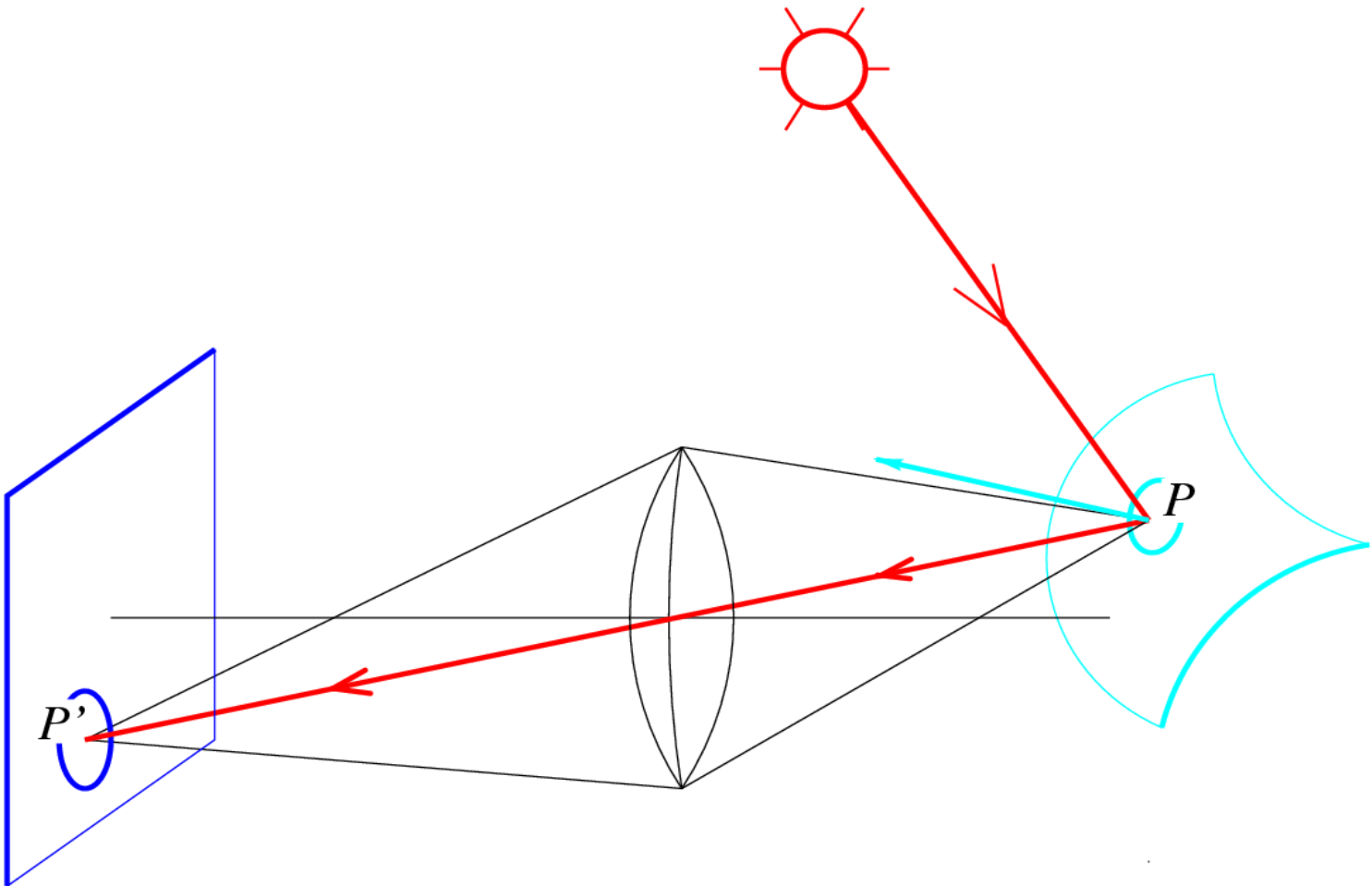


Lecture 4:

Light & Color

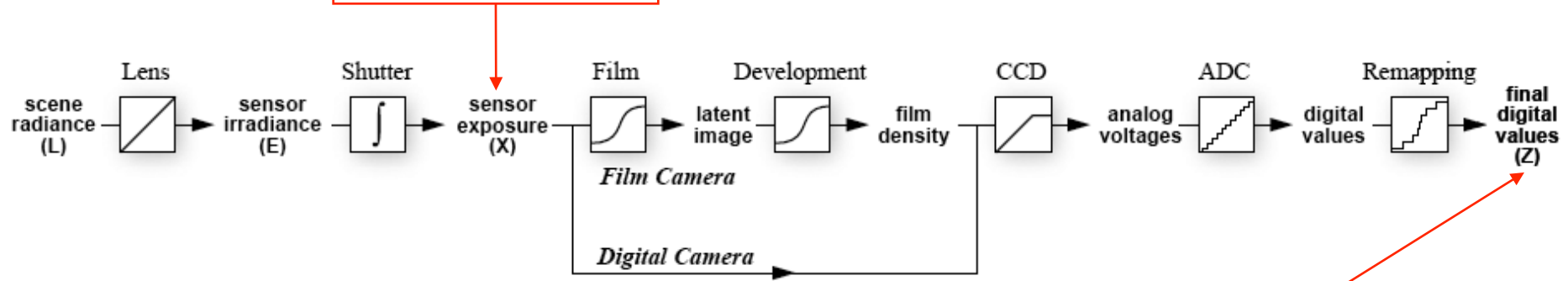
Prof. Rob Fergus

Image formation



From light rays to pixel values

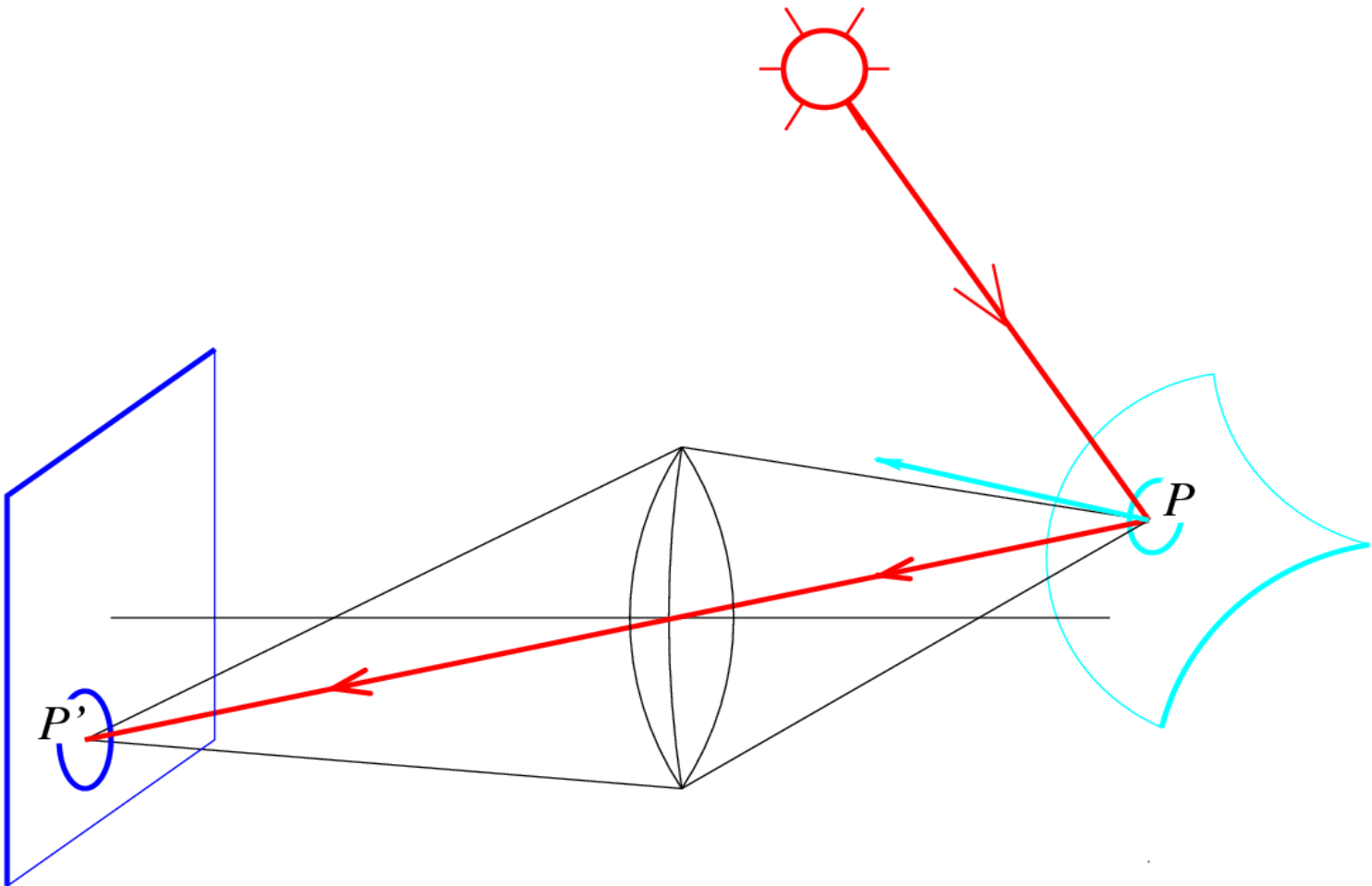
$$X = E \cdot \Delta t$$



$$Z = f(E \cdot \Delta t)$$

- Camera response function: the mapping f from irradiance to pixel values
 - Useful if we want to estimate material properties
 - Enables us to create high dynamic range images

Image formation

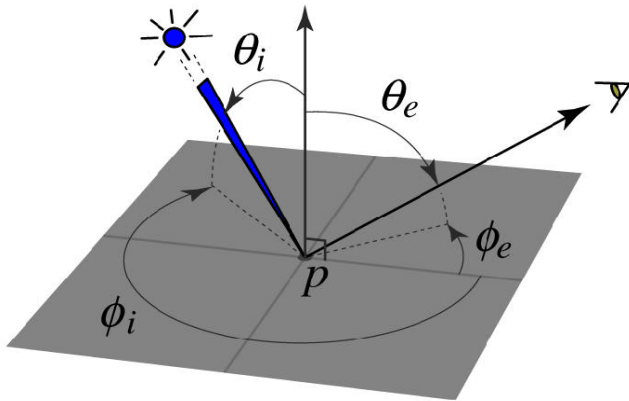


The interaction of light and surfaces

- What happens when a light ray hits a point on an object?
 - Some of the light gets **absorbed**
 - converted to other forms of energy (e.g., heat)
 - Some gets **transmitted** through the object
 - possibly bent, through “refraction”
 - Or scattered inside the object (subsurface scattering)
 - Some gets **reflected**
 - possibly in multiple directions at once
 - Really complicated things can happen
 - fluorescence
- Let’s consider the case of reflection in detail
 - Light coming from a single direction could be reflected in all directions.
How can we describe the amount of light reflected in each direction?

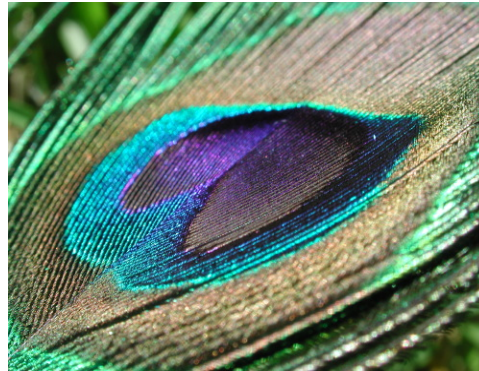
Bidirectional reflectance distribution function (BRDF)

- Model of local reflection that tells how bright a surface appears when viewed from one direction when light falls on it from another
- Definition: ratio of the **radiance** **L** in the **emitted** direction to **irradiance** **E** in the **incident** direction

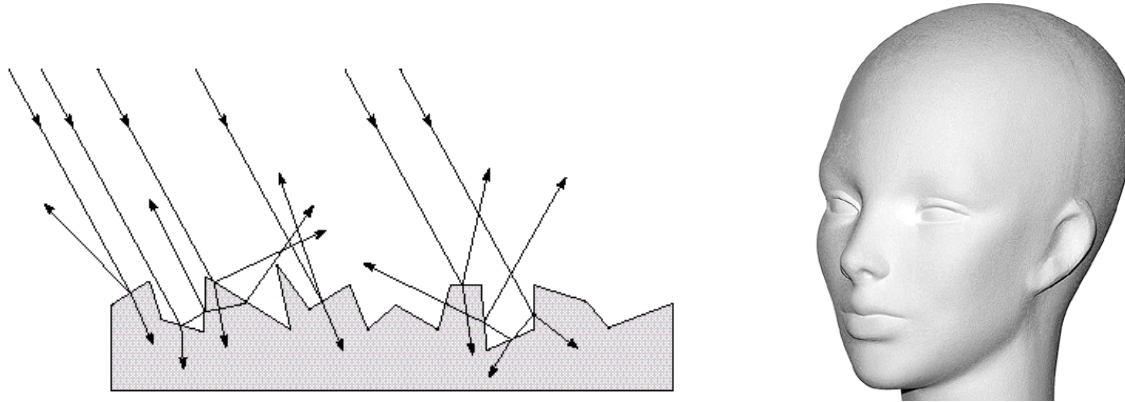


$$\rho(\theta_i, \phi_i, \theta_e, \phi_e) = \frac{L_e(\theta_e, \phi_e)}{E_i(\theta_i, \phi_i)} = \frac{L_e(\theta_e, \phi_e)}{L_i(\theta_i, \phi_i) \cos \theta_i d\omega}$$

BRDFs can be incredibly complicated...



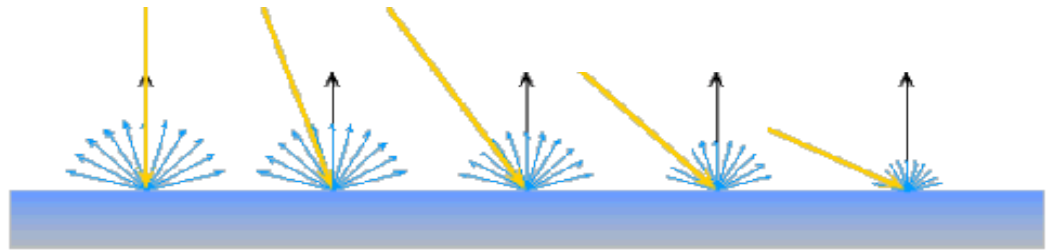
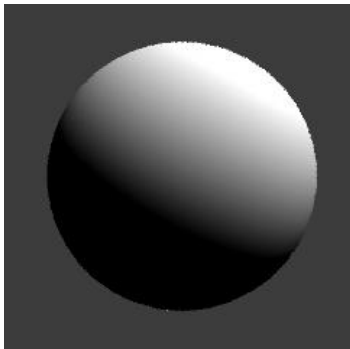
Diffuse reflection



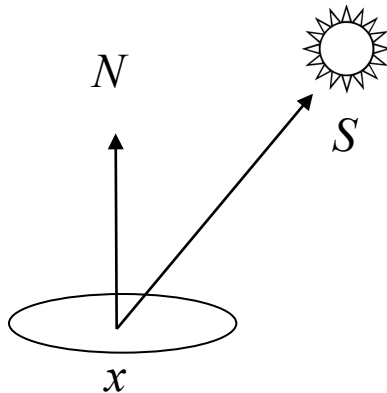
- Light is reflected equally in all directions
 - Dull, matte surfaces like chalk or latex paint
 - Microfacets scatter incoming light randomly
- **BRDF is constant**
 - *Albedo*: fraction of incident irradiance reflected by the surface

Diffuse reflection: Lambert's law

- Viewed brightness does not depend on viewing direction, but it *does* depend on direction of illumination



$$B(x) = \rho(x)(N(x) \cdot S(x))$$



B : radiosity

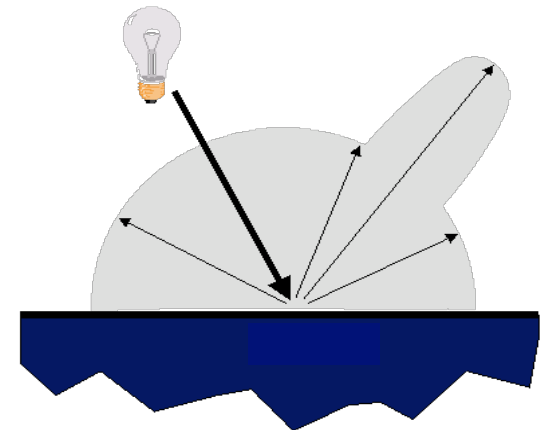
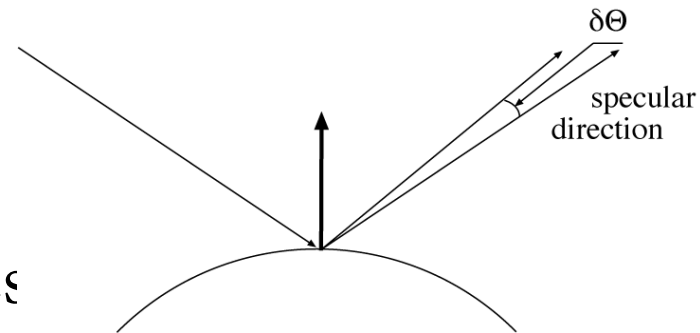
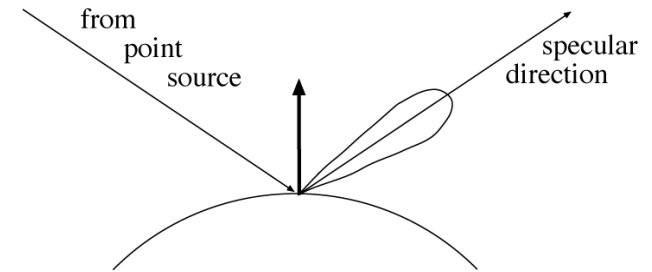
ρ : albedo

N : unit normal

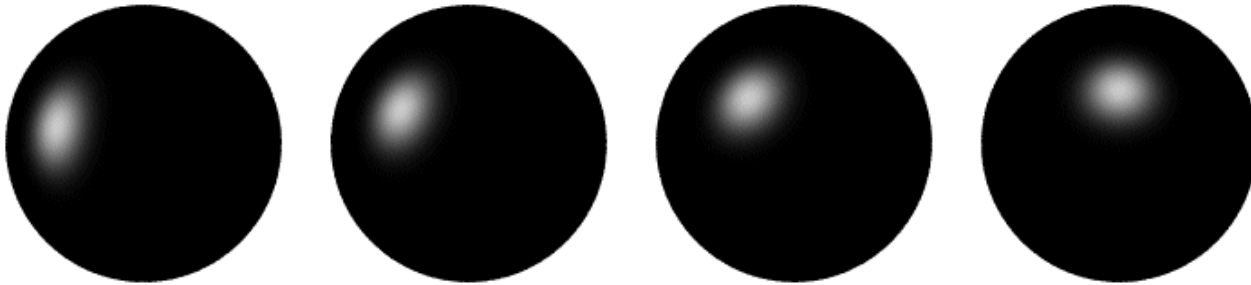
S : source vector (magnitude proportional to intensity of the source)

Specular reflection

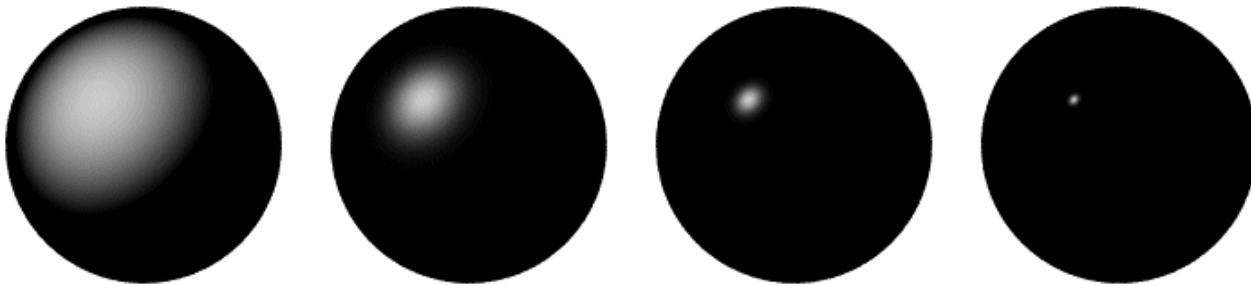
- Radiation arriving along a source direction leaves along the specular direction (source direction reflected about normal)
- Some fraction is absorbed, some reflected
- On real surfaces, energy usually goes into a lobe of directions
- Phong model: reflected energy falls off with $\cos^n(\delta\theta)$
- Lambertian + specular model: sum of diffuse and specular term



Specular reflection



Moving the light source



Changing the exponent

Color

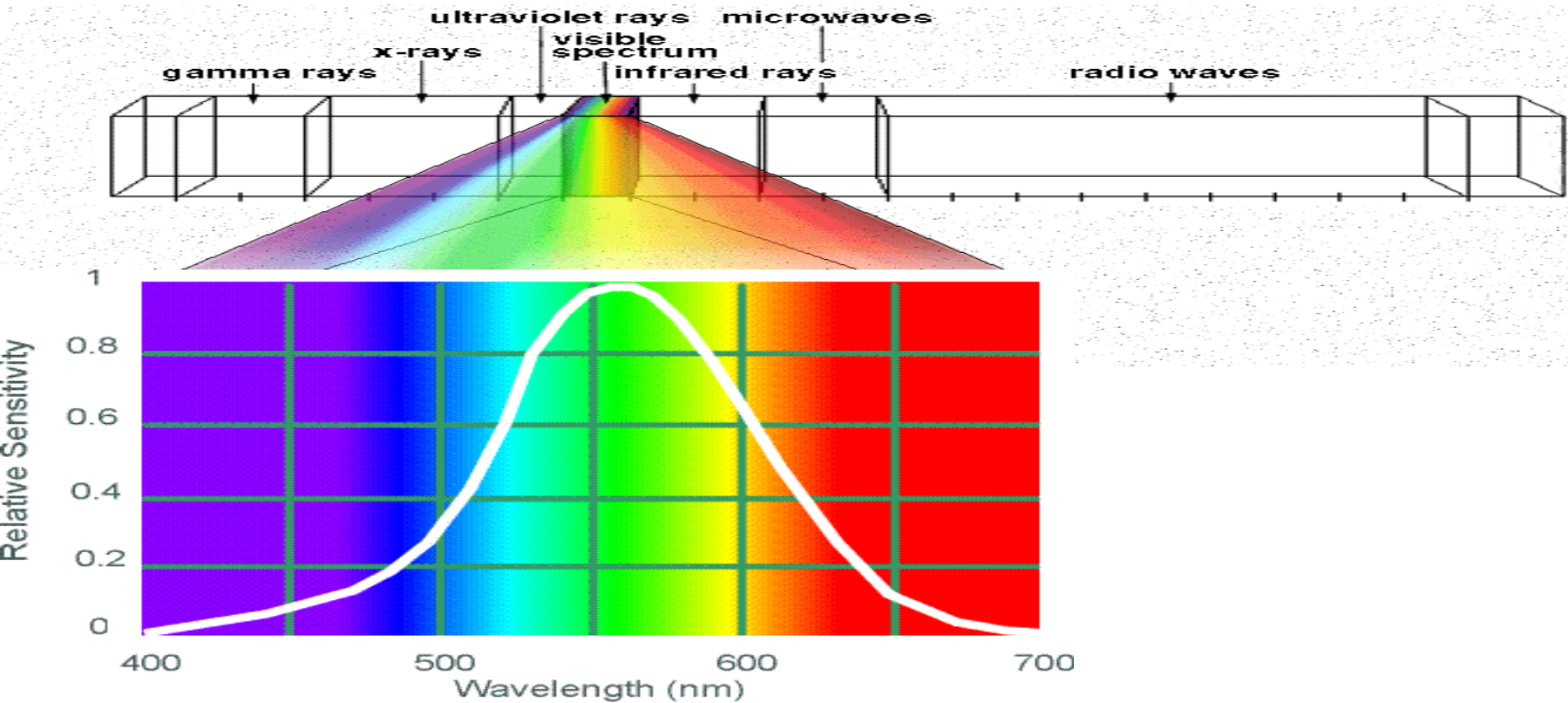
What is color?

- Color is a psychological property of our visual experiences when we look at objects and lights,
not a physical property of those objects or lights
(S. Palmer, *Vision Science: Photons to Phenomenology*)
- Color is the result of interaction between physical light in the environment and our visual system

Overview of Color

- Physics of color
- Human encoding of color
- Color spaces
- White balancing

Electromagnetic Spectrum

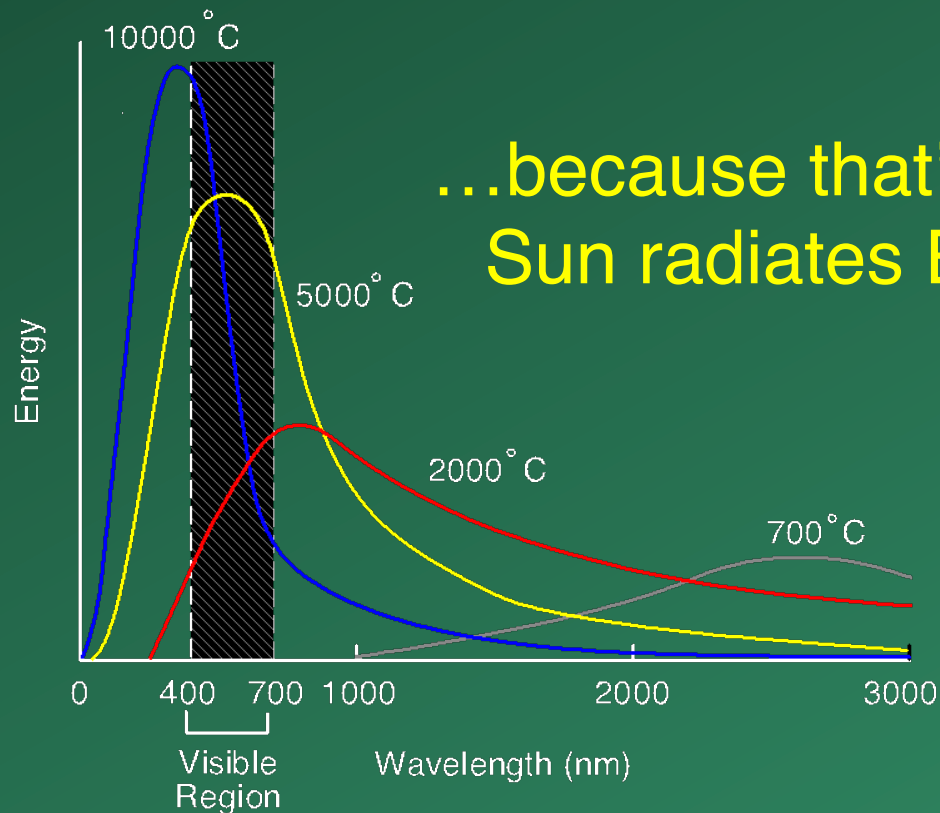


Human Luminance Sensitivity Function

Visible Light

Plank's law for Blackbody radiation
Surface of the sun: $\sim 5800\text{K}$

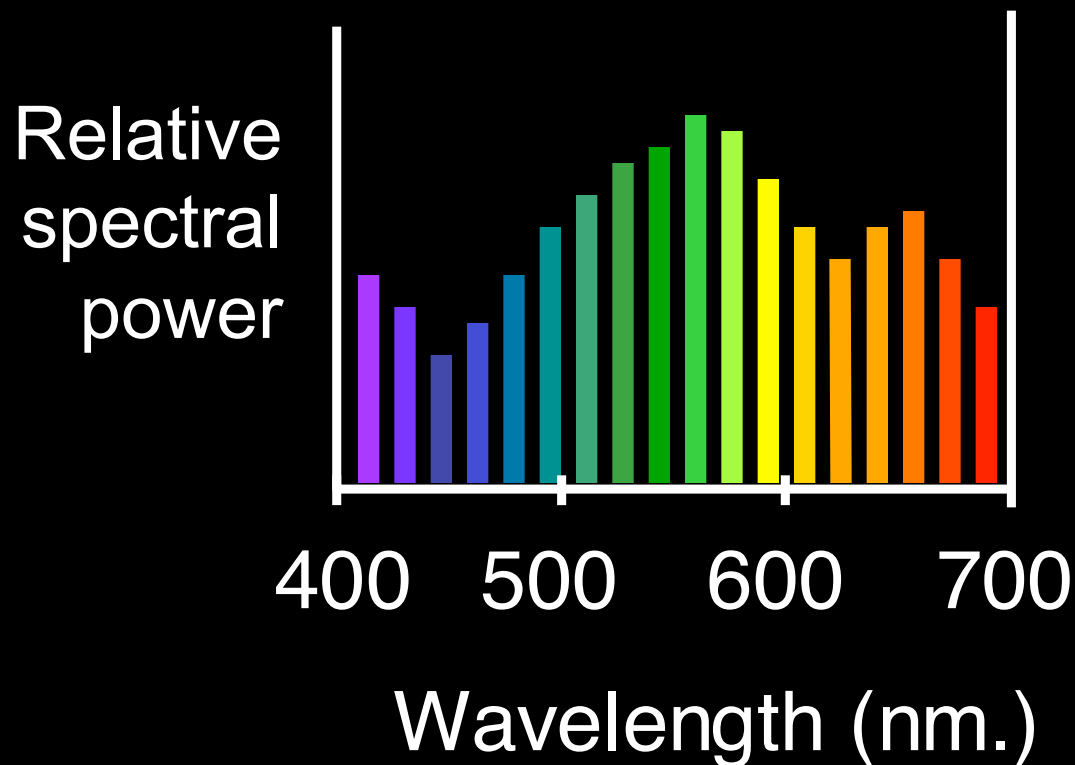
Why do we see light of these wavelengths?



...because that's where the Sun radiates EM energy

The Physics of Light

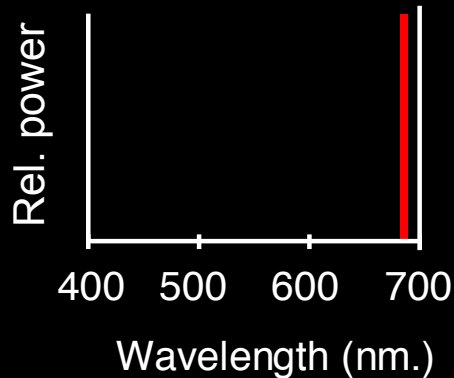
Any source of light can be completely described physically by its spectrum: the amount of energy emitted (per time unit) at each wavelength 400 - 700 nm.



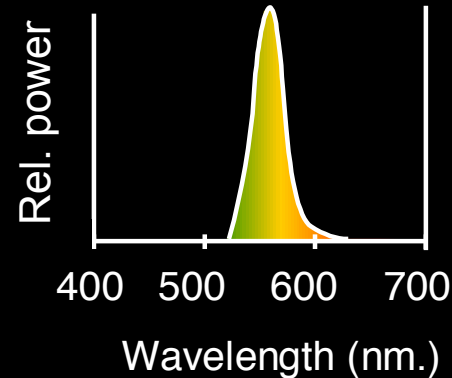
The Physics of Light

Some examples of the spectra of light sources

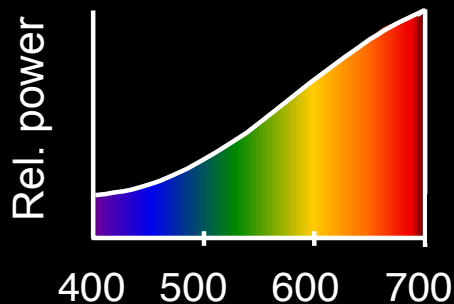
A. Ruby Laser



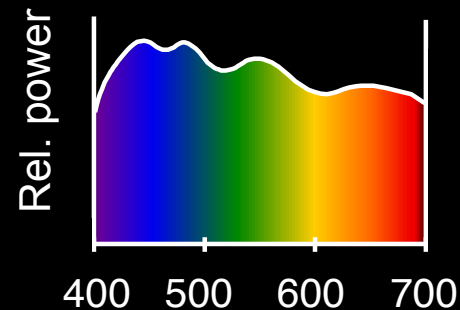
B. Gallium Phosphide Crystal



C. Tungsten Lightbulb

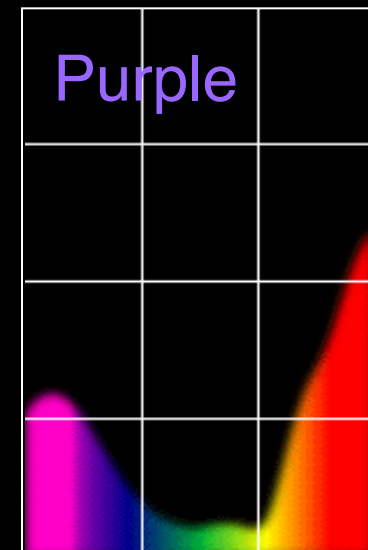
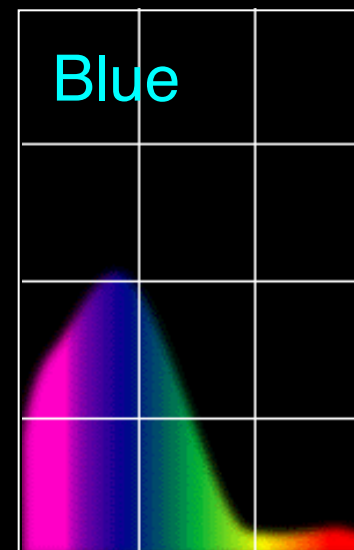
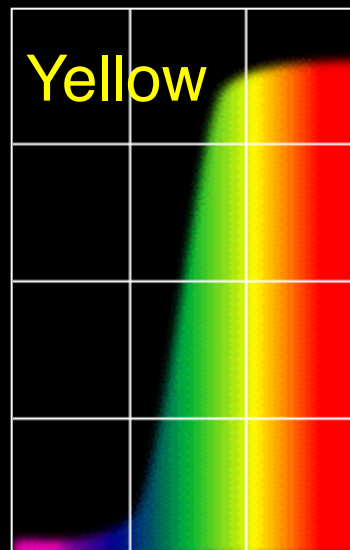
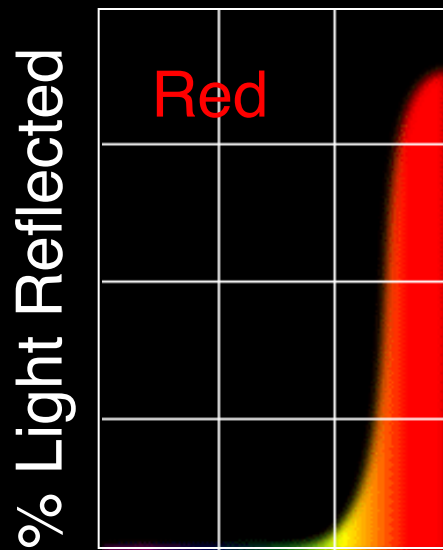


D. Normal Daylight



The Physics of Light

Some examples of the reflectance spectra of surfaces



400

700

400

700

400

700

400

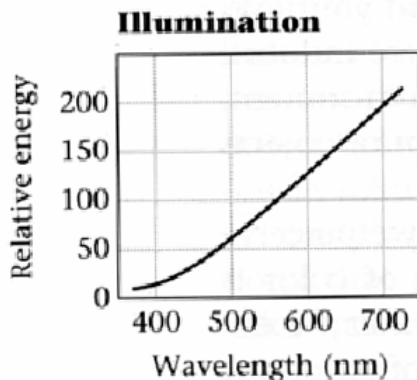
700

Wavelength (nm)

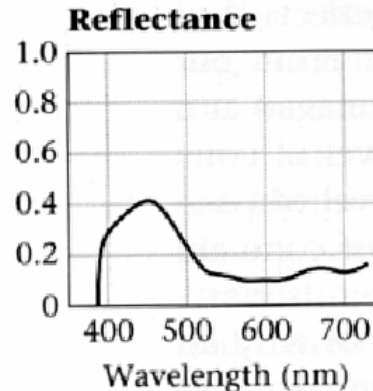
Interaction of light and surfaces



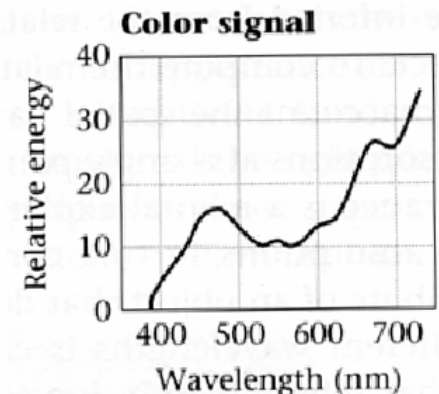
- Reflected color is the result of interaction of light source spectrum with surface reflectance
- Spectral radiometry
 - All definitions and units are now “per unit wavelength”
 - All terms are now “spectral”



• *



=



Interaction of light and surfaces

- What is the observed color of any surface under monochromatic light?

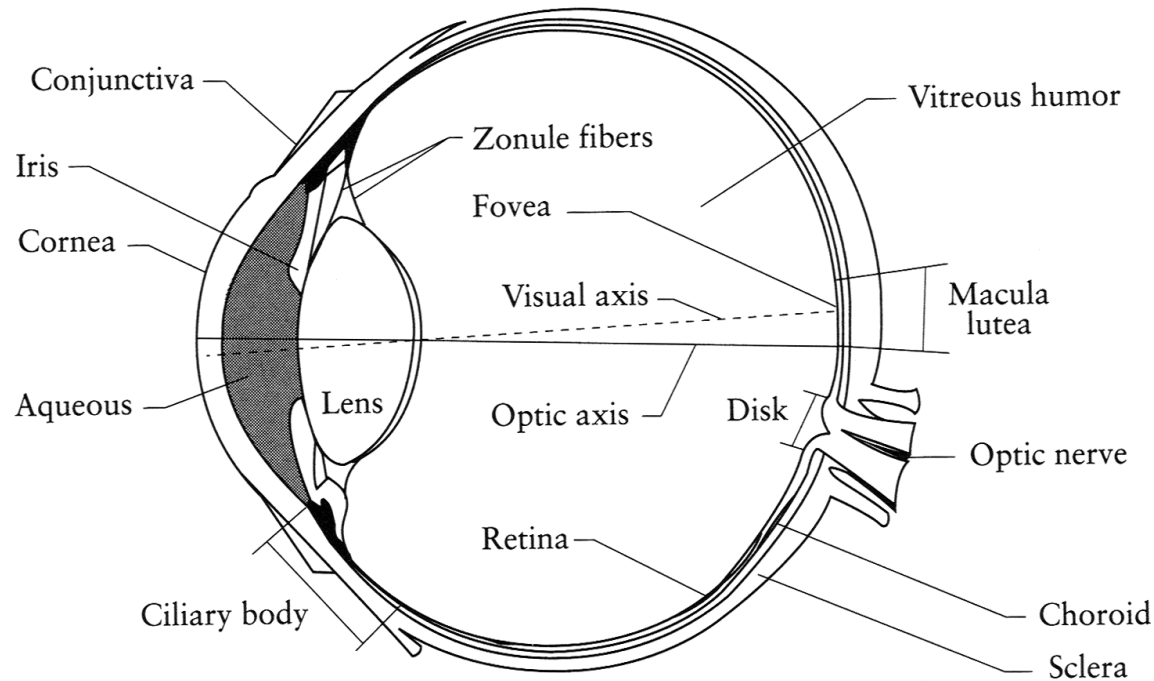


[Olafur Eliasson, *Room for one color*](#)

Overview of Color

- Physics of color
- Human encoding of color
- Color spaces
- White balancing

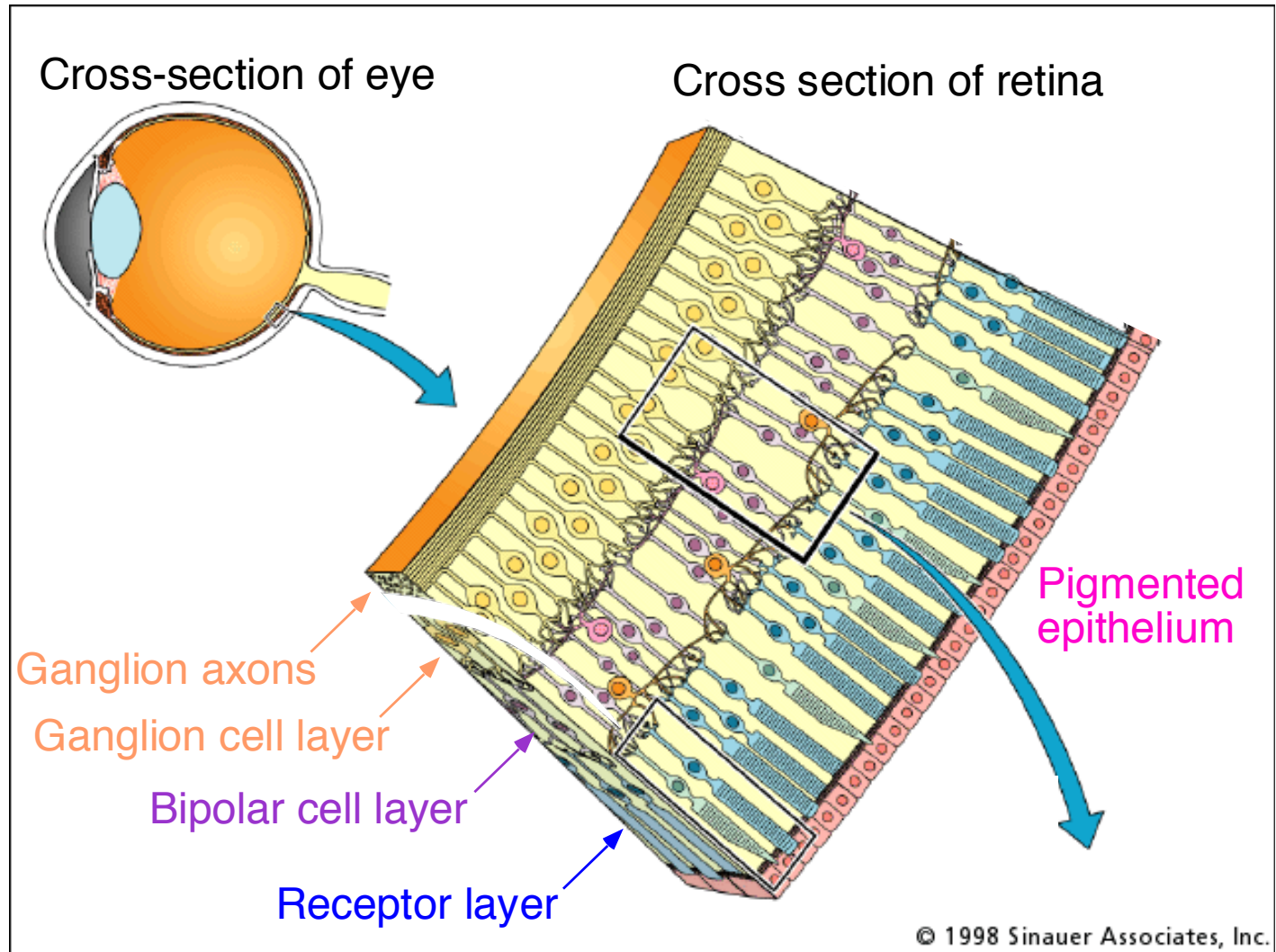
The Eye



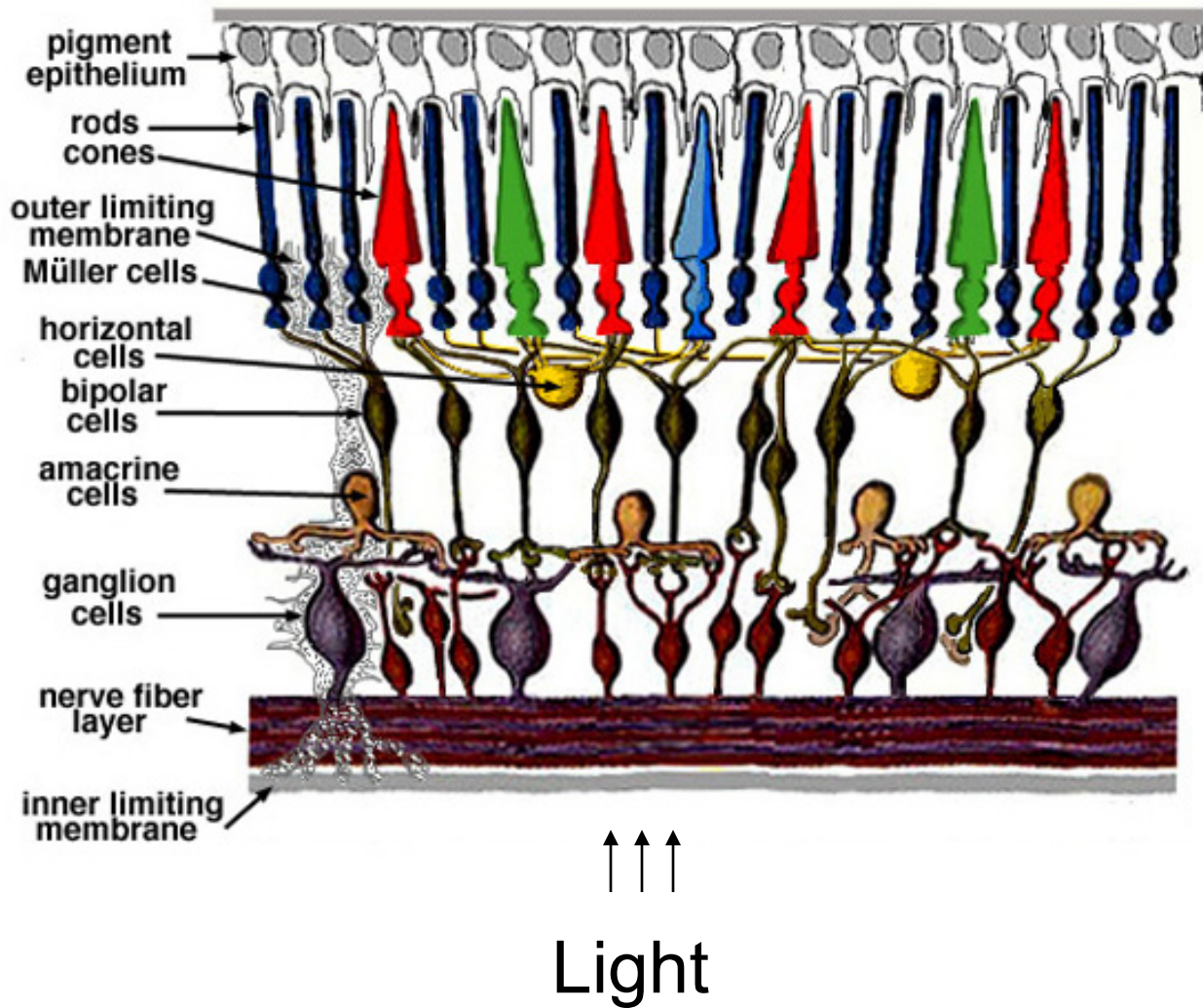
The human eye is a camera!

- **Iris** - colored annulus with radial muscles
- **Pupil** - the hole (aperture) whose size is controlled by the iris
- What's the "film"?
 - photoreceptor cells (rods and cones) in the **retina**

The Retina



Retina up-close



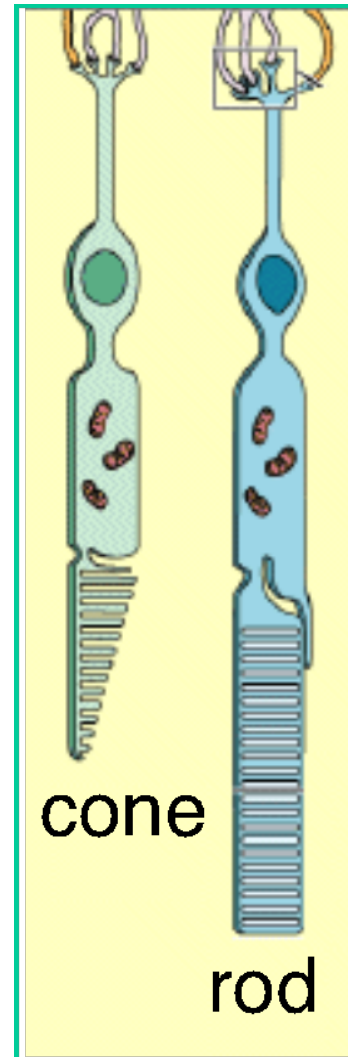
Two types of light-sensitive receptors

Cones

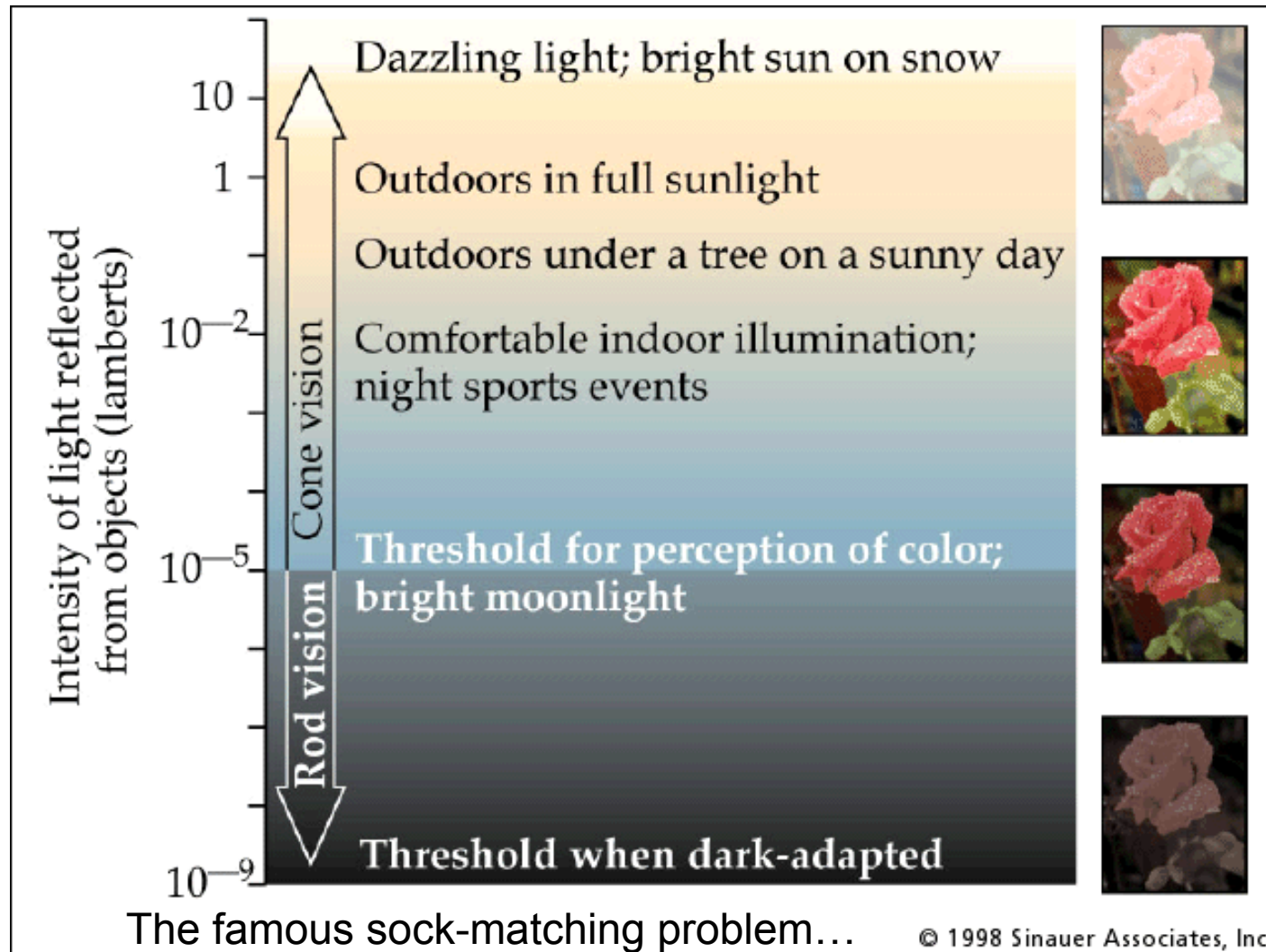
cone-shaped
less sensitive
operate in high light
color vision

Rods

rod-shaped
highly sensitive
operate at night
gray-scale vision

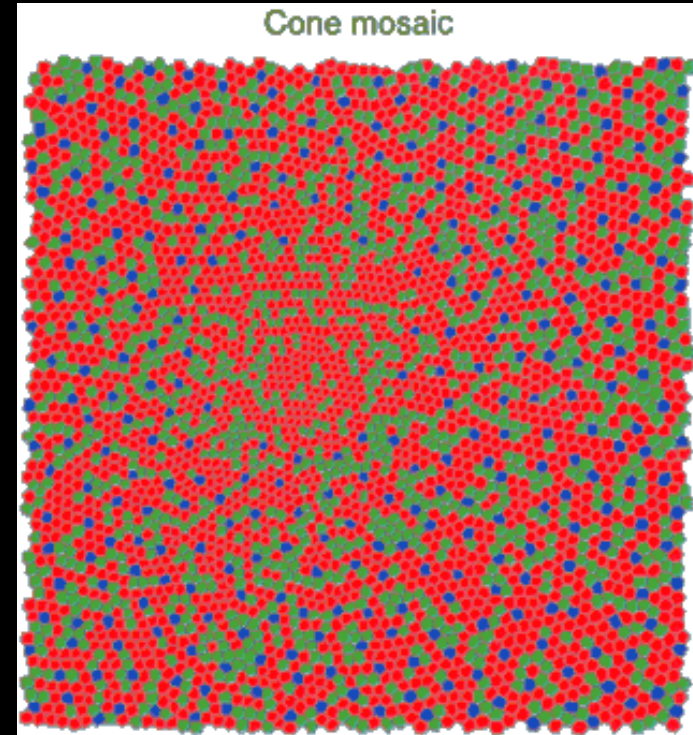
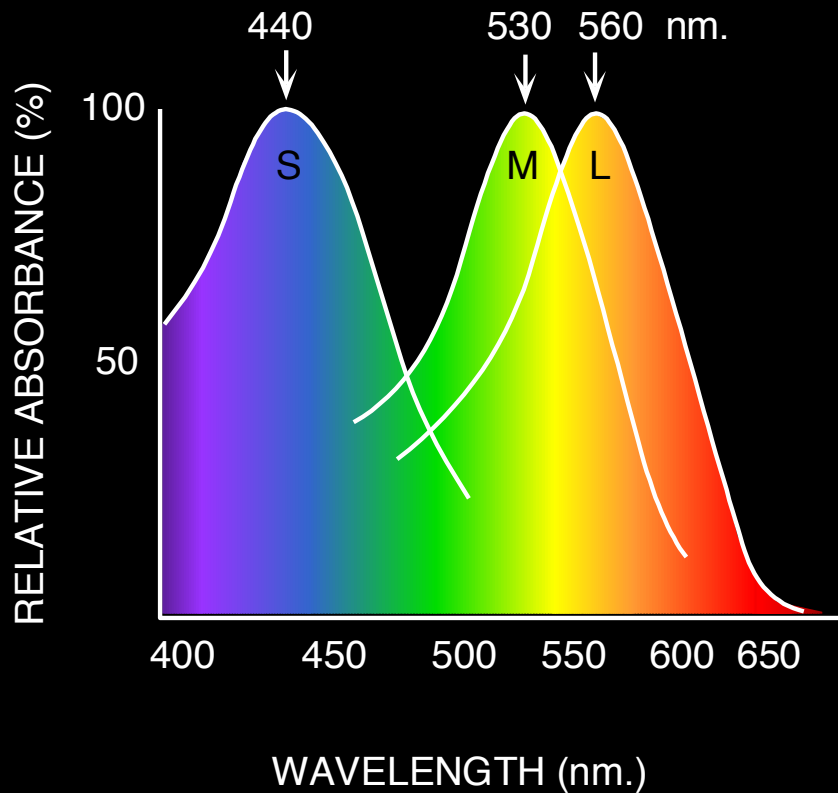


Rod / Cone sensitivity



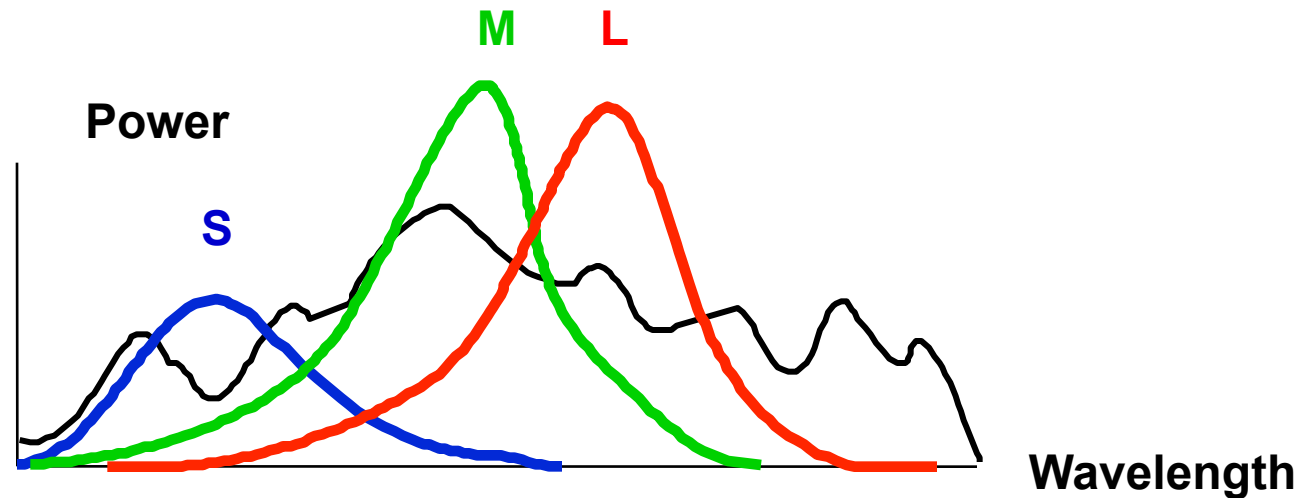
Physiology of Color Vision

Three kinds of cones:



- Why are M and L cones so close?
- Are there 3?

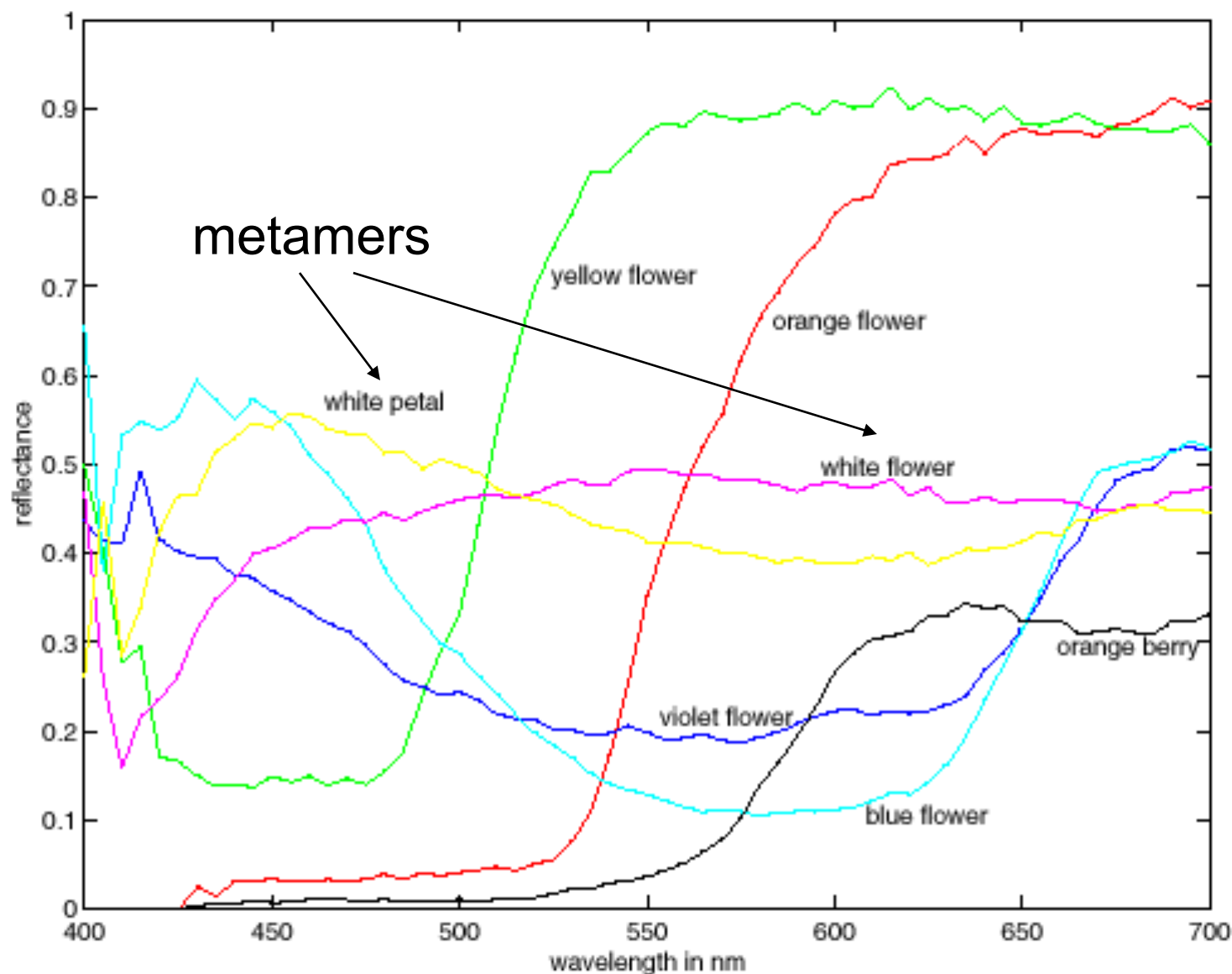
Color perception



Rods and cones act as filters on the spectrum

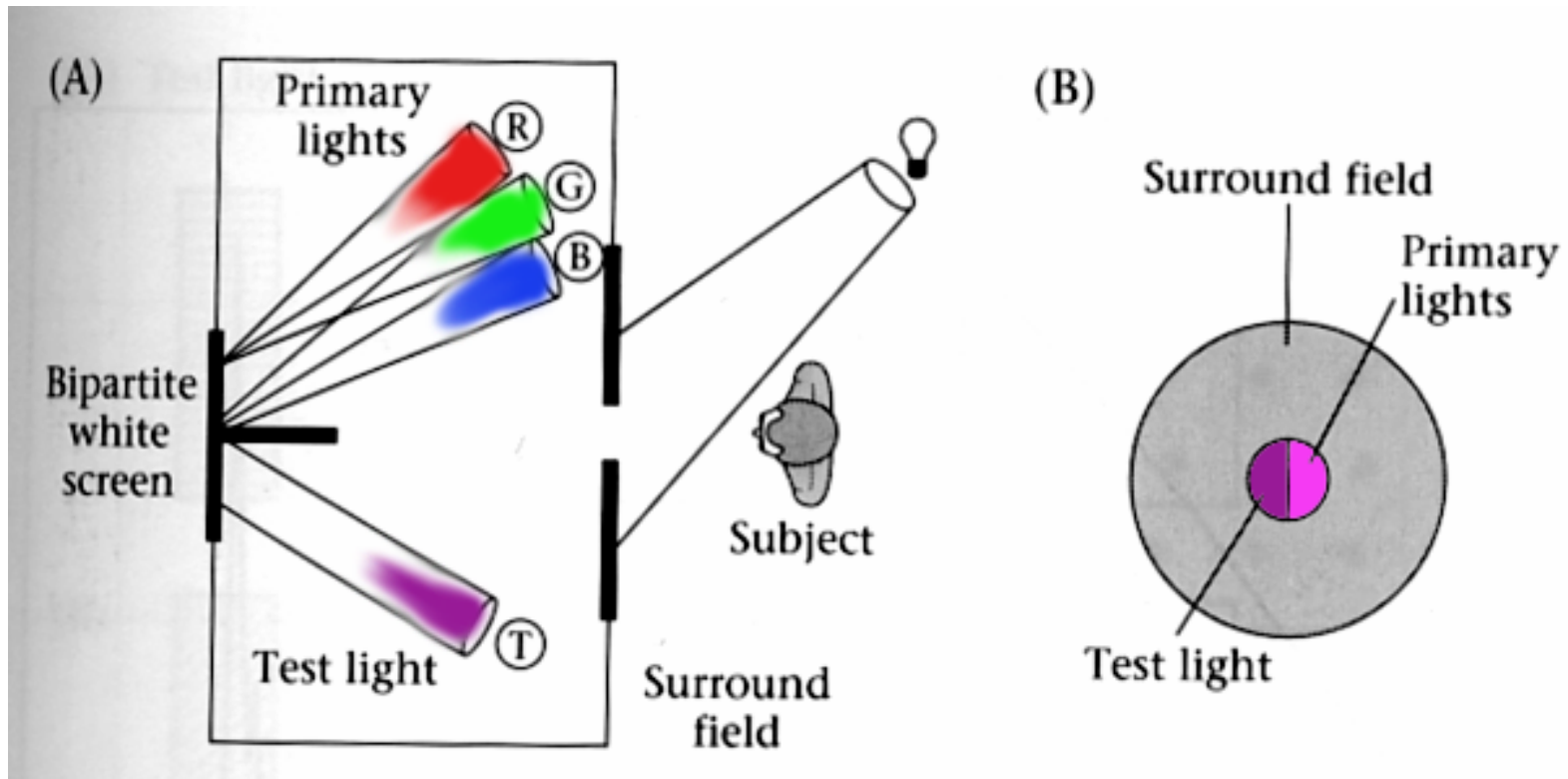
- To get the output of a filter, multiply its response curve by the spectrum, integrate over all wavelengths
 - Each cone yields one number
- Q: How can we represent an entire spectrum with 3 numbers?
- A: We can't! Most of the information is lost.
 - As a result, two different spectra may appear indistinguishable
 - » such spectra are known as **metamers**

Spectra of some real-world surfaces

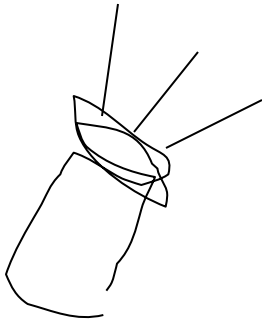
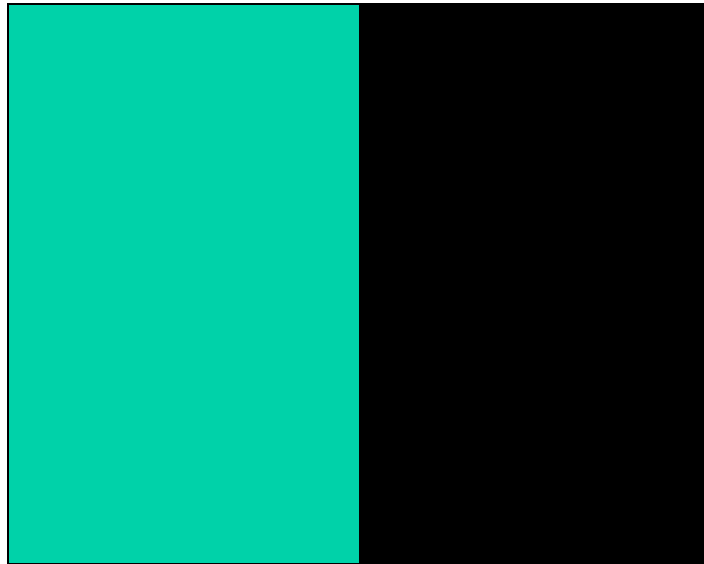


Standardizing color experience

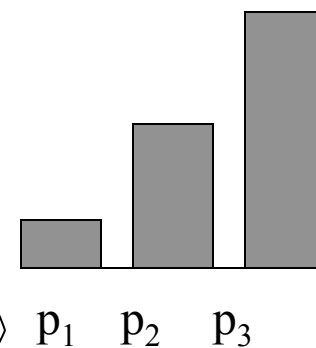
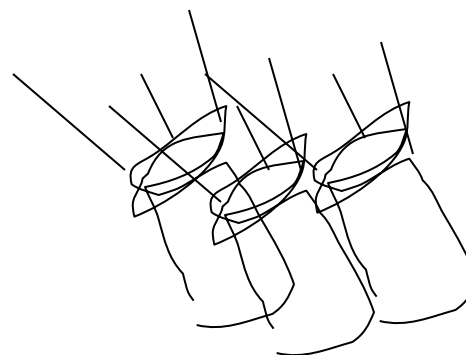
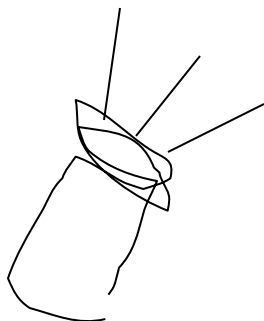
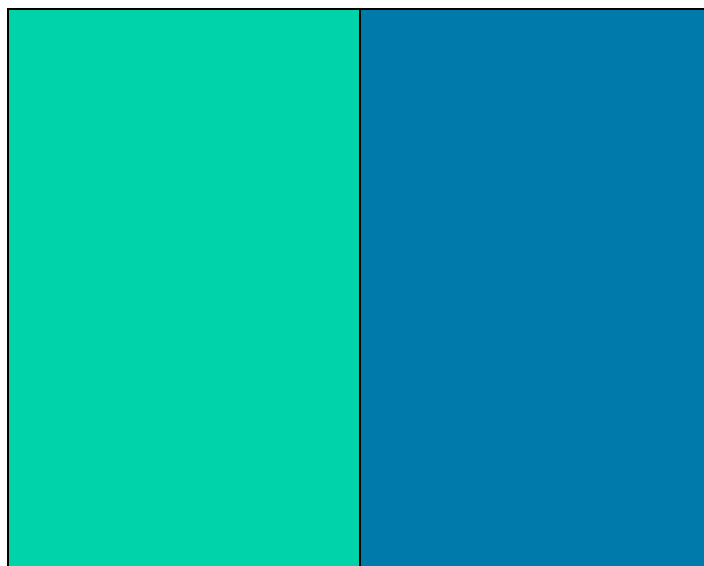
- We would like to understand which spectra produce the same color sensation in people under similar viewing conditions
- Color matching experiments



Color matching experiment 1

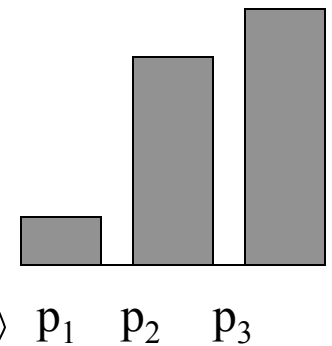
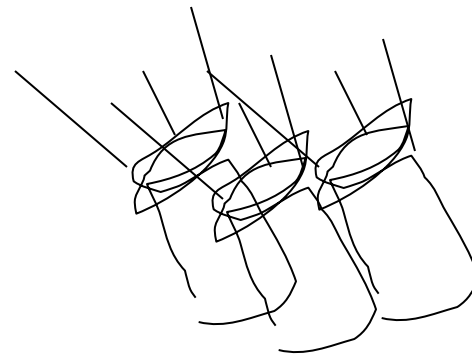
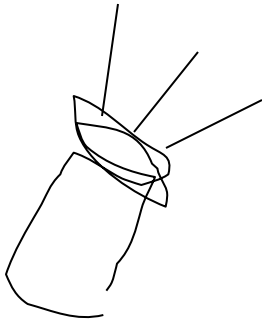
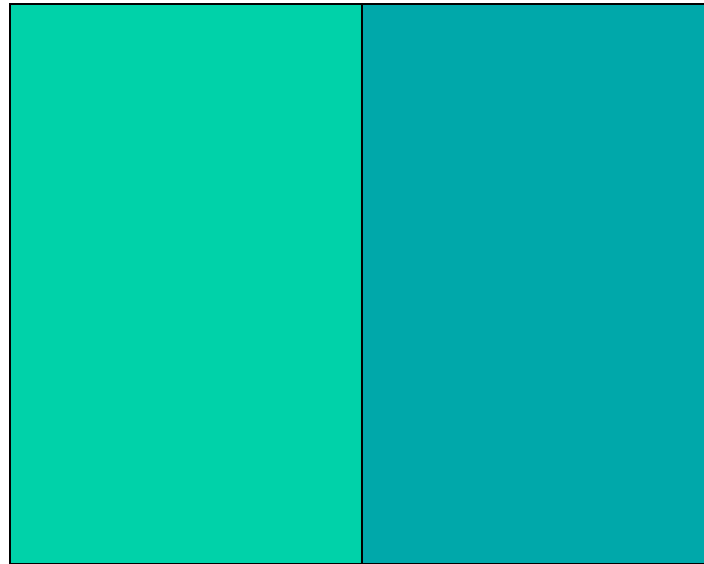


Color matching experiment 1

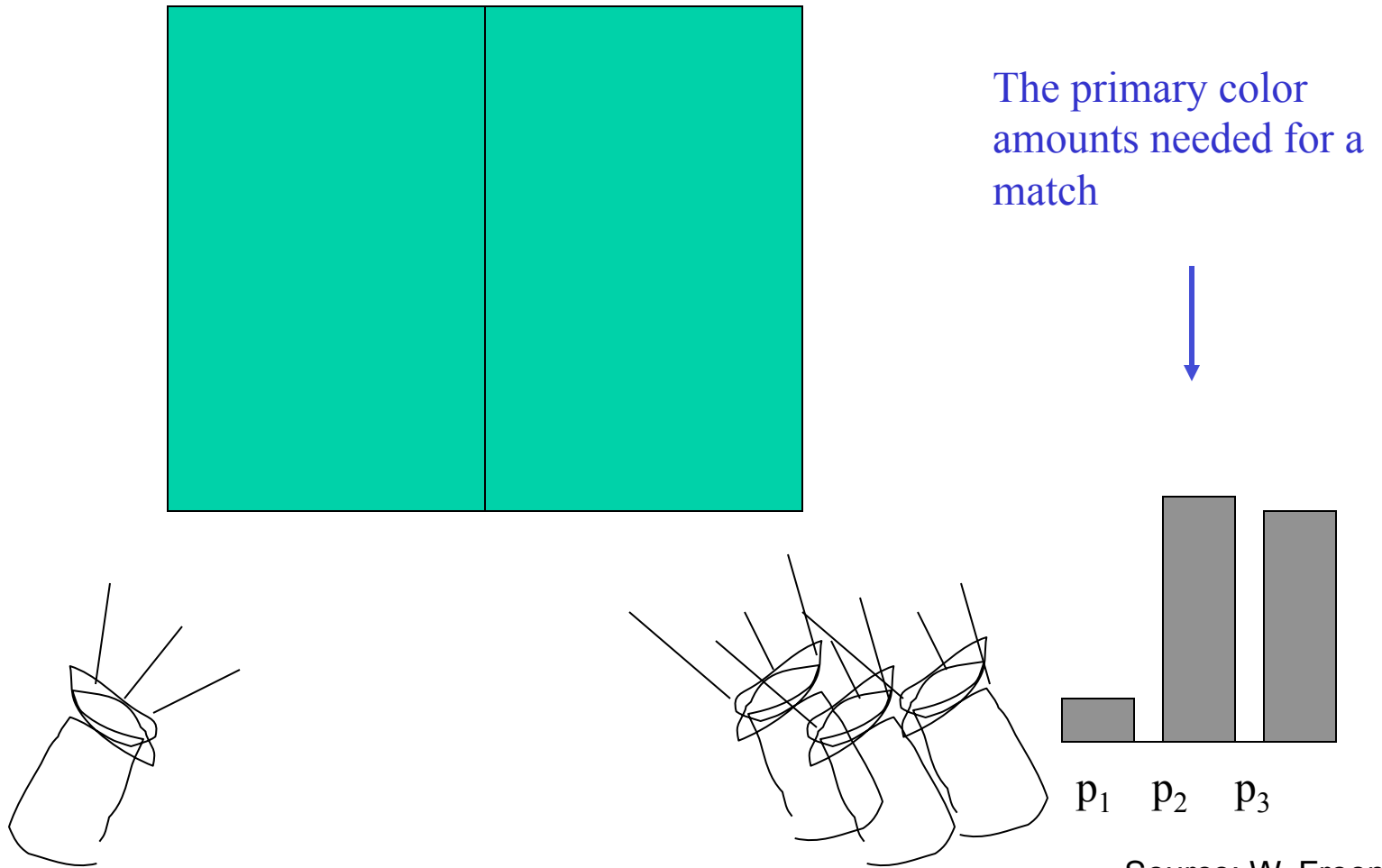


Source: W. Freeman

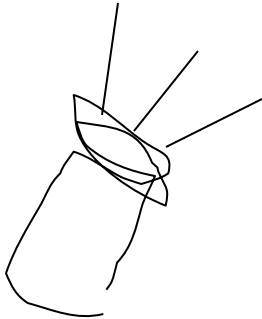
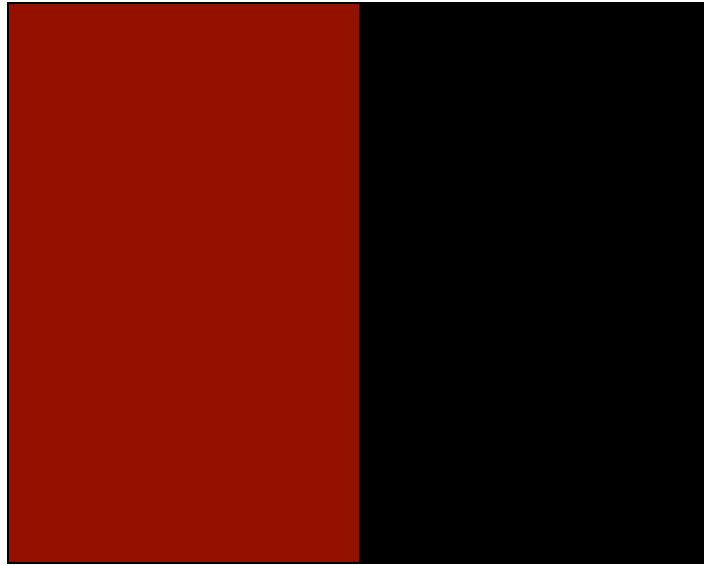
Color matching experiment 1



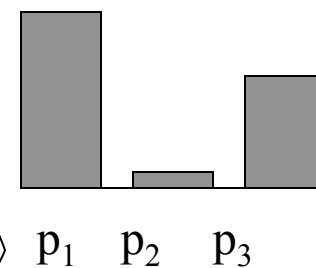
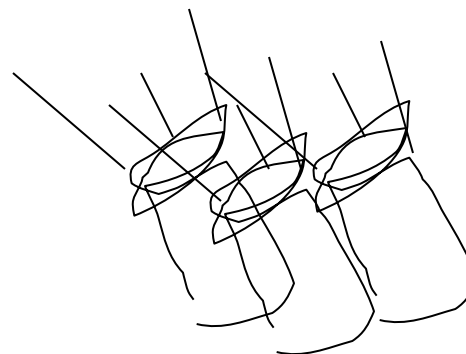
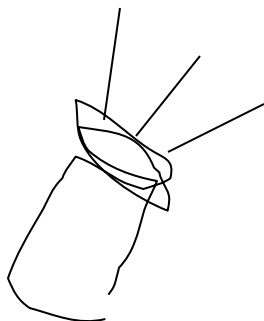
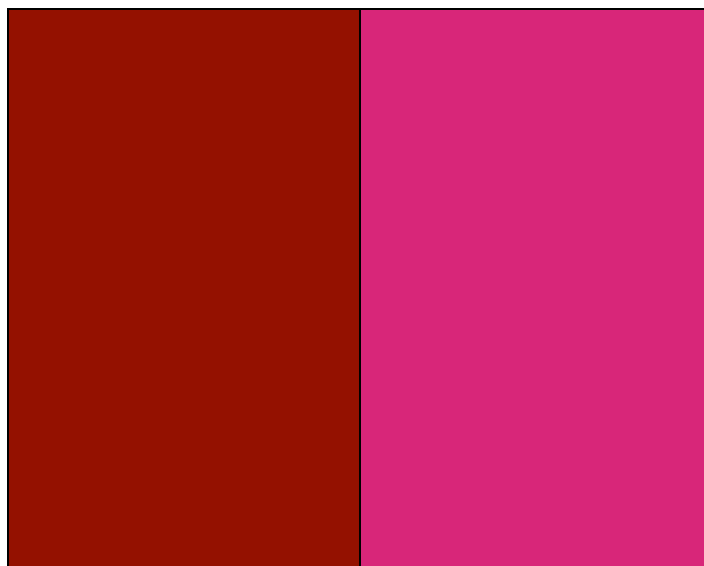
Color matching experiment 1



Color matching experiment 2

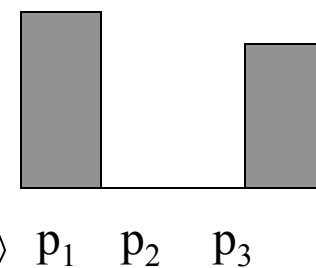
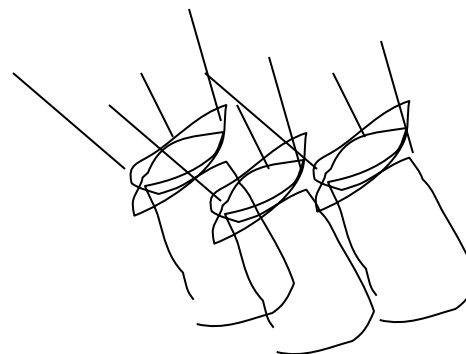
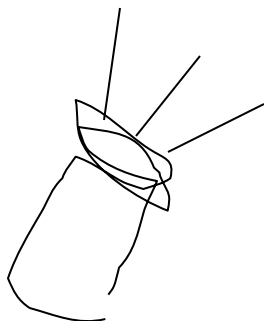
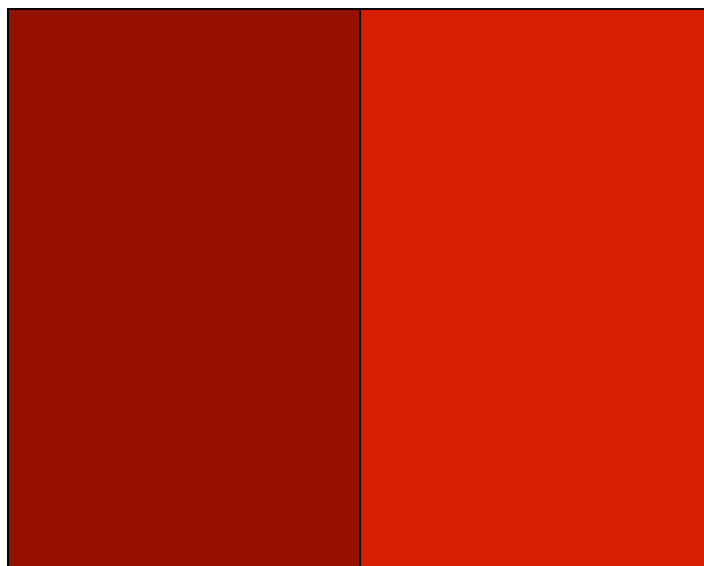


Color matching experiment 2



Source: W. Freeman

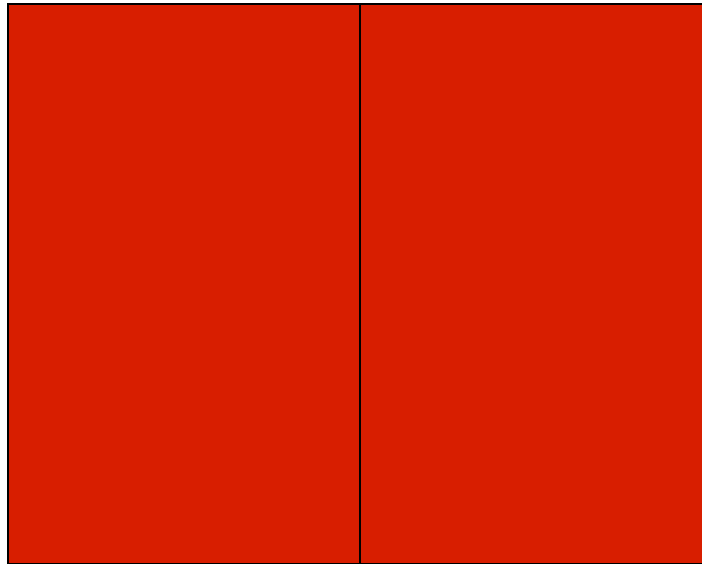
Color matching experiment 2



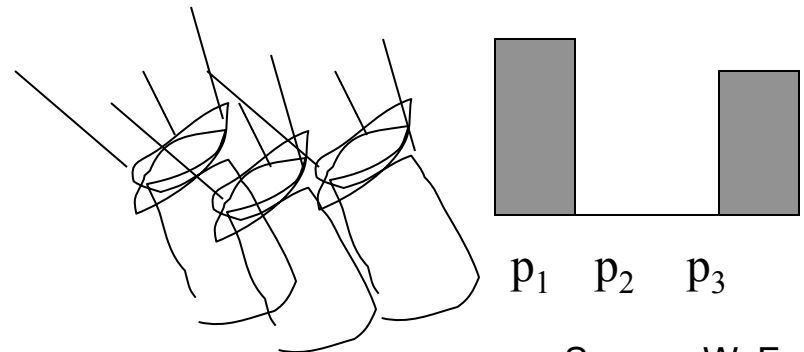
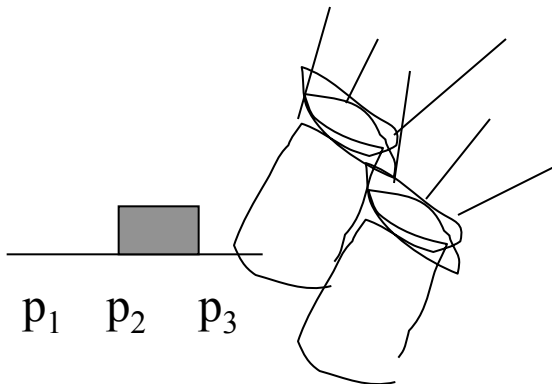
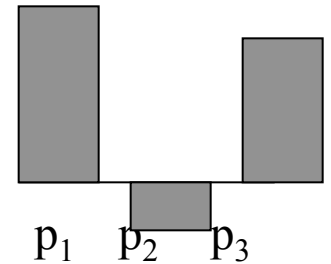
Source: W. Freeman

Color matching experiment 2

We say a “negative” amount of p_2 was needed to make the match, because we added it to the test color’s side.



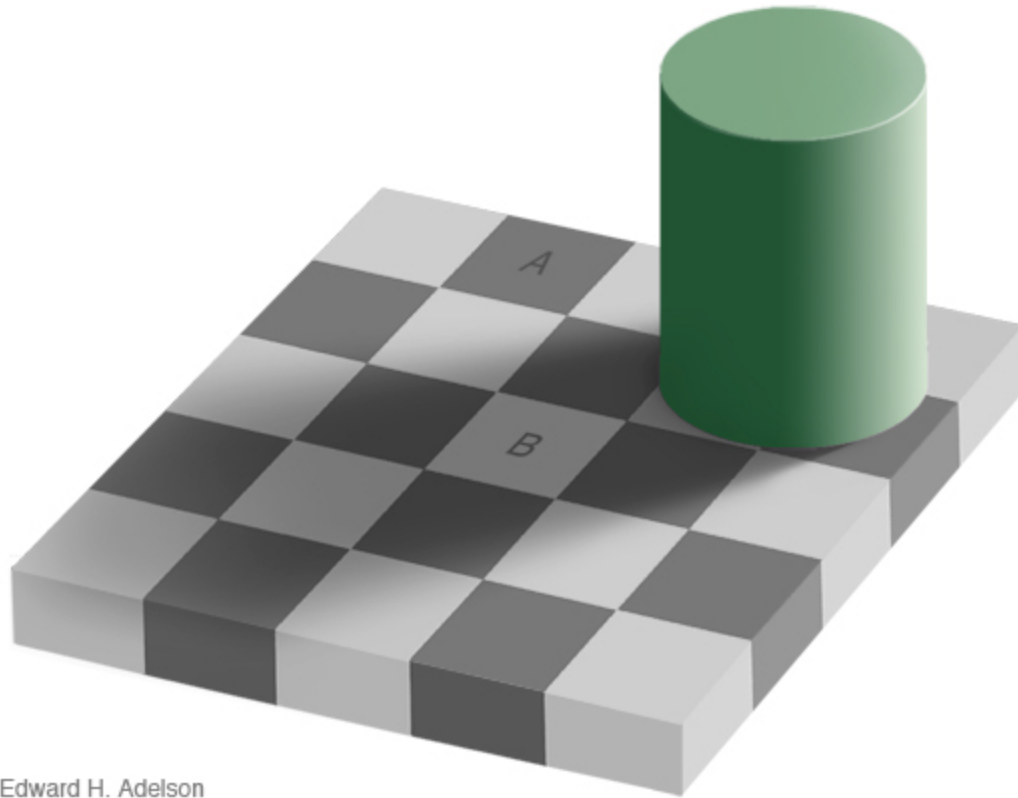
The primary color amounts needed for a match:



Trichromacy

- In color matching experiments, most people can match any given light with three primaries
 - Primaries must be *independent*
- For the same light and same primaries, most people select the same weights
 - Exception: color blindness
- Trichromatic color theory
 - Three numbers seem to be sufficient for encoding color
 - Dates back to 18th century (Thomas Young)

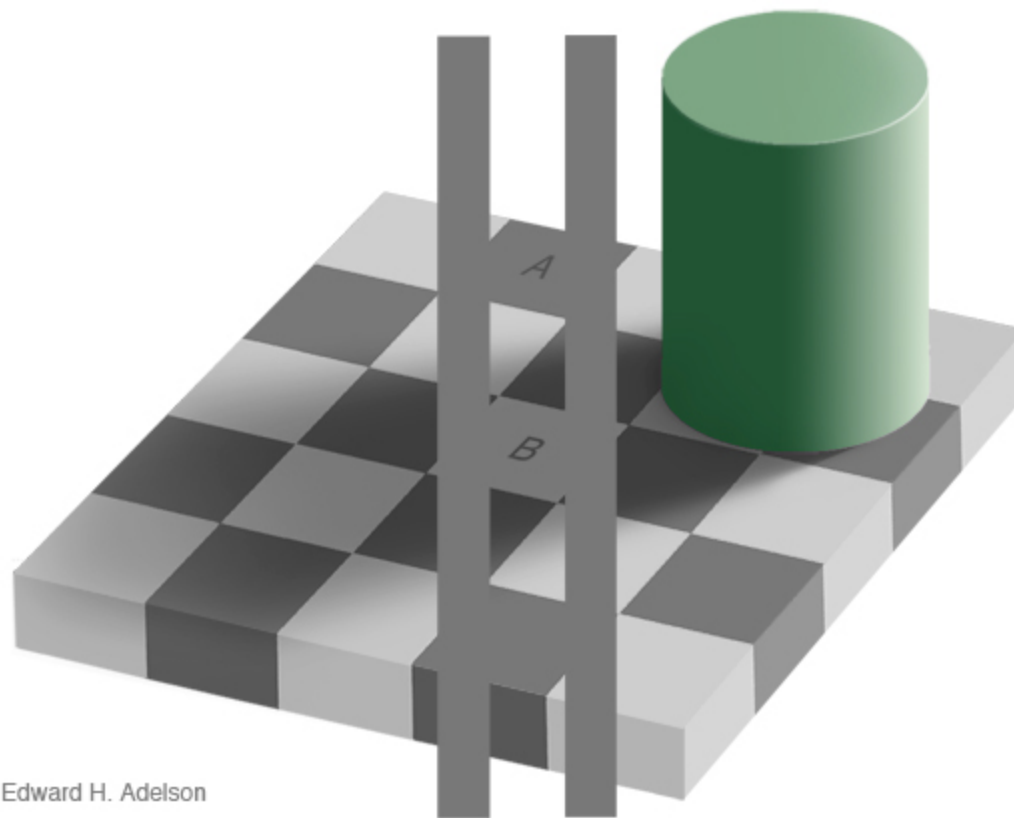
Lightness constancy



Edward H. Adelson

http://web.mit.edu/persci/people/adelson/checkershadow_illusion.html

Lightness constancy



- Possible explanations
 - Simultaneous contrast
 - Reflectance edges vs. illumination edges

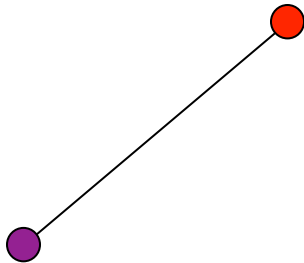
http://web.mit.edu/persci/people/adelson/checkershadow_illusion.html

Overview of Color

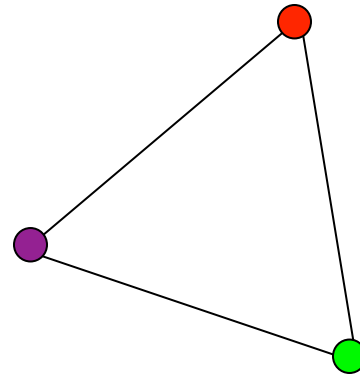
- Physics of color
- Human encoding of color
- Color spaces
- White balancing

Linear color spaces

- Defined by a choice of three *primaries*
- The coordinates of a color are given by the weights of the primaries used to match it

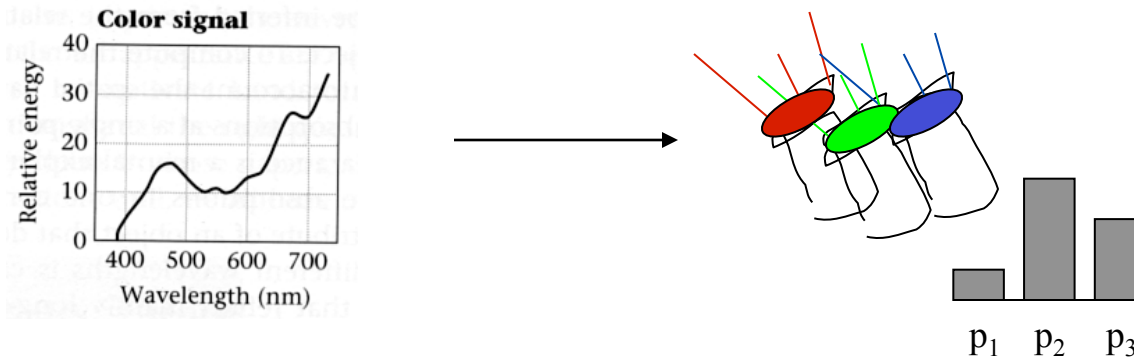


mixing two lights produces
colors that lie along a straight
line in color space



mixing three lights produces
colors that lie within the triangle
they define in color space

How to compute the weights of the primaries to match any spectral signal

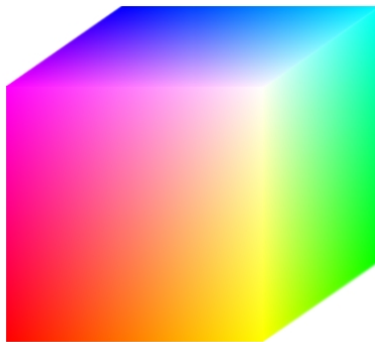





- **Matching functions:** the amount of each primary needed to match a monochromatic light source at each wavelength

RGB space

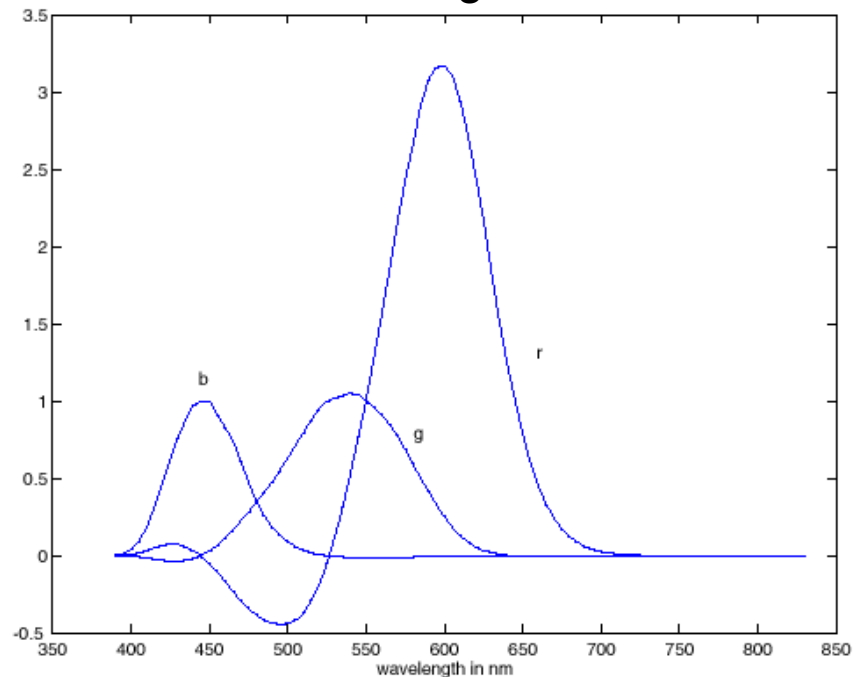
- Primaries are monochromatic lights (for monitors, they correspond to the three types of phosphors)
- *Subtractive matching* required for some wavelengths

RGB primaries



 $p_1 = 645.2 \text{ nm}$
 $p_2 = 525.3 \text{ nm}$
 $p_3 = 444.4 \text{ nm}$

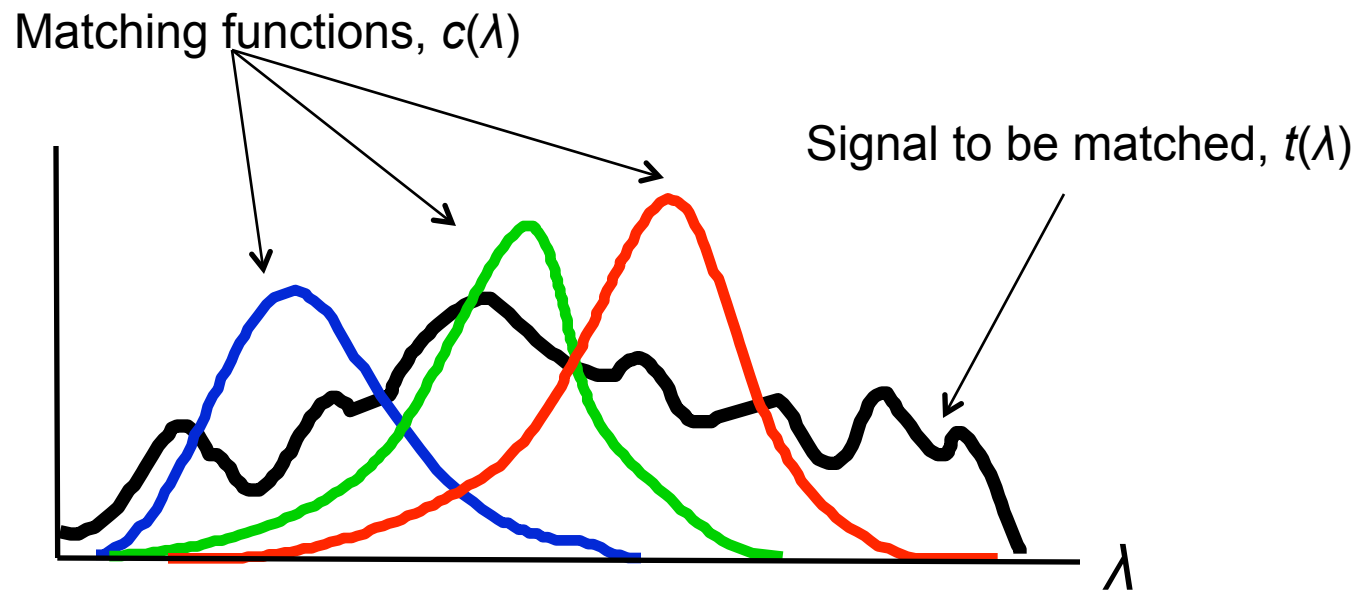
RGB matching functions



How to compute the weights of the primaries to match any spectral signal

- Let $c(\lambda)$ be one of the matching functions, and let $t(\lambda)$ be the spectrum of the signal. Then the weight of the corresponding primary needed to match t is

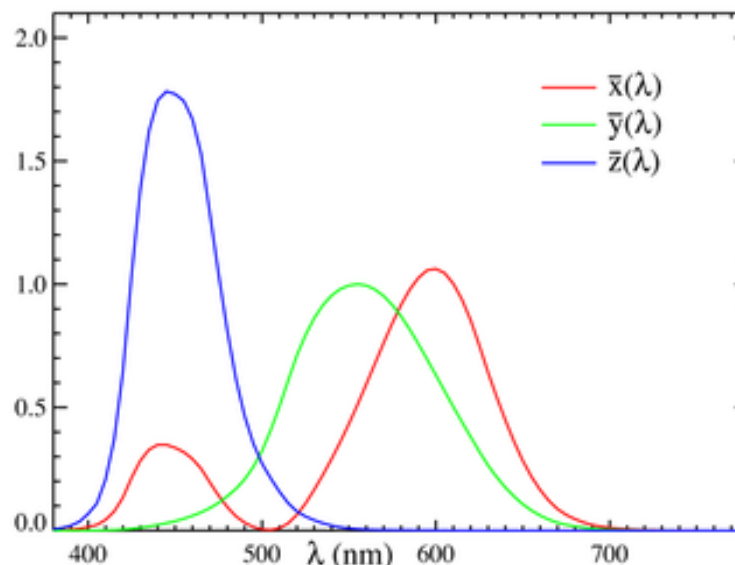
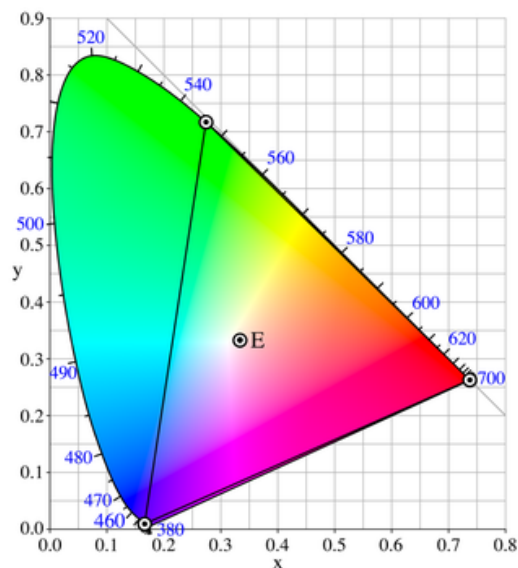
$$w = \int_{\lambda} c(\lambda)t(\lambda)d\lambda$$



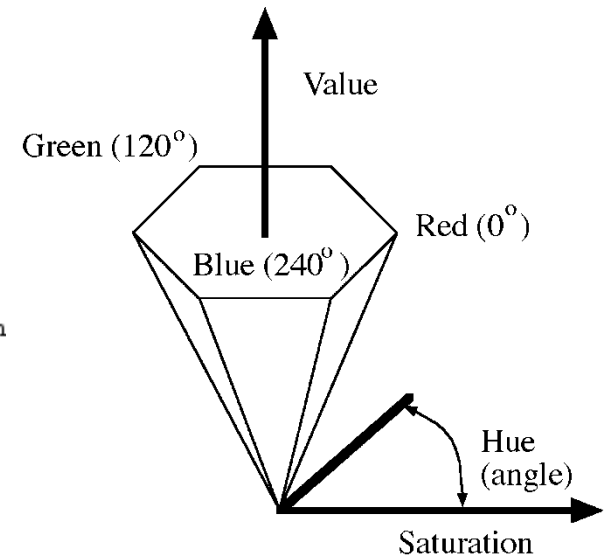
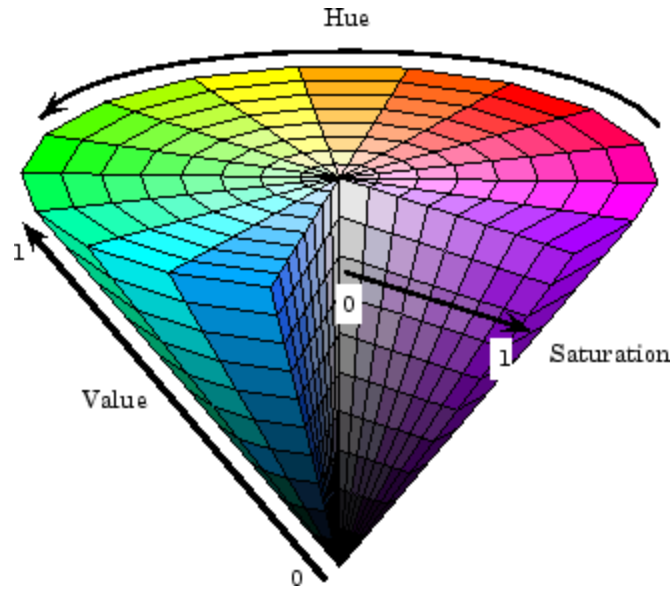
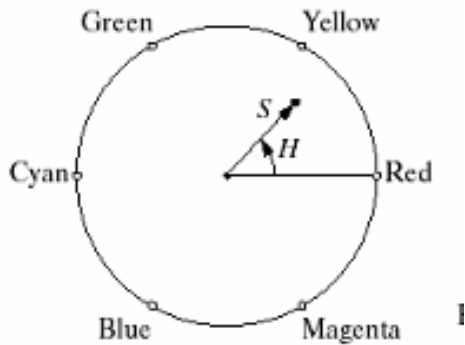
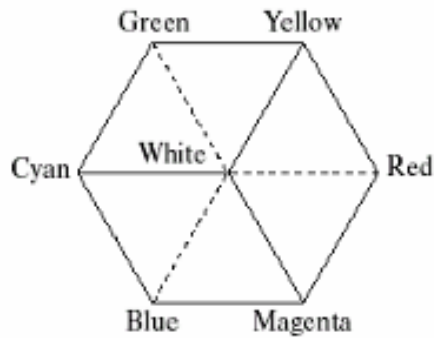
Linear color spaces: CIE XYZ

- Primaries are imaginary, but matching functions are everywhere positive
- The Y parameter corresponds to brightness or *luminance* of a color
- 2D visualization: draw (x,y) , where $x = X/(X+Y+Z)$, $y = Y/(X+Y+Z)$

Matching functions



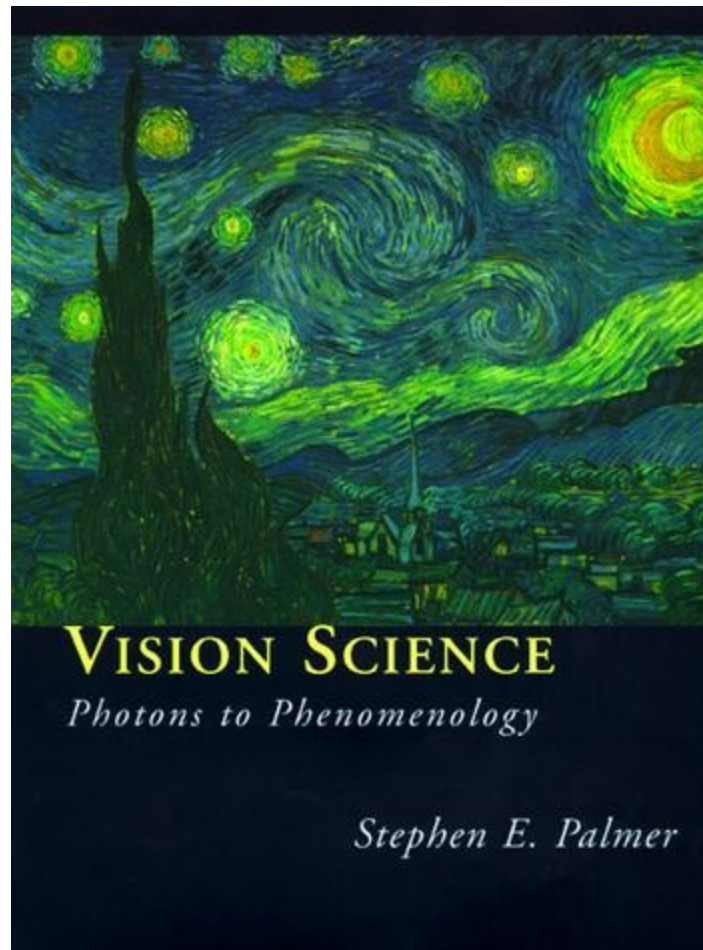
Nonlinear color spaces: HSV



- Perceptually meaningful dimensions: Hue, Saturation, Value (Intensity)
- RGB cube on its vertex

Useful reference

Stephen E. Palmer, **Vision Science: Photons to Phenomenology**, MIT Press, 1999



Overview of Color

- Physics of color
- Human encoding of color
- Color spaces
- White balancing

White balance

- When looking at a picture on screen or print, we adapt to the illuminant of the room, not to that of the scene in the picture
- When the white balance is not correct, the picture will have an unnatural color “cast”

incorrect white balance

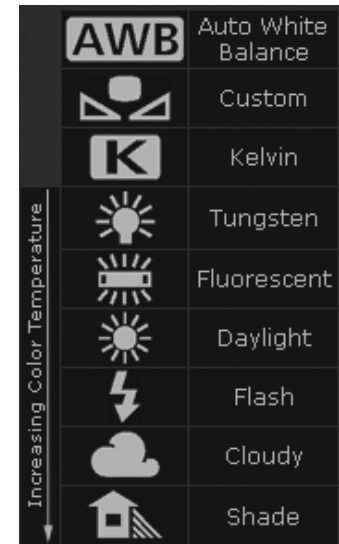


correct white balance



White balance

- Film cameras:
 - Different types of film or different filters for different illumination conditions
- Digital cameras:
 - Automatic white balance
 - White balance settings corresponding to several common illuminants
 - Custom white balance using a reference object



White balance

- Von Kries adaptation
 - Multiply each channel by a gain factor
 - A more general transformation would correspond to an arbitrary 3x3 matrix

White balance

- Von Kries adaptation
 - Multiply each channel by a gain factor
 - A more general transformation would correspond to an arbitrary 3x3 matrix
- Best way: gray card
 - Take a picture of a neutral object (white or gray)
 - Deduce the weight of each channel
 - If the object is recoded as r_w, g_w, b_w
use weights $1/r_w, 1/g_w, 1/b_w$

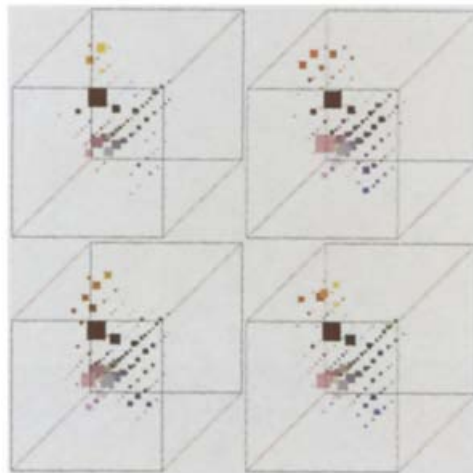
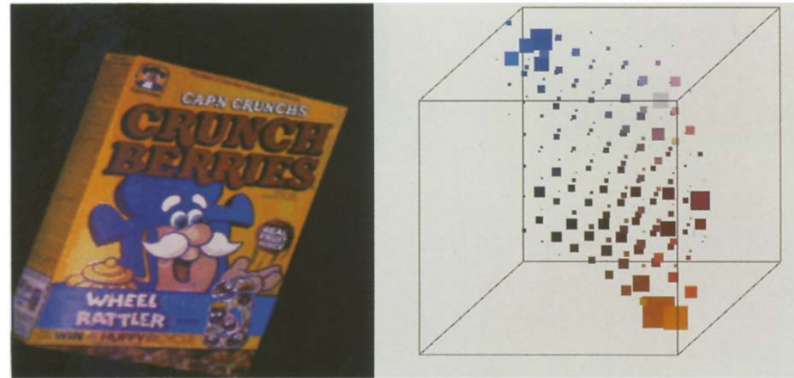
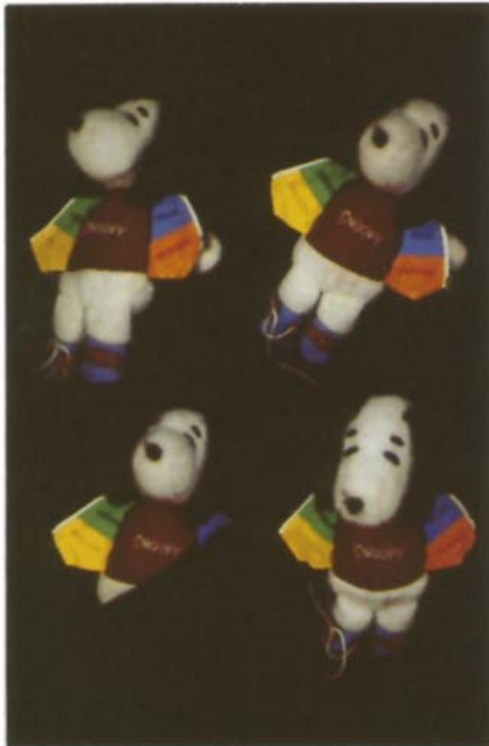


White balance

- Without gray cards: we need to “guess” which pixels correspond to white objects
- Gray world assumption
 - The image average r_{ave} , g_{ave} , b_{ave} is gray
 - Use weights $1/r_{ave}$, $1/g_{ave}$, $1/b_{ave}$
- Brightest pixel assumption (non-saturated)
 - Highlights usually have the color of the light source
 - Use weights inversely proportional to the values of the brightest pixels
- Gamut mapping
 - Gamut: convex hull of all pixel colors in an image
 - Find the transformation that matches the gamut of the image to the gamut of a “typical” image under white light
- Use image statistics, learning techniques

Uses of color in computer vision

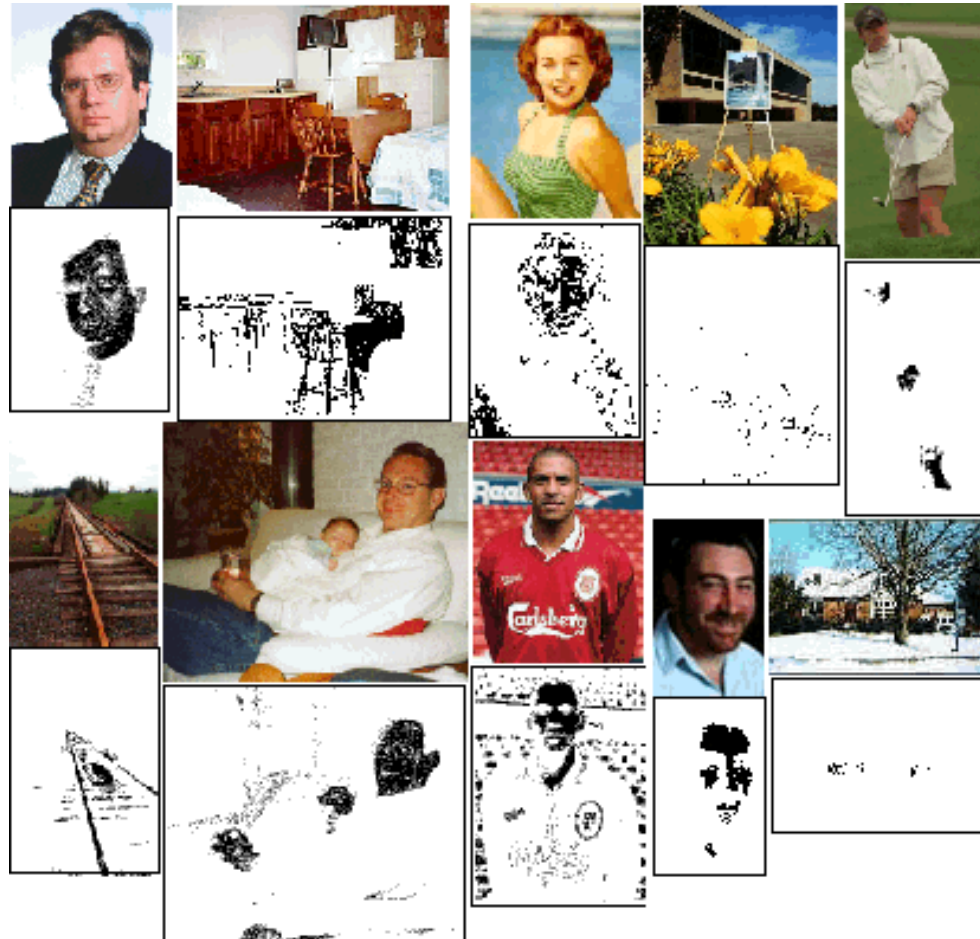
Color histograms for indexing and retrieval



Swain and Ballard, [Color Indexing](#), IJCV 1991.

Uses of color in computer vision

Skin detection



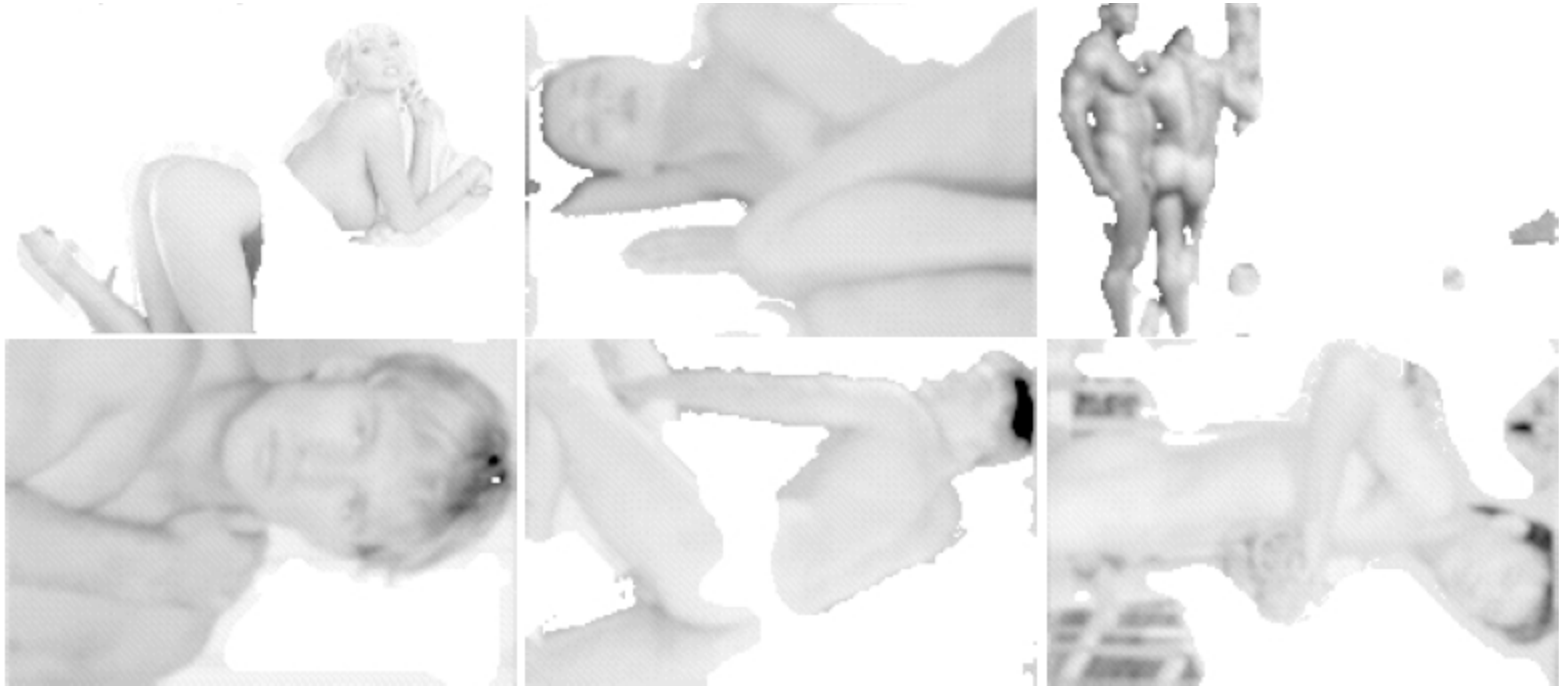
M. Jones and J. Rehg,

[Statistical Color Models with Application to Skin](#)

Source: S. Lazebnik

Uses of color in computer vision

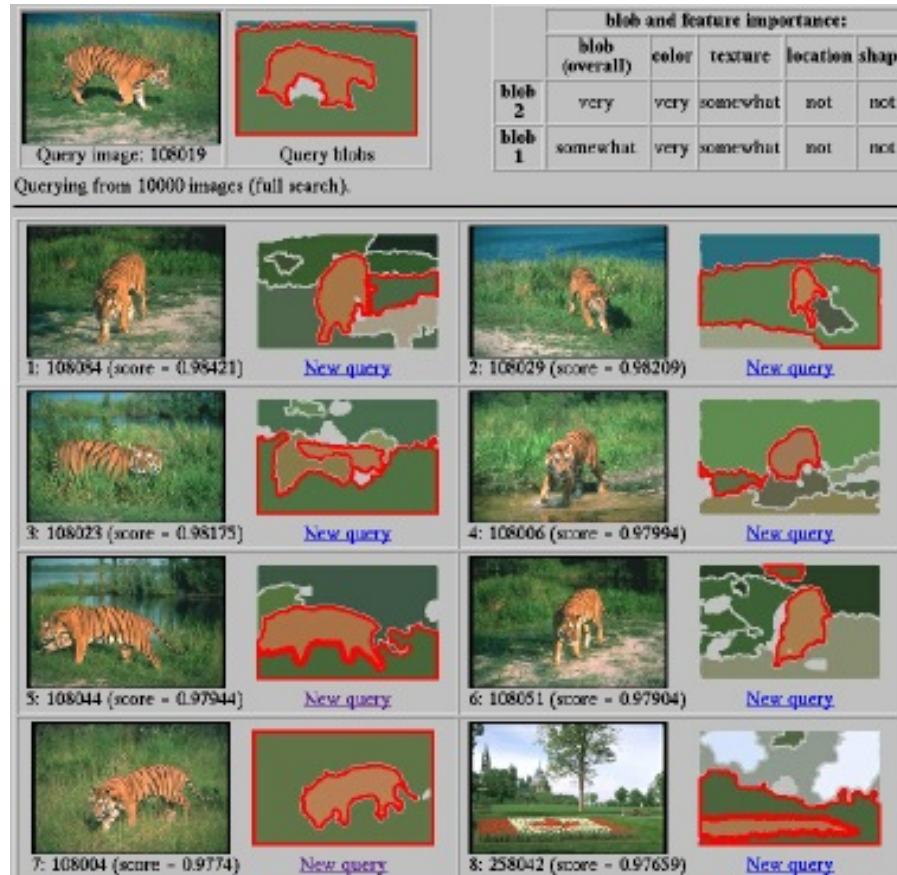
Nude people detection



Forsyth, D.A. and Fleck, M. M.,
[Automatic Detection of Human Nudes,](#) *International Journal of Computer Vision* , **32** , 1, 63-77, August, 1999

Uses of color in computer vision

Image segmentation and retrieval



C. Carson, S. Belongie, H. Greenspan, and Ji. Malik, Blobworld: Image segmentation using Expectation-Maximization and its application to image querying, ICVIS 1999.

Uses of color in computer vision

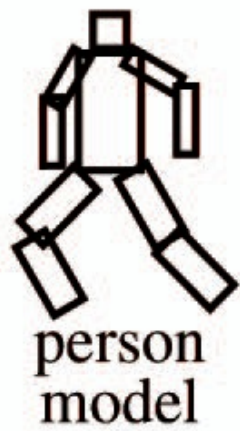
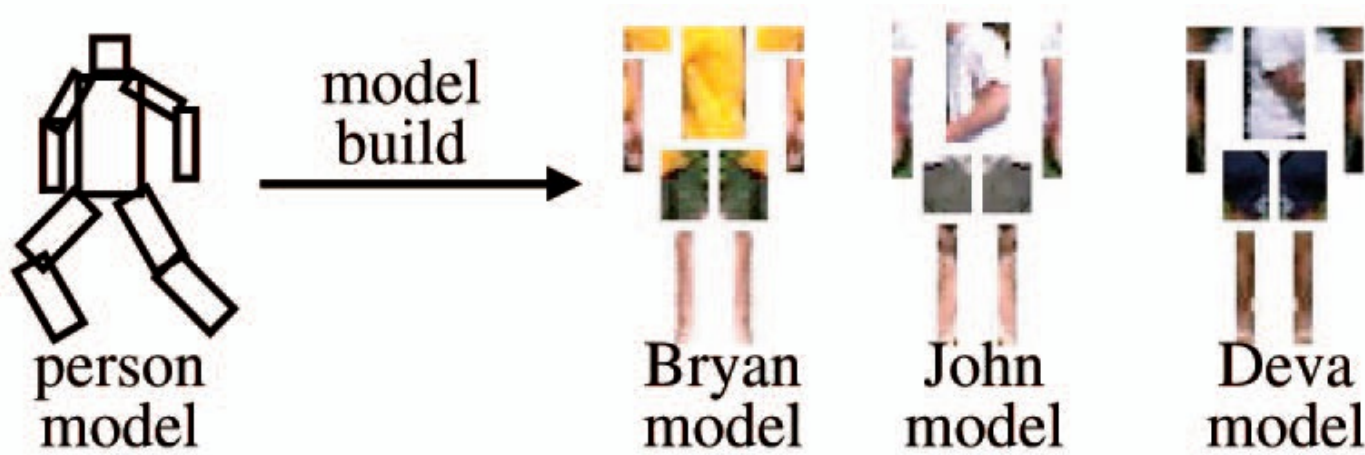
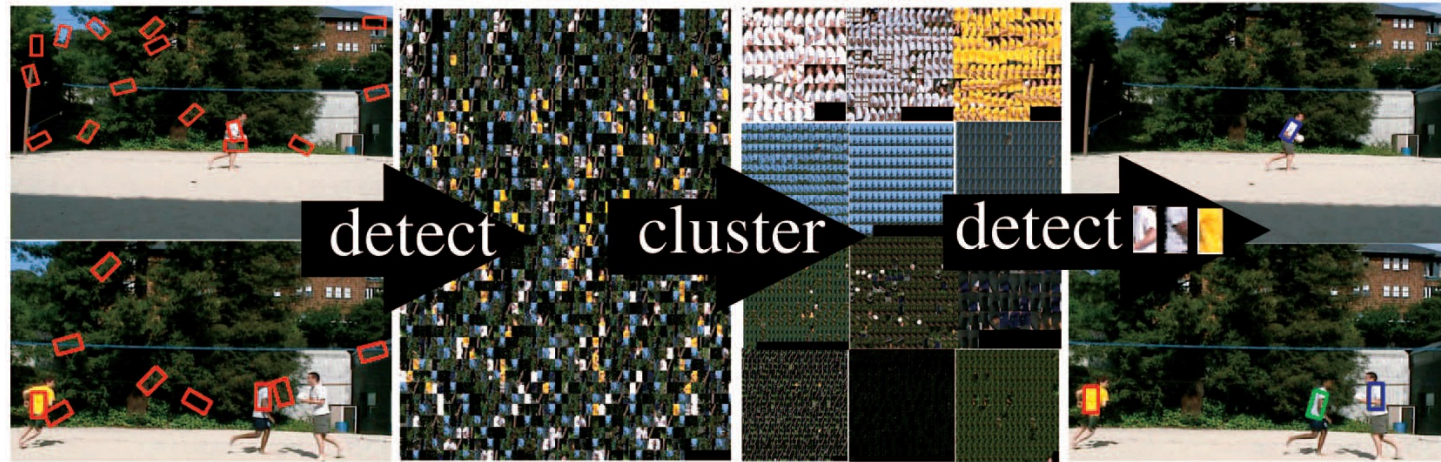
Robot soccer



M. Sridharan and P. Stone,
[Towards Eliminating Manual Color Calibration at RoboCup](#). RoboCup-2005: Robot Soccer World Cup IX,
Springer Verlag, 2006

Uses of color in computer vision

Building appearance models for tracking



model
build

