectives on Unsupervised Learning

<u>1. Density estimation</u> Given data {x}, build p(x).

E.g. k-Means, PCA, RBMs, sparse coding etc.

Assumption: good model of data requires representation that will be generically useful 2. Train model to use "free-labels" from task that is somewhat similar to one we actually care about

- Often called "self-supervised" learning
- Free-labels often come from exploiting knowledge of domain

Historical Note

- Deep Learning revival started in ~2006
 Hinton & Salakhudinov Science paper on RBMs
- Unsupervised Learning was focus from 2006-2012

- In ~2012 great results in vision, speech with supervised methods appeared
 - Less interest in unsupervised learning

Arguments for Unsupervised Learning

- Want to be able to exploit unlabeled data
 - Vast amount of it often available
 - Essentially free
- Good regularizer for supervised learning
 - Helps generalization
 - Transfer learning
 - Zero / one-shot learning

Another Argument for Unsupervised Learning

When we're learning to see, nobody's telling us what the right answers are — we just look. Every so often, your mother says "that's a dog", but that's very little information.

You'd be lucky if you got a few bits of information — even one bit per second — that way. The brain's visual system has 10^{14} neural connections. And you only live for 10^9 seconds.

So it's no use learning one bit per second. You need more like 10^5 bits per second. And there's only one place you can get that much information: from the input itself.

— Geoffrey Hinton, 1996

Taxonomy of Approaches

- Autoencoder (most common)
 - RBMs / DBMs
 - Denoising autoencoders
 - Predictive sparse decomposition
- Decoder-only
 - Sparse coding
 - Deconvolutional Nets

Loss involves some kind of reconstruction error

- Encoder-only
 - Implicit or self-supervision, e.g. from video
- Adversarial Networks [to be covered in class on 12/16]

Auto-Encoder



Auto-Encoder Example 1

• Restricted Boltzmann Machine [Hinton '02]



Auto-Encoder Example 2

• Predictive Sparse Decomposition [Ranzato et al., '07]



Auto-Encoder Example 2

• Predictive Sparse Decomposition [Kavukcuoglu et al., '09]



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Energy-Based Unsupervised Learning

Energy-Based Unsupervised Learning

Learning an energy function (or contrast function) that takes

- Low values on the data manifold
- Higher values everywhere else





The energy surface is a "contrast function" that takes low values on the data manifold, and higher values everywhere else

Special case: energy = negative log density

Example: the samples live in the manifold $Y_2 = Y_1^2$



Transforming Energies into Probabilities (if necessary)

The energy can be interpreted as an unnormalized negative log density

Gibbs distribution: Probability proportional to exp(-energy)

Beta parameter is akin to an inverse temperature

Don't compute probabilities unless you absolutely have to

Because the denominator is often intractable



Learning the Energy Function

parameterized energy function E(Y,W)

- Make the energy low on the samples
- Make the energy higher everywhere else
- Making the energy low on the samples is easy
- But how do we make it higher everywhere else?



Seven Strategies to Shape the Energy Function

- **1. build the machine so that the volume of low energy stuff is constant** PCA, K-means, GMM, square ICA
- **2. push down of the energy of data points, push up everywhere else** Max likelihood (needs tractable partition function)
- **3. push down of the energy of data points, push up on chosen locations** contrastive divergence, Ratio Matching, Noise Contrastive Estimation, Minimum Probability Flow
- **4. minimize the gradient and maximize the curvature around data points** score matching
- **5. train a dynamical system so that the dynamics goes to the manifold** denoising auto-encoder
- 6. use a regularizer that limits the volume of space that has low energy
 Sparse coding, sparse auto-encoder, PSD
- 7. if E(Y) = ||Y G(Y)||^2, make G(Y) as "constant" as possible.
 Contracting auto-encoder, saturating auto-encoder

1. build the machine so that the volume of low energy stuff is constant
 PCA, K-means, GMM, square ICA...

PCA $E(Y) = // W_T W Y - Y // 2$



K-Means, Z constrained to 1-of-K code $E(Y) = min_z \sum_i // Y - W_i Z_i // 2$





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Max likelihood (requires a tractable partition function)





Sparse coding, sparse auto-encoder, Predictive Saprse Decomposition



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Sparse Modeling, Sparse Auto-Encoders, Predictive Sparse Decomposition LISTA

How to Speed Up Inference in a Generative Model?

Factor Graph with an asymmetric factor

Inference $Z \rightarrow Y$ is easy

Run Z through deterministic decoder, and sample Y

Inference $Y \rightarrow Z$ is hard, particularly if Decoder function is many-to-one

- MAP: minimize sum of two factors with respect to Z
- \sim Z* = argmin_z Distance[Decoder(Z), Y] + FactorB(Z)

Examples: K-Means (1of K), Sparse Coding (sparse), Factor Analysis



Sparse Coding & Sparse Modeling

[Olshausen & Field 1997]

Sparse linear reconstruction

Energy = reconstruction_error + code_prediction_error + code_sparsity

$$E(\underline{Y}^{i}(\underline{Y}^{J}, \overline{Z})) = \|\underline{Y}^{i}\|_{T} W_{d} \|\underline{Z}^{i}\|_{T}^{2} + \sum_{d} \sum_{j} |z_{j}|$$





Examples: most ICA models, Product of Experts



Encoder-Decoder Architecture

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[Kavukcuoglu, Ranzato, LeCun, rejected by every conference, 2008-2009]

Train a "simple" feed-forward function to predict the result of a complex optimization on the data points of interest



1. Find optimal Zi for all Yi; 2. Train Encoder to predict Zi from Yi

- Training sample
- Input vector which is NOT a training sample
- Feature vector





- Training sample
- Input vector which is NOT a training sample
- Feature vector

Training based on minimizing the reconstruction error over the training set



- Training sample
- Input vector which is NOT a training sample
- Feature vector

BAD: machine does not learn structure from training data!! It just copies the data.



- Training sample
- Input vector which is NOT a training sample
- Feature vector

IDEA: reduce number of available codes.







- Training sample
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IDEA: reduce number of available codes.





- Training sample
- Input vector which is NOT a training sample
- Feature vector

IDEA: reduce number of available codes.



Predictive Sparse Decomposition (PSD): sparse auto-encoder Y LeCun MA Ranzato

[Kavukcuoglu, Ranzato, LeCun, 2008 \rightarrow arXiv:1010.3467],

Prediction the optimal code with a trained encoder

Energy = reconstruction_error + code_prediction_error + code_sparsity

$$E(Y^{i}, Z) = ||Y^{i} - W_{d}Z||^{2} + ||Z - g_{e}(W_{e}, Y^{i})||^{2} + \lambda \sum_{j} |z_{j}|$$

$$g_{e}(W_{e}, Y^{i}) = shrinkage(W_{e}Y^{i})$$



PSD: Basis Functions on MNIST

Basis functions (and encoder matrix) are digit parts

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Learned Features on natural patches: V1-like receptive fields

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Convolutional Sparse Coding

Replace the dot products with dictionary element by convolutions.

- Input Y is a full image
- Each code component Zk is a feature map (an image)
- Each dictionary element is a convolution kernel

Regular sparse coding
$$E(Y,Z) = ||Y - \sum_{k} W_k Z_k||^2 + \alpha \sum_{k} |Z_k|$$

Convolutional S.C.
$$E(Y,Z) = ||Y - \sum_k W_k * Z_k||^2 + \alpha \sum_k |Z_k|$$

$$\mathbf{Y} = \sum_{k} \cdot \mathbf{w}_{k} * \mathbf{z}_{k}$$

"deconvolutional networks" [Zeiler, Taylor, Fergus CVPR 2010]
Convolutional PSD: Encoder with a soft sh() Function

Convolutional Formulation

Extend sparse coding from *PATCH* to *IMAGE*

$$\mathcal{L}(x, z, \mathcal{D}) = \frac{1}{2} ||x - \sum_{k=1}^{K} \mathcal{D}_k * z_k||_2^2 + \sum_{k=1}^{K} ||z_k - f(W^k * x)||_2^2 + |z|_1$$



▶ *PATCH* based learning

CONVOLUTIONAL learning

Convolutional Sparse Auto-Encoder on Natural Images

Filters and Basis Functions obtained with 1, 2, 4, 8, 16, 32, and 64 filters.





Phase 1: train first layer using PSD



FEATURES



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Phase 1: train first layer using PSD

Phase 2: use encoder + absolute value as feature extractor



FEATURES



- Phase 1: train first layer using PSD
- Phase 2: use encoder + absolute value as feature extractor
- Phase 3: train the second layer using PSD



Using PSD to Train a Hierarchy of Features

- Phase 1: train first layer using PSD
- Phase 2: use encoder + absolute value as feature extractor
- Phase 3: train the second layer using PSD
- Phase 4: use encoder + absolute value as 2nd feature extractor



- Phase 1: train first layer using PSD
- Phase 2: use encoder + absolute value as feature extractor
- Phase 3: train the second layer using PSD
- Phase 4: use encoder + absolute value as 2nd feature extractor
- Phase 5: train a supervised classifier on top
- Phase 6 (optional): train the entire system with supervised back-propagation



Pedestrian Detection, Face Detection

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[Osadchy,Miller LeCun JMLR 2007],[Kavukcuoglu et al. NIPS 2010] [Sermanet et al. CVPR 2013]

ConvNet Architecture with Multi-Stage Features

Feature maps from all stages are pooled/subsampled and sent to the final classification layers

Pooled low-level features: good for textures and local motifs

▶ High-level features: good for "gestalt" and global shape



[Sermanet, Chintala, LeCun CVPR 2013]

Pedestrian Detection: INRIA Dataset. Miss rate vs false

positives

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[Kavukcuoglu et al. NIPS 2010] [Sermanet et al. ArXiv 2012]

Stacked Auto-Encoders



Training phase 2: Supervised Fine-Tuning



Effects of Pre-Training

• From [Hinton & Salakhudinov, Science 2006]



See also: Why Does Unsupervised Pre-training Help Deep Learning? Dumitru Erhan, Yoshua Bengio ,Aaron Courville, Pierre-Antoine Manzagol PIERRE-Pascal Vincent, Sammy Bengio, JMLR 2010

Deep Boltzmann Machines



Shape Boltzmann Machine



"The Shape Boltzmann Machine: a Strong Model of Object Shape", Ali Eslami, Nicolas Heess and John Winn, CVPR 2012

Decoder-Only Models

- Examples:
 - Sparse coding
 - Deconvolutional Networks [Zeiler & Fergus, '10]
- No encoder to compute features

- So need to perform optimization
 - Can be relatively fast

Sparse Coding (Patch-based)

• Over-complete linear decomposition of input *y* using dictionary *D*

$$= 0.3 \times + 0.5 \times + 0.2 \times$$

$$C(y,D) = \underset{z}{\operatorname{argmin}} \ \frac{\lambda}{2} \|Dz - y\|_{2}^{2} + |z|_{1}$$



Dictionary D

- ℓ_1 regularization yields solutions with few non-zero elements
- Output is sparse vector: z = [0, 0.3, 0, ..., 0.5, ..., 0.2, ..., 0]

Deconvolutional Network Layer

 Convolutional form of sparse coding [Zeiler & Fergus, CVPR 2010]. Also Kavukcuoglu et al. NIPS 2010



Toy Example



Overall Architecture (2 layers)



Layer 2 Filters

• 50 filters/feature maps, showing max for each map projected down to image





Layer 3 filters

• 100 filters/feature maps, showing max for each map

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Layer 3 filters

• 100 filters/feature maps, showing max for each map

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Layer 3 filters

• 100 filters/feature maps, showing max for each map

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Results on Caltech 101

• Comparison to other methods using Lazebnik's SPM with hard vector quantization

Our model - layer 1	66.5%	
Chen <i>et al.</i> layer-1+2	$65.7\pm0.7\%$	
Kavukcuoglu <i>et al</i> .	$65.7\pm0.7\%$	Convolutional
Zeiler <i>et al.</i> layer-1+2	$66.9 \pm 1.1\%$	Sparse Coding
Boureau <i>et al.</i> (Hard)	$70.9\pm1.0\%$	
Jarrett <i>et al</i> .	$65.6 \pm 1.0\%$	Other approaches
Lazebnik <i>et al</i> .	$64.6\pm0.7\%$	using SPM with Hard quantization
Lee <i>et al.</i> layer-1+2	$65.4\pm0.5\%$	

Encoder-Only Models

- In vision setting, essentially a convnet trained without explicit class labels
- But still use feed-forward convnet to predict labels (of some kind)
- What kinds of labels?
 - Need to be "free", i.e. zero or minimal human effort required to obtain
 - Typically exploit some property of images/video
- Often called self-supervised learning
- Note: NOT generic approach -- only valid for image/video domain

Self-Supervised Learning

- Unsupervised feature learning by augmenting single images, Alexey Dosovitskiy, Jost Tobias Springenberg and Thomas Brox, NIPS 2014
- Colorful Image Colorization, Richard Zhang, Philip Isola, Alexei Efros, ECCV 2016
- Unsupervised Visual Representation Learning by Context Prediction, Carl Doersch, Abhinav Gupta, Alexei Efros, ICCV 2015
- Unsupervised Learning of Visual Representations using Videos, Xiaolong Wang, Abhinav Gupta, ICCV 2015

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Unsupervised Learning of Transformations

[Unsupervised feature learning by augmenting single images, Alexey Dosovitskiy, Jost Tobias Springenberg and Thomas Brox, NIPS 2014]

- Take patches from images
- For each patch, make lots of peturbed versions
- Treat each patch + perturbed copies as a separate classs
- Train supervised convnet
- Introducing prior knowledge about irrelevant transformations via perturbations



	STL-10	CIFAR-10-reduced	CIFAR-10	Caltech-101
K-means [6]	60.1 ± 1	70.7 ± 0.7	82.0	—
Multi-way local pooling [5]		—		77.3 ± 0.6
Slowness on videos [25]	61.0			74.6
Receptive field learning [16]		—	$[83.11]^1$	75.3 ± 0.7
Hierarchical Matching Pursuit (HMP) [3]	64.5 ± 1	—		
Multipath HMP [4]		—		82.5 ± 0.5
Sum-Product Networks [8]	62.3 ± 1	—	$[83.96]^1$	—
View-Invariant K-means [15]	63.7	72.6 ± 0.7	81.9	—
This paper	67.4 ± 0.6	69.3 ± 0.4	77.5	$76.6 \pm 0.7^{\ 2}$

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Input





Ground Truth





Output





Predicting Labels from Data



Predicting Data from Data



Cross-Channel Encoder



[1] Chen *et al.* In arXiv, 2016.[2] Yu and Koltun. In ICLR, 2016

Task Generalization: ILSVRC linear classification

conv1 conv2 conv3 conv4 conv5

lightness



Task Generalization: ILSVRC linear classification


Task Generalization: ILSVRC linear classification



Task Generalization: ILSVRC linear classification



Hidden Unit (conv5) Activations

sky



trees

water

Hidden Unit (conv5) Activations

faces



dog faces

flowers

Dataset & Task Generalization on PASCAL VOC

Does the feature representation *transfer* to other datasets and tasks?



Classification

Krähenbühl et al. In ICLR, 2016.

Detection Fast R-CNN. Girshick. In ICCV, 2015.

Segmentation FCNs. Long et al. In CVPR, 2015.

Dataset & Task Generalization on PASCAL VOC



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Scaling Self-Supervision

Learning Perception and Action without Human Supervision

Abhinav Gupta



context as supervision

[Collobert & Weston 2008; Mikolov et al. 2013]

house, where the professor lived without his wife and child; or so he said jokingly sometimes: "Here's where I live. My house." His daughter often added, without resentment, for the visitor's information, "It started out to be for me, but it's really his." And she might reach in to bring forth an inch-high table lamp with fluted shade, or a blue dish the size of her little fingernail, marked "Kitty" and half full of eternal neile but she was sure to replace these, after they had been admired, pretty near exactly where they had been. The little house was very orderly, and just big enough for all it contained, though to some tastes the bric-à-brac in the parlor might seem excessive. The dughter's preference was for the store-bought gimmicks and appliances, the toasters and carpet sweepers of Lilliput, but she knew that most adult visitors would

idea

Train a CNN to predict the patches in context











Semantics from a nonsemantic task





Relative Position Task





Avoiding Trivial Shortcuts





Include a gap

Jitter the patch locations



What is learned?



how do we evaluate?

■ Use as pre-trained network for VOC object detection.

Compare to ConvNet trained with ImageNet and ConvNet without Pre-training.

VOC 2007 Detection Performance



take-home summary

Surprising: Within image-context leads to across-image similarities.

Significantly better than no pre-training, but the performance is still below ImageNet pre-training.

Videos: Use tracking





Approach: Outline





PATCH MINING IN VIDEOS

- Track 8M patches in 100K videos from YouTube.
- Use tracking algorithms with no learning.



PATCH MINING IN VIDEOS





Sliding Window Searching





Query Tracked (First Frame) (Last Frame)

Some Examples







SE













LEARNING VIA VIDEOS

- Space of negatives is huge might take lot of time for network to learn
- Hard Negative Mining for Triplet
 Sampling
 - Random Selection (150K iterations)
 - Hard Negatives: Negative patches giving high loss
 - Backprop only for Hard Negatives
 - Hard Negative Mining for 200K iterations

What does the network learn?

trained using 8M tracks from 100K YouTube

Videos

Pool5 Neurons



Nearest Neighbor



Query

(a) Imagenet AlexNet

(b) Unsupervised AlexNet



Summary

- Unsupervised learning big unsolved problem in ML/AI
- Lots of active research
- Auto-encoder appealing idea but performance is underwhelming
- Self-supervised methods interesting, but not generic
- New approaches offer promise, e.g. generative adversarial nets and variational auto-encoders
 - Will be covered by Emily Denton on 12/15