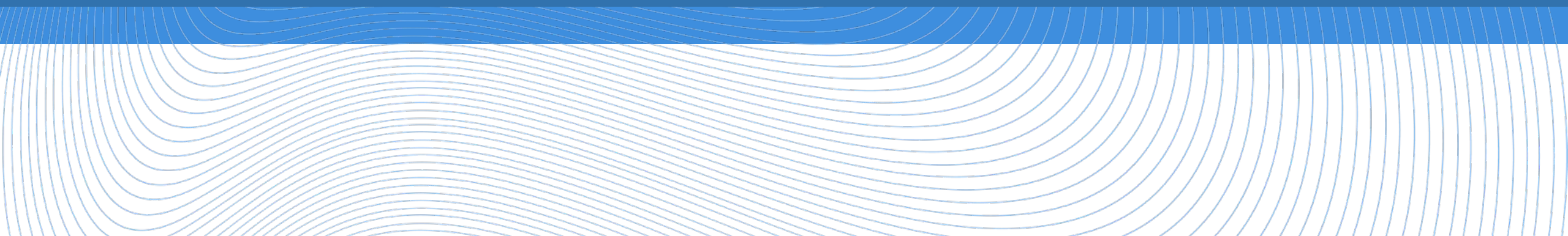


Metamorph: Synthesizing Large Objects from Dafny Specifications

Aleksandr Fedchin, Alexander Y. Bai, Jeffrey S. Foster



Key Challenge

- Testing in OOP context may require setting up complex objects that have private fields
- Challenge: generating programs (sequences of method calls) that produce objects with required properties
- Our idea: use method specifications in a verification-aware setting to guide the synthesis

Example Dafny API

Postconditions are assumed
after method calls

Preconditions must be
proved before method calls

```
datatype User = User(friends:set<nat>,  
                     requests:set<nat>)  
  
class SocialNetwork {  
  ghost var users: map<nat,User>  
  constructor() ensures users == map[] {...}  
  
  method AddUser(id:nat)  
    requires id ∉ users  
    ensures users == old(users)[id:=User({},{})]  
    {...}  
  
  method RemoveUser(id:nat) ...  
  method FriendRequest(from:nat, to:nat) ...  
  method RequestResponse  
    (from:nat, to:nat, answer:bool) ... }
```

Example Dafny API

Ghost fields are unavailable at runtime, cannot be set directly

```
datatype User = User(friends:set<nat>,
                      requests:set<nat>)

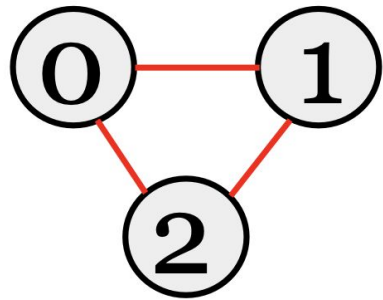
class SocialNetwork {
  ghost var users: map<nat, User>
  constructor() ensures users == map[] {...}

  method AddUser(id:nat)
    requires id ∉ users
    ensures users == old(users)[id:=User({}, {})]
    {...}

  method RemoveUser(id:nat) ...
  method FriendRequest(from:nat, to:nat) ...
  method RequestResponse
    (from:nat, to:nat, answer:bool) ... }
```

Method bodies hidden for modular verification, may not be implemented in Dafny

Example Synthesis Problem

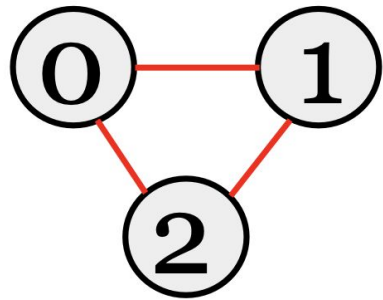


(describes a social network
with 3 users, all of whom
are friends)

```
method Goal()  
  returns (s:SocialNetwork)  
  ensures s.users.Keys == {0, 1, 2}  
         ^ 1 ∈ s.users[0].friends  
         ^ 1 ∈ s.users[2].friends  
         ^ 2 ∈ s.users[0].friends  
{
```

```
s := new SocialNetwork();  
s.AddUser(0); s.AddUser(1);  
s.FriendRequest(0, 1);  
s.RequestResponse(1, 0, true);  
s.AddUser(2);  
s.FriendRequest(0, 2);  
s.RequestResponse(2, 0, true);  
s.FriendRequest(1, 2);  
s.RequestResponse(2, 1, true); }
```

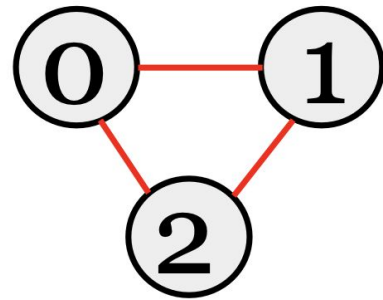
Example Synthesis Problem



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         ^ 1 ∈ s.users[0].friends  
         ^ 1 ∈ s.users[2].friends  
         ^ 2 ∈ s.users[0].friends  
{  
  s := new SocialNetwork();  
  s.AddUser(0); s.AddUser(1);  
  s.FriendRequest(0, 1);  
  s.RequestResponse(1, 0, true);  
  s.AddUser(2);  
  s.FriendRequest(0, 2);  
  s.RequestResponse(2, 0, true);  
  s.FriendRequest(1, 2);  
  s.RequestResponse(2, 1, true); }  
}
```

Example Synthesis Problem



(describes a social network with 3 users, all of whom are friends)

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method Goal()  
  returns (s:SocialNetwork)  
  ensures s.users.Keys == {0, 1, 2}  
    ∧ 1 ∈ s.users[0].friends  
    ∧ 1 ∈ s.users[2].friends  
    ∧ 2 ∈ s.users[0].friends  
{  
  s := new SocialNetwork();  
  s.AddUser(■); s.AddUser(■);  
  s.FriendRequest(■);  
  s.RequestResponse(■);  
  s.AddUser(■);  
  s.FriendRequest(■);  
  s.RequestResponse(■);  
  s.FriendRequest(■);  
  s.RequestResponse(■); }  
}
```

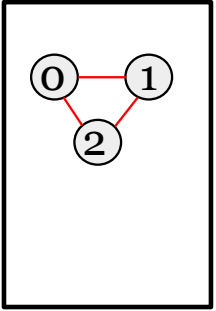
Problem:
Inferring all
primitive
arguments at
once may take
minutes even if
the method
sequence is
already known

Key Ideas

- Perform goal-directed backward synthesis
(goal = an object state = conjunction of constraints)
- Reconstruct method arguments and prior objects states from verifier counterexamples
- Guide synthesis to minimize the number of unsatisfied constraints

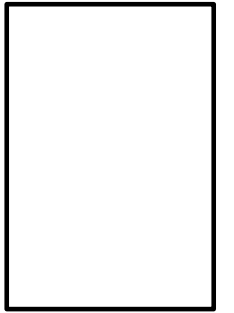
Example

Target State



(3 users,
all of
whom are
friends)

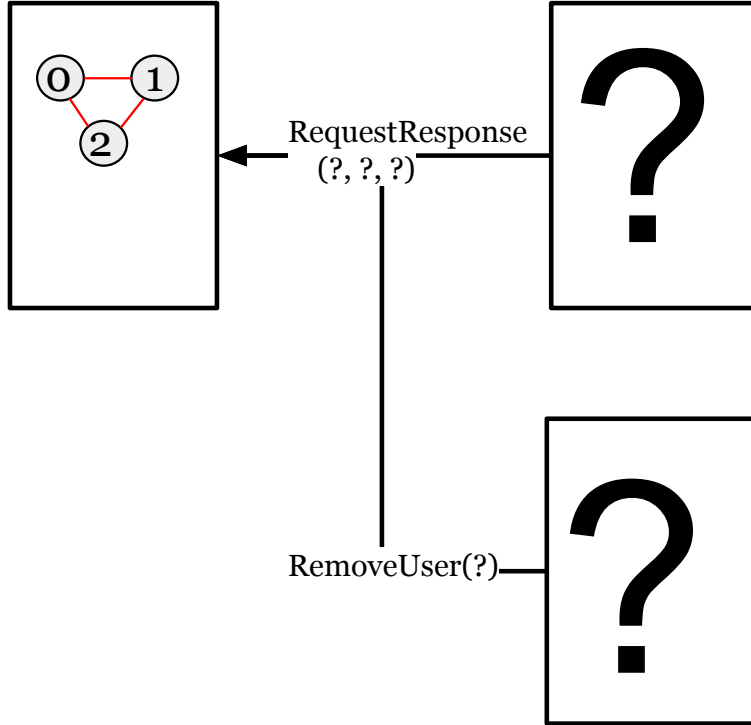
Initial State



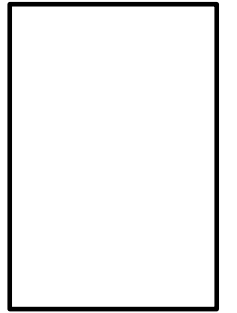
(empty
social
network)

Example

Target State



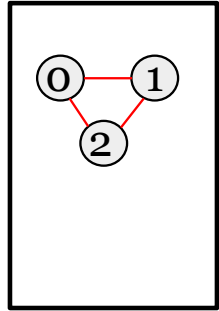
Initial State



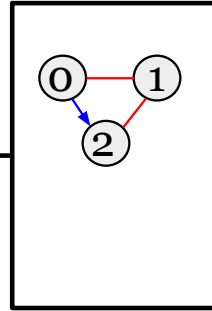
Asking the verifier to infer the
method arguments and
preceding states

Example

Target State

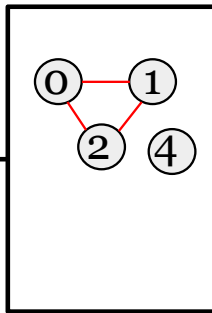


S₁



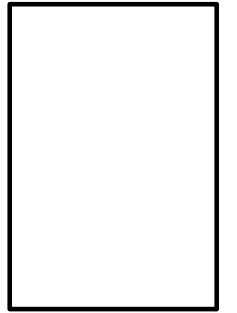
RequestResponse
(2, 0, true)

S₂



RemoveUser(4)

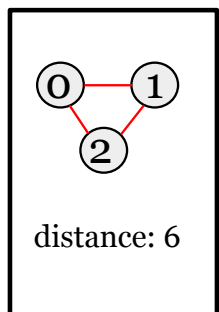
Initial State



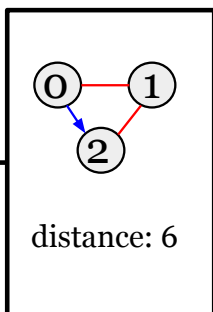
Which of the two states to
explore first?

Example: Piecewise Distance Metric

Target State

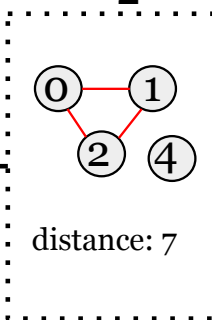


S_1



RequestResponse
(2, 0, true)

S_2



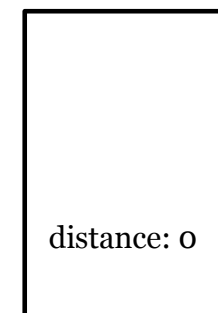
RemoveUser(4)

to add 3 users,
to add 2 connections,
to add 1 request,
TOTAL

≥ 3 calls to AddUser*
 ≥ 2 calls to RequestResponse
 ≥ 1 call to FriendRequest
 $\geq \underline{6 \text{ calls}}$

Better!

Initial State



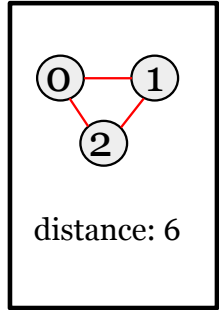
to add 4 users,
to add 3 connections,
TOTAL

≥ 4 calls to AddUser
 ≥ 3 calls to RequestResponse
 $\geq \underline{7 \text{ calls}}$

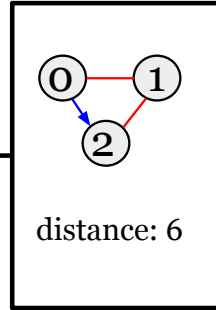
*Because Dafny verifier proves that a single call to AddUser adds at most one user and that no other method can add users.

Example

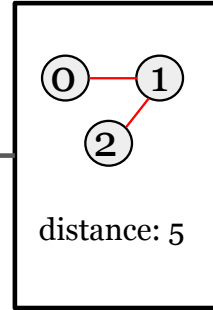
Target State



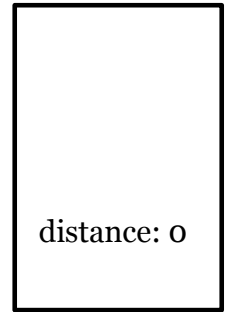
S_1



S_3



Initial State



RequestResponse
(2, 0, true)

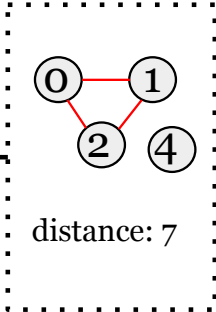
FriendRequest
(0, 2)

RequestResponse
(2, 1, true)

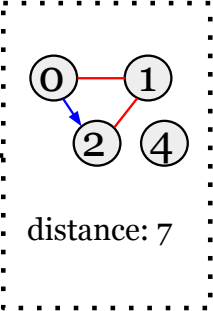
RemoveUser(4)

RemoveUser(4)

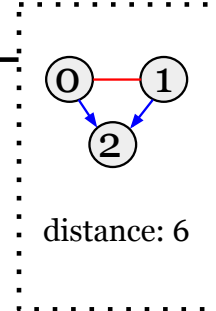
S_2



S_6

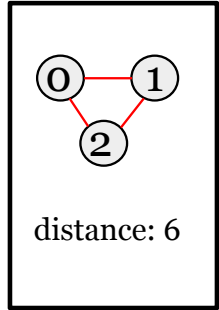


S_5

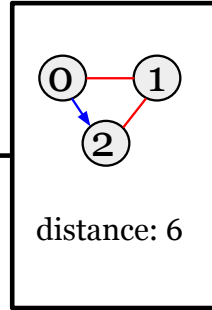


Example

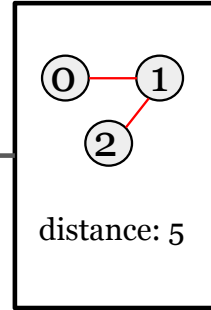
Target State



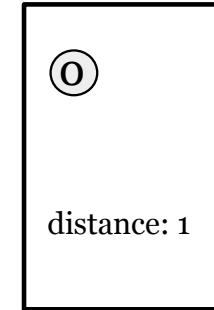
S_1



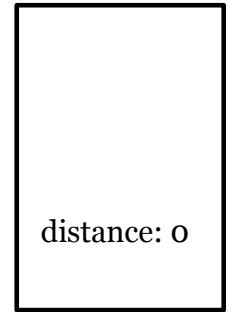
S_3



S_7



Initial State



RequestResponse
(2, 0, true)

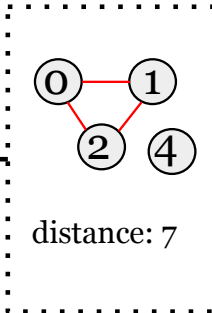
FriendRequest
(0, 2)

RequestResponse
(2, 1, true)

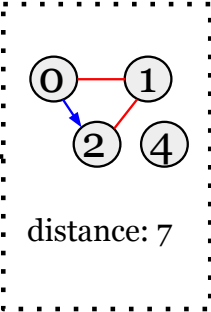
RemoveUser(4)

RemoveUser(4)

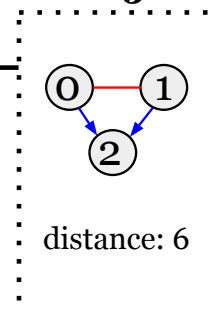
S_2



S_6

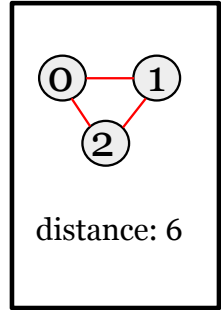


S_5

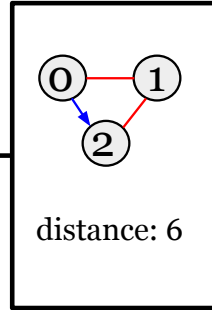


Example

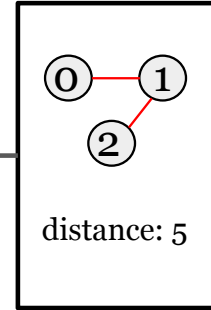
Target State



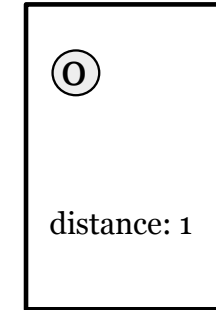
S₁



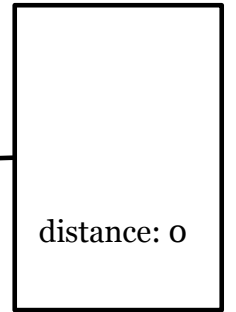
S₃



S₇



Initial State



RequestResponse
(2, 0, true)

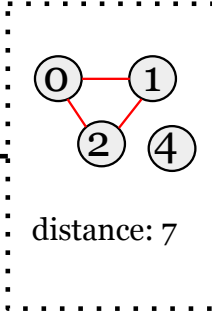
FriendRequest
(0, 2)

RequestResponse
(2, 1, true)

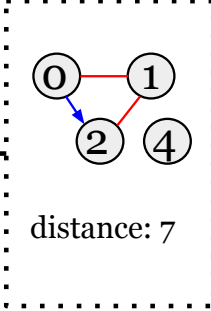
RemoveUser(4)

RemoveUser(4)

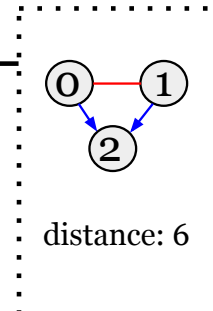
S₂



S₆



S₅



Evaluation

We evaluate Metamorph on 8 APIs:

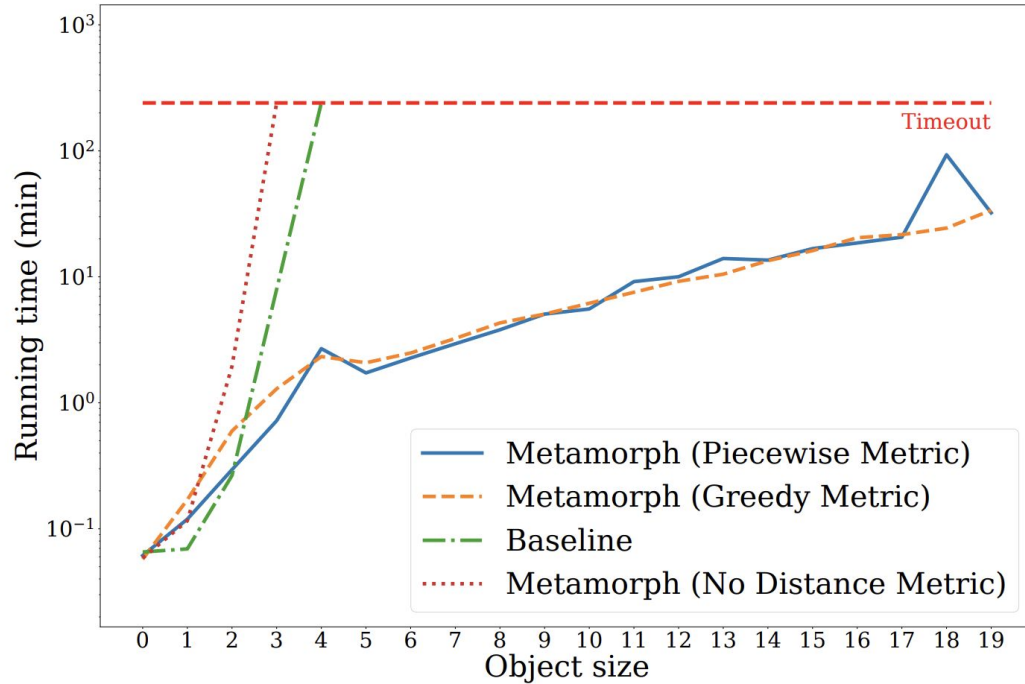
- Binary Tree
- Freezable Array*
- Doubly Linked List
- Queue
- Firewall* (graph-like API)
- Social Network
- Simple Virtual Machine
- HKDF* (from AWS ESDK)

*adapted from prior studies

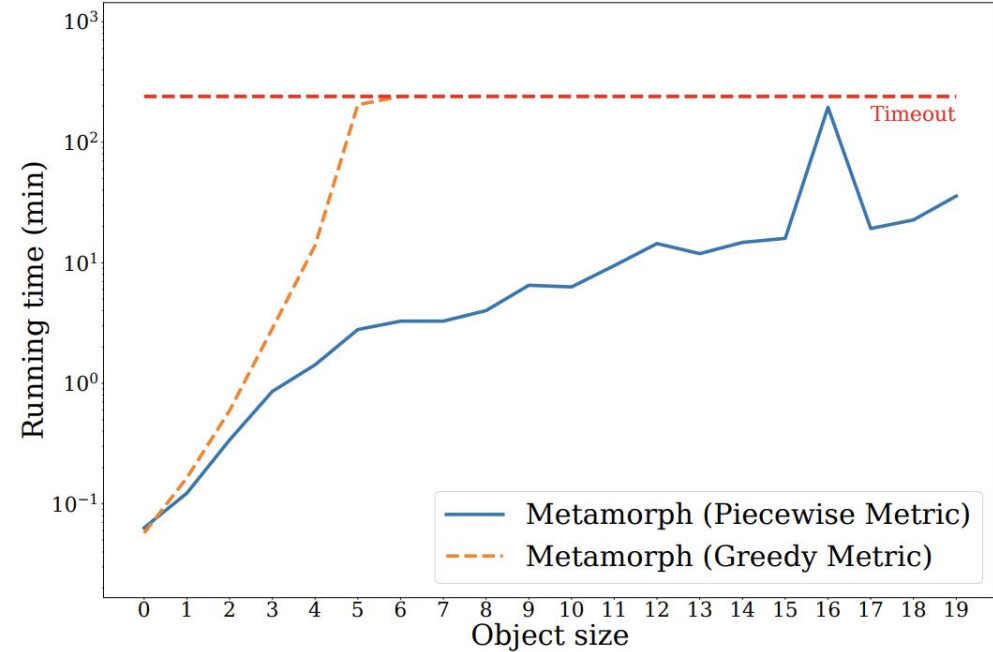
We compare the synthesis time of several approaches on increasingly larger objects:

1. Baseline - asking Dafny verifier to prove that no program generates the desired object, reconstruct the result from the counterexample.
2. Metamorph (No Distance Metric)
3. Metamorph (Piecewise Distance Metric)
4. Metamorph (Greedy Distance Metric, counts number of constraints that change)

Evaluation: Social Network Benchmark



(a) Social Network.



(b) Social Network with Relaxed Object Invariant.

Summary

- We use counterexamples to reason about effects of method calls
- We propose 2 distance metrics to guide the search over object states
- We evaluate Metamorph on 8 APIs
- Metamorph can synthesize programs up to 57 method calls
- We found that Metamorph performs better when a distance metric is used, piecewise distance metric is better than the greedy metric in select cases (e.g., incomplete API specification)
- We prototyped an integration of Metamorph with Dafny Testing Toolkit

Backup Slides

Relaxed Object Invariant

```
datatype User = User(friends:set<nat>,  
                    requests:set<nat>)  
class SocialNetwork {  
  ...  
  predicate IsValid() reads this {  
    && (forall u1, u2 ::  
      // removed "u2 in users" condition  
      (u1 in users && u2 in users[u1].requests) ==> (u1 != u2))  
    ...  
  }  
}
```

Guiding the Search: Distance Metrics

