# Programming Languages 

Prolog<br>CSCI-GA.2110-001<br>Summer 2011

## Prolog overview

- Stands for Programming in Logic.
- Invented in approximately 1972.
- Belongs to the logical and declarative paradigms.
- Based on first order predicate calculus.
- Used for artificial intelligence, theorem proving, expert systems, and natural language processing.
- Used as a standalone language or complements traditional languages.
- Radically different than most other languages.
- Each program consists of 2 components:
- database (program): contains facts and rules
- query : ask questions about relations


## Stating Facts

Two ways to state facts:

```
?- [user].
sunny.
```


## consult user <br> state the fact

\% user://1 compiled $0.00 \mathrm{sec}, 408$ bytes true.
(same as ?- consult(user).)
Or:
?- assert(sunny). state the fact true.

## Stating Facts 2

## What facts can we describe?

1. Items ?- assert(sunny).
2. Relationships between items:
?- assert(likes(john,mary)).

Query the database:
?- likes(john,mary).
true.
?- likes(mary,john).
false.
?- likes(john,sue).
false.

## Relations

- Relations take an arbitrary number of parameters.
- Arguments can be legal Prolog terms : integer, atom, variable, structure.
- Atoms: letters, digits, underscore with lowercase characters, or anything in quotes.
- Legal: hello, hi123, two_words, "G_1)!\#)@blah"
- Illegal: Hello, 123hi, _hello, two-words
- Variables: Any word beginning with a capital letter.
- Structures: Functors with a list of arguments.

Note: variables bind to values, not memory locations.
?- likes(john,Who).
Who = mary
Prolog will display one instantiation. Type a semicolon for more.

## More Relations

All satisfying likes relations:
?- likes(Who1,Who2).
Who1 = john; Who2 = mary
Constrain queries using variables:
?- likes(Who,Who).
false.
(People who like themselves.)
Use wild card to determine if some instantiation exists:
?- likes(john,_).
true.
(That is, john likes someone-we don't care who.)
Wild cards can be used in conjunction with variables:
?- likes(Who,_).
Who = john

```
Rules express conditional statements about our world.
Consider the assertion: "All men are mortal."
Expressible as modus ponens: human }->\mathrm{ mortal.
mortal is a goal (or head), and human is a subgoal (or body).
?- assert(mortal(X) :- human(X)).
true.
?- assert(human(socrates)).
true.
Now we query:
?- mortal(socrates).
true.
You can also ask who is mortal:
?- mortal(X).
\(X=\) socrates
```


## Conjunction and Disjunction

Conjunction is expressed using commas:
?- fun(X) :- red(X), car(X).
Disjunction is expressed with semicolons or separate clauses:
?- $f u n(X)$ :- $\operatorname{red}(X) ; \quad \operatorname{car}(X)$.
... is the same as

```
?- fun(X) :- red(X).
?- fun(X) :- car(X). Order of rules matters!
```

Consider:

```
?- assert(car(jeep)). assert(car(ford)). assert(red(jeep)).
```

?- fun(jeep).
true.
?- fun(ford).
false.

## Multi-Variable Rules

daughter (X,Y) :- mother (Y, X), female(X).
grandfather (X,Y) :- male(X), parent(X,Z), parent(Z,Y).
Quantification:
■ Variables appearing in the goal are universally quantified.
■ Variables appearing only in the subgoal are existentially quantified.

The grandfather goal reads as:
$\forall_{\mathrm{X}, \mathrm{Y}} \exists_{\mathrm{Z}}$ : grandfather $(\mathrm{X}, \mathrm{Y}) \Leftarrow \operatorname{male}(\mathrm{X})$, parent $(\mathrm{X}, \mathrm{Z})$, parent $(\mathrm{Z}, \mathrm{Y})$.

## Resolution Principle

Prolog responds to queries using the resolution principle:
If $C_{1}$ and $C_{2}$ are rules and the head of $C_{1}$ matches one of the terms in the body of $C_{2}$, then replace the term in $C_{2}$ with the body of $C_{1}$.

## Example:

$C_{1}$ : happy (X) :- workday (Z), day_off(X,Z).
$C_{2}$ : go_walking(X) :- happy (X).

1. Query: ?- go_walking(emily).
2. Instantiate the rule: go_walking(emily) :- happy (emily).
3. Apply resolution principle: go_walking(emily) :- workday(Z), day_off(emily,Z).

## Unification

Consider again:
$C_{1}$ : happy (X) :- workday (Z), day_off(X,Z).
$C_{2}$ : go_walking(X) :- happy (X).
When the user queries ?- go_walking(emily), How does Prolog make the connection? go_walking(emily) go_walking(X)

Answer: unification.

## Unification Algorithm

1. Constants: Any constant unifies with itself.
2. Structures: Same functor, same arity, arguments unify recursively.
3. Variables: Unify with anything.
(a) Value: variable takes on the value.
(b) Another Variable: unify by reference.

Some examples:

| 21 | 21 | 21 |
| :---: | :---: | :---: |
| X | 5 | $\mathrm{X}=5$ |
| love (X,me) | love (you, Y) | $\mathrm{X}=\mathrm{you}, \mathrm{Y}=\mathrm{me}$ |
| love (X,Y) | love (you, Y) | $X=$ you, $Y=Y$ |
| 8 | 15 | error |
| love (X,Y) | foobar (you, Y) | error |
| $c(X, c(Y, c(Z, n))$ ) | $c(h e, c(s h e, ~ c(i t, n)))$ | $\mathrm{X}=$ he, $\mathrm{Y}=$ she, $\mathrm{Z}=$ it |
| love (X,Y) | love (you,f(Y)) | $\mathrm{X}=\mathrm{you}, \mathrm{Y}=$ ? ? |

## Occurs Check

Consider:
equal(Y, f(Y)).
Let's try unifying $\mathrm{Y}=\mathrm{f}(\mathrm{Y})$. We have:

```
equal(Y, f(Y)) no match
equal(f(Y), f(f(Y))) no match
equal(f(f(Y)), f(f(f(Y)))) no match
equal(f(f(f(Y))), f(f(f(f(Y))))) no match
Infinite recursion!
```

This situation can be caught with an occurs check.

## More on Occurs Check

An occurs check causes unification to fail if variable is contained within a structure.

- Prevents infinite loops or unsoundness.
- Inefficient to implement (linear in the size of the largest term).
- Most implementations of Prolog (like SWI Prolog) omit it.

Therefore, in SWI Prolog:
?- equal(Y, f(Y)).
$Y=f(Y)$.
If you insist on the occurs check, you can force it in SWI:
?- unify_with_occurs_check(X,f(X)).
false.

## Execution Order

There are two ways to answer a query:

1. Forward chaining: start with existing clauses and work forward.
2. Backward chaining: start with goal and work backward. (Used by Prolog).

If the body of a rule unifies with the heads of other rules in some particular order, it can be expressed as a tree.

## Execution Order

```
Consider:
rainy(seattle).
rainy(rochester).
cold(seattle).
snowy(X) :- rainy(X), cold(X).
?- snowy(X).
```



## Reflexive Transitive Closure

```
More than one "application" of a rule:
?- connect(Node,Node).
?- connect(N1,N2) :- edge(N1,Link), connect(Link,N2).
Now add some edges:
    ?- assert(edge(a,b)). ?- assert(edge(c,d)).
    ?- assert(edge(a,c)). ?- assert(edge(d,e)).
    ?- assert(edge(b,d)). ?- assert(edge(f,g)).
?- connect(a,e).
true.
```

```
connect(a,e) :- edge(a,b), connect(b,e)
```

connect(a,e) :- edge(a,b), connect(b,e)
connect(b,e) :- edge(b,d), connect(d,e)
connect(b,e) :- edge(b,d), connect(d,e)
connect(d,e) :- edge(d,e), connect(e,e)

```
connect(d,e) :- edge(d,e), connect(e,e)
```

?- connect(d,f).
false.

## Backtracking

- Prolog maintains a list of goals to be satisfied.
- When a goal is queried, all subgoals of the goal are added to the list.
- goal(X,Y) :- subgoal1(X), subgoal2(Y).
- Prolog will try to satisfy all subgoals.
- If a subgoal cannot be satisfied, Prolog will try another way.
- subgoal1(X) :- subsubgoal1(X).
- subgoal1(X) :- subsubgoal2(X), subsubgoal3(X).

■ This is called backtracking.

- Carried out through a tree data structure:
- Goal is a node.
- Subgoals are children of the node.


## Backtracking Example

```
Consider:
rainy(seattle).
rainy(rochester).
cold(rochester).
snowy(X) :- rainy(X), cold(X).
?- snowy(X).
```



## Backtracking in Prolog

```
?- rainy(seattle). ?- rainy(rochester).
?- cold(rochester). ?- snowy(X) :- rainy(X), cold(X).
```

Print the backtrace by invoking trace., then snowy (X).

```
Call: (6) snowy(_G466) ? creep
Call: (7) rainy(_G466) ? creep
Exit: (7) rainy(seattle) ? creep
Call: (7) cold(seattle) ? creep
Fail: (7) cold(seattle) ? creep
Redo: (7) rainy(_G466) ? creep
Exit: (7) rainy(rochester) ? creep
Call: (7) cold(rochester) ? creep
Exit: (7) cold(rochester) ? creep
Exit: (6) snowy(rochester) ? creep
X = rochester
```


## Lists

Lists are denoted by [ a , b, c ].
A cons pair is denoted [ $\mathrm{X} \mid \mathrm{Y}$ ] where X is the head and Y is the tail.
Rules for testing list membership:
?- assert(member(X, [X|Xs])).
?- assert(member(X, [Y|Ys]) :- member(X,Ys)).
Testing membership:
?- member (b, $[a, b, c]$ ).
true.
?- member (b, $[a, c])$.
false.
You can also extract list membership:
?- member (X, $[\mathrm{a}, \mathrm{b}, \mathrm{c}]$ ).
$X=a ; X=b ; X=c$.

Consider a list reverse rule:
reverse([], []).
reverse([X|Xs],Zs) :- reverse(Xs,Ys), append(Ys,[X],Zs).
Reverse-accumulate:
reverse(Xs,Ys) :- reverse(Xs, [],Ys).
reverse([X|Xs],Acc,Ys) :- reverse(Xs, [X|Acc],Ys).
reverse([],Ys,Ys).
Invoking the reverse rule:
?- reverse([a,b,c], X).
$X=[c, b, a]$.
?- reverse([a,b,c], [a, c,b]).
false.

## Tree for Reverse

The reverse rule at work:


## Cut Operator

You can tell Prolog to stop backtracking using the cut operator, !.

- Used to "commit" all unifications up to the point of the !
- Will never backtrack through any subgoal to the left of !
- Done to optimize performance.
- Generally requires intuition about the program.


## Consider:

prime_candidate(X) :- member(X, candidates), prime(X).

- Variable $X$ may appear several times in candidates.
- Once $X$ is found to be in candidates, no need to try other possibilities.
- Solution: use the cut operator.
- member (X, [X|_]) :- !.
- member $\left(\mathrm{X},\left[\_\mid \mathrm{T}\right]\right)$ :- member $(\mathrm{X}, \mathrm{T})$.


## More on Cut

The cut operator can also serve as an if-then-else construct: statement :- condition, !, then_part. statement :- else_part.

- Cut prevents the condition from being retested.
- If condition is true, subgoal then_part will be attempted.
- If then_part fails, the system will not backtrack into the condition.
- If first goal fails, the second goal will be tried.

One way to negate a subgoal is using predicate not: unmarried_student(X) :- not(married(X)), student(X).

Definition of not (also known as $\backslash+$ ): not(Goal) :- call(Goal), !, fail. not(Goal).

- Predicate fail unconditionally fails.
- Predicate call treats the input term as a goal and attempts to satisfy it.

Example:
single(Person) :- \+ married(Person,_), \+ married(_, Person).
Note: \+ indicates inability to prove-not falsehood.

