

Our original time series : $Ts = \langle 1,2,3,1,2,3 \rangle$

We use a basic window size 2 and a sliding windows size 6

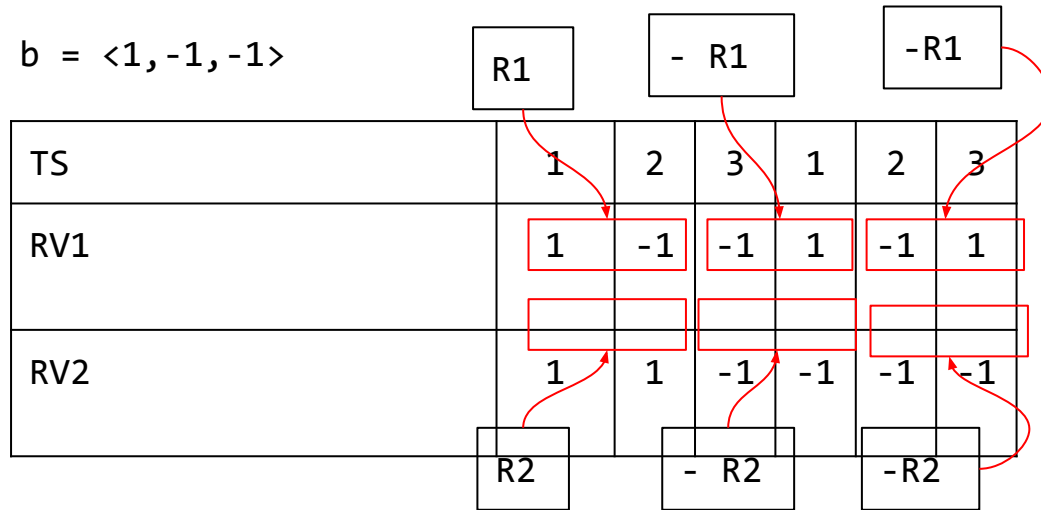
We build 2 basic random vectors of size 2 :

$$R1 = \langle 1, -1 \rangle, R2 = \langle 1, 1 \rangle$$

We build 2 random vectors RV1 and RV2 of size 6 using basic random vectors R1 or -R1 (to build RV1) and R2 or -R2 (to build RV2) . This choice is determined by a random vector b:

if $b_i = 1$ we use R1 and if $b_i = -1$ we use -R1.

We set $b = \langle 1, -1, -1 \rangle$



We obtain the following

Sketch $TS^*(RV1, RV2)$:

$$\langle (-1+2+1), (3+-4+-5) \rangle$$


$$\langle -2, -6 \rangle$$

We add two incoming values : $\langle 3, 2 \rangle$

We remove the two first values in the series : $\langle 1, 2 \rangle$

And The series becomes : $\langle 3, 1, 2, 3, 3, 2 \rangle$

time series	1	2	3	1	2	3	3	2
RV1			1	-1	-1	1	-1	1
RV2			1	1	-1	-1	-1	-1

 New values in the time series

We update the current sketch by deleting the first dot product of the two outdated values


Current sketch : $\langle (-\cancel{1} - 2 + 1), (3 - \cancel{4} - 5) \rangle$

We add two incoming values : $\langle 3, 2 \rangle$

We remove the two first values in the series : $\langle 1, 2 \rangle$

And The series becomes : $\langle 3, 1, 2, 3, 3, 2 \rangle$

time series	1	2	3	1	2	3	3	2
RV1			1	-1	-1	1	-1	1
RV2			1	1	-1	-1	-1	-1

 New values in the time series

We update the current sketch by deleting the first dot product of the two outdated values

Current sketch : $\langle (-1 + -2 + 1), (3 + -4 + -5) \rangle$

Then, the values are shifted and multiplied by 1 or -1 according to "b". Here "-2" becomes "2" because it moves from a position having value -1 to a position having value 1 in "b".

New sketch : $\langle (2 + 1 + ?), (4 + -5 + ?) \rangle$


Reminder b = $\langle 1, -1, -1 \rangle$

We add two incoming values : $\langle 3, 2 \rangle$

We remove the two first values in the series : $\langle 1, 2 \rangle$

And The series becomes : $\langle 3, 1, 2, 3, 3, 2 \rangle$

time series	1	2	3	1	2	3	3	2
RV1			1	-1	-1	1	-1	1
RV2			1	1	-1	-1	-1	-1

 New values in the time series

We update the current sketch by deleting the first dot product of the two outdated values

Current sketch : $\langle (-1+2+1), (3+4+5) \rangle$


And we add the values of the dot product restricted to the two incoming values.

New sketch : $\langle (2+1+1), (4+5+5) \rangle$
 $\langle 2, -6 \rangle$

And again, we add two incoming values : $\langle 1, 3 \rangle$

We remove two values in the series : $\langle 3, 1 \rangle$ The series becomes : $\langle 2, 3, 3, 2, 1, 3 \rangle$

time series	3	1	2	3	3	2	3	1
RV1			1	-1	-1	1	-1	1
RV2			1	1	-1	-1	-1	-1

 New values in the time series

We update the current sketch by deleting the dot product of the two outdated values

Current sketch : $\langle \cancel{2+1+-1}, \cancel{4+-5+-5} \rangle$

And we add the values of the dot product restricted to the two incoming values.

New sketch : $\langle (-1+-1+-2), (5+-5+-4) \rangle$
 $\langle -4, -4 \rangle$

We repeat the same process every timesteps...