Scaling Multicore Databases via Constrained Parallel Execution

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ABSTRACT
Multicore in-memory databases often rely on traditional concurrency control schemes such as two-phase-locking (2PL) or optimistic concurrency control (OCC). Unfortunately, when the workload exhibits a non-trivial amount of contention, both 2PL and OCC sacrifice much parallel execution opportunity. In this paper, we describe a new concurrency control scheme, interleaving constrained concurrency control (IC3), which provides serializability while allowing for parallel execution of certain conflicting transactions. IC3 combines the static analysis of the transaction workload with runtime techniques that track and enforce dependencies among concurrent transactions. The use of static analysis simplifies IC3’s runtime design, allowing it to scale to many cores. Evaluations on a 64-core machine using the TPC-C benchmark show that IC3 outperforms traditional concurrency control schemes under contention. It achieves the throughput of 434K transactions/sec on the TPC-C benchmark configured with only one warehouse. It also scales better than several recent concurrent control schemes that also target contended workloads.

1. INTRODUCTION
Rapid increase of memory volume and CPU core counts have stimulated much recent development of multi-core in-memory databases [42, 15, 20, 27, 49, 51, 34, 54]. As the performance bottleneck has shifted from I/O to CPU, how to maximally take advantage of the CPU resources of multiple cores has become an important research problem.

A key challenge facing multi-core databases is how to support serializable transactions while maximizing parallelism so as to scale to many CPU cores. Popular concurrency control schemes are based on two-phase locking (2PL) [5, 19] or optimistic concurrency control (OCC) [26, 5]. Both achieve good parallel execution when concurrent transactions rarely conflict with each other. Unfortunately, when the workload exhibits contention, the performance of both schemes crumbles. 2PL makes transactions grab read/write locks, thus it serializes the execution of transactions as soon as they make a conflicting access to some data item. OCC performs worse under contention because it aborts and retries conflicting transactions.

There is much parallelism left unexploited by 2PL and OCC in contended workloads. As an example, suppose transactions 1 and 2 both modify data items A and B. One can safely interleave their execution as long as both transactions modify items A and B in the same order. Under 2PL or OCC, their execution is serialized. This paper presents IC3, a concurrency control scheme for multi-core in-memory databases, which unlocks such parallelism among conflicting transactions.

A basic strategy for safe interleaving is to track dependencies that arise as transactions make conflicting data access and to enforce tracked dependencies by constraining a transaction’s subsequent data access. This basic approach faces several challenges in order to extract parallelism while guaranteeing serializability: How to know which data access should be constrained and which ones should not? How to ensure transitive dependencies are not violated without having to explicitly track them (which is expensive)? How to guarantee that tracked dependencies are always enforceable at runtime?

IC3’s key to solving these challenges is to combine runtime techniques with a static analysis of the transaction workload to be executed. IC3’s static analysis is based on the foundation laid out by prior work on transaction chopping [4, 41]. In particular, it constructs a static conflict graph (SC-graph) in which a transaction is represented as a series of atomic pieces each making one or more database accesses. Two pieces of different transactions are connected if both access the same table and one of the accesses is a write. A cycle involving multiple pieces of some transaction (i.e. an SC-cycle) indicates a potential violation of serializability when interleaving the execution of those pieces involved in the SC-cycle. Transaction chopping [41] precludes any SC-cycle in a workload by merging pieces into a larger atomic unit. By contrast, IC3 permits most types of SC-cycles and relies on its runtime to render them harmless by constraining the execution of the corresponding pieces.

The runtime of IC3 only tracks and enforces direct dependencies; this is more efficient and scalable than explicitly tracking and enforcing transitive dependencies, as is done in [33]. Without the aid of static analysis, this simplified runtime does not expose much parallelism: once a transaction T becomes dependent on another T′, T has no choice but to wait for T′ to finish in order to prevent potential violations of transitive dependencies. Static analysis helps unlock the parallelism inherent in a workload. If there exists an SC-cycle connecting the next piece p of T to some piece p′ of the dependent transaction T′, then IC3 can shortcut the wait and execute p as soon as p′ has finished without waiting for the rest of T′. As most SC-cycles are among instances of the same type of transaction, this shortcut is very common and is crucial for IC3’s performance. Static analysis also helps IC3 ensure all tracked dependencies are enforceable at runtime. In particular, we identify a class of SC-cycles as
deadlock-prone in that they may cause deadlocks when IC3 tries to constrain piece execution. We remove the subset of SC-cycles that are deadlock-prone by combining pieces.

We contrast IC3’s approach to existing work [36, 2, 48, 46, 16] that also expose parallelism among contended transactions (see § 7 for a more complete discussion). Dependency-aware transaction memory (DATM) [36] and Ordered shared lock [2] permit safe interleaving should it arise at runtime and otherwise abort. As such aborts may cascade, IC3’s approach to pro-actively constraining execution for safe interleaving is more robust. Deterministic database [48, 46, 16] generates a dependency graph that deterministically orders transactions’ conflicting record access in accordance with transactions’ global arrival order. This fine-grained runtime technique avoids certain unnecessary constraints incurred by IC3 because static analysis cannot accurately predict actual runtime conflict. However, as the dependency graph is generated by one thread, deterministic database does not scale as well as IC3 when running on a large number of cores.

We have implemented IC3 in C++ using the codebase of Silo [49]. Evaluations on a 64-core machine using microbenchmarks and TPC-C [44] show that IC3 outperforms traditional 2PL and OCC under moderate to high amounts of contention. For the TPC-C benchmark configured with 1 warehouse, IC3 achieves 434K transactions/sec on 64 threads while the throughput of 2PL and OCC is under 50K transactions/sec. IC3 also scales better than deterministic lazy evaluation [16] and DATM [36] under high contention.

2. MOTIVATION AND APPROACH

In this section, we consider those parallel execution opportunities that are not exploited by 2PL and OCC. We discuss the challenges in enabling safe interleaving (§ 2.1) and explain IC3’s key ideas at a high level (§ 2.2).

2.1 Parallelism Opportunity and Challenges

When concurrent transactions make conflicting database access, much opportunity for parallelism is lost when using traditional concurrency control protocols like 2PL and OCC. Consider two transactions, T1 and T2, each of which reads and modifies records A and B, i.e. T1 = R1(A), W1(A), R1(B), W1(B) and T2 = R2(A), W2(A), R2(B), W2(B). Both 2PL and OCC effectively serialize the execution of T1 and T2. However, safe parallel execution of T1 and T2 exists, as shown by the example in Figure 1a. In this example, once T2 reads record A after T1’s write, T2’s subsequent read from record B will be constrained to occur after that of T1’s write to B, thereby ensuring serializability. Some existing protocols, such as Commit conflicting transactions [36] and Ordered sharing lock [2], augment OCC or 2PL to permit the safe interleaving in Figure 1a should it happen at runtime. However, if the actual interleaving happens to be unsafe (e.g. W1(A) → R2(A) but R2(B) → W1(B)), these protocols [36, 2] abort offending transactions, resulting in a cascading effect because interleaved data access have read uncommitted writes. To avoid costly cascading aborts, it is better to actively constrain the interleaving to guarantee safety instead of passively permitting interleaving that happens to be safe.

The example of Figure 1a suggests an intuitive, albeit naive, solution to exploit parallelism. Specifically, the database could track the dependencies among transactions as they make conflicting data accesses (including read-write or write-write conflicts). It would then ensure that tracked dependencies are not violated later (i.e. no dependency cycles arise) by delaying a transaction’s subsequence data access when necessary. For the example in Figure 1a, we would track T1 → T2 when T2 performs R2(A) after W1(A). Subsequently, the database would block R2(B) until W1(B) has finished in order to enforce the dependency T1 → T2. While this naive approach works for the example in Figure 1a, it does not work for general transactions, due to the following challenges.

Knowing which data access to enforce dependency on. In order to minimize unnecessary blocking, we need to know the series of records to be accessed by a transaction beforehand. In the example of Figure 1a, if T2 knows that its dependent transaction T1 will update record B (and T1 makes no other access to B), T2 only needs to wait for W1(B) to finish before performing its own access R2(B). If a transaction’s record access information is not known, T2 must wait for T1 to finish its execution in entirety, leaving no opportunities for interleaving.

Handling transitive dependencies. The naive approach is not correct for general transactions, because it does not handle transitive dependencies. To see why, let us consider the example in Figure 1b, in which T3 becomes dependent on T2 (i.e. T2 → T3) after T3 has written to record A after T2. During subsequent execution, T2 becomes dependent on another transaction T1, resulting in the transitive dependency T1 (→ T2) → T3. This transitive dependency needs to be enforced by delaying T3’s write to record C after that of T1. Techniques for tracking transitive dependencies exist in the distributed setting [33], but the required computation would impose much overhead when used in the multi-core setting.

Trapped dependencies are not always enforceable. The naive approach assumes that it is always possible to enforce tracked dependencies. While this assumption holds for some workloads, it is not the case for arbitrary real-world transaction workloads. For example, if T1 = W1(A), W1(B) and T2 = W2(B), W2(A), no safe interleaving of T1 and T2 exists. If the database permits both to execute concurrently, it is impossible to enforce the tracked dependencies later.

2.2 IC3’s Approach

To solve the challenges of safe parallel execution, one could rely solely on the runtime to analyze transactions’ record access information and to enforce the dependency among them. Deterministic databases [48, 46, 16] take such an approach.
proach. They generate a dependency graph that deterministically orders transactions’ conflicting record access in accordance with transactions’ global arrival order and enforces the dependency during execution, sometimes lazily [16]. While this approach can enforce dependency precisely, it does not scale well to a large number of cores, as the dependency analysis is performed by one thread and can become a performance bottleneck (§ 6). IC3 uses a different approach that augments runtime techniques with an offline static analysis of the workload. Below, we discuss the main ideas of IC3.

**Static analysis.** Most OLTP workloads consist of a mix of known transaction types. For each type of transaction, we typically know which table(s) the transaction reads or writes [4, 41, 33, 53]. Utilizing such information, static analysis chops each transaction into pieces, each of which makes an atomic data access. IC3’s runtime decides which pair of pieces needs to be constrained (e.g., if both make conflicting access to the same table) to enforce tracked dependencies. Moreover, static analysis can also determine when there may exist no safe interleaving at runtime and take preemptive steps to ensure all tracked dependencies are enforceable. The upside of static analysis is that it simplifies IC3’s runtime dependency tracking and enforcement. The downside is that it can cause the runtime to unnecessarily constrain certain safe interleaving. We discuss techniques to mitigate the performance cost of over-constraining (§ 7).

**Efficient runtime dependency tracking and enforcement.** IC3 tracks and enforces only direct dependencies which occur between two transactions when they make consecutive, conflicting access to the same record. By augmenting these direct dependencies with information from offline static analysis, IC3 can ensure all transitive dependencies are obeyed without explicitly tracking them.

To see how static analysis helps, let us consider a naive scheme that can obey all transitive dependencies while only tracking direct ones. In this scheme, every transaction \( T \) must wait for its directly dependent transactions to commit before \( T \) is allowed to commit or perform subsequent data access. Such conservative waiting ensures that all transitive dependencies are obeyed. For example, in Figure 1b, \( T_2 \) waits for its directly dependent transaction \( T_2 \) to commit before it proceeds to write to record \( C \). Because \( T_2 \) also waits for its directly dependent transaction \( T_1 \) to commit before \( T_2 \) commits, we are able to ensure \( T_1 \rightarrow T_2 \rightarrow T_3 \) for their corresponding access to record \( C \) without ever explicitly tracking and discovering the transitive dependency \( T_1 \rightarrow T_2 \rightarrow T_3 \).

The naive scheme kills the parallel execution opportunity shown in Figure 1a. For example, it will prevent the interleaved execution in Figure 1a, as \( T_2 \) waits for \( T_1 \) to commit before it is allowed to perform \( R_2(B) \). The key to making direct dependency enforcement work well is to leverage the static analysis of the workload. With the help of static analysis, we add two rules that bypass the default behavior of making \( T_2 \) wait for its direct dependency \( T_1 \) to commit. 1) if static analysis shows that no potential transitive dependencies may arise between \( T_1 \) and \( T_2 \) due to \( T_2 \)’s next data access, the runtime can safely let \( T_2 \) perform that access without blocking for \( T_1 \). 2) if static analysis shows that \( T_2 \)’s next data access might potentially conflict with some of \( T_1 \)’s later access, then \( T_2 \) only needs to wait for the corresponding access of \( T_1 \) to finish instead of waiting for the entirety of \( T_1 \) to finish and commit. The second rule applies to Figure 1a to allow its interleaving. Both rules are crucial for achieving good performance for practical workloads. We will elaborate the combined static analysis and runtime techniques in the next section (§ 3) and provide intuitions for their correctness.

### 3. Basic Design

This section describes the design of IC3. We discuss how IC3 analyzes static conflict information (§ 3.1), how its runtime utilizes this information to track and enforce dependency (§ 3.2), and lastly, how IC3 ensures that all tracked dependencies are enforceable (§ 3.3). We provide a proof sketch for correctness in § 3.5.

![Figure 2: SC-graph with two instances of the same transaction type.](image)

**3.1 Static Analysis.**

IC3 is an in-memory database with a one-shot transaction processing model, i.e., a transaction starts execution only when all its inputs are ready. Many existing databases have the same transaction model (e.g., H-store [42], Calvin [46, 48], Silo [49]). IC3’s current API provides transactions over sorted key/value tables whose primitives for data access are: Get("tableName", key), Put("tableName", key, value), Scan("tableName", keyRange)\(^1\).

For the basic design, we assume the transaction workload is static and known before the execution of any transaction. We relax this assumption and propose techniques to handle dynamic workloads and ad-hoc transactions in § 4.5. IC3 performs the static analysis by first constructing a static conflict graph (SC-graph), which is introduced by prior work on transaction chopping [4, 41]. In an SC-graph, each transaction is represented as a series of atomic pieces each making one or more data access. Pieces within a transaction are connected by a S(ibling)-edge. To construct a SC-graph for a given workload, we include two instances of each transaction type and connect two pieces belonging to different transactions with a C(conflict)-edge if they potentially conflict, i.e., two pieces access the same column of the same database table and one of which is a write access. IC3 analyzes user transaction code to decompose each transaction into pieces and to construct the resulting SC-graph (see details in § 5).

Suppose the example of Figure 1a corresponds to a workload consisting of the following one type of transaction:

\(^1\)Get/put/Scan also optionally take column names as parameters to restrict access to the specified subset of columns.
There is a danger for containing two instances of the same transaction, therefore, realizability at runtime. Specifically, if there exists an SC-commit before T control (OCC).

The execution of each transaction after all its pieces are finished. The atomicity and improve multi-core scaling, transactions by tracking and enforcing dependencies among direct dependencies at runtime. Without static analysis, a 3.2 Dependency Tracking and Enforcement

IC3 executes a transaction piece-by-piece and commits the transaction after all its pieces are finished. The atomicity of each piece is guaranteed using traditional concurrency control (OCC). IC3 ensures the serializability of multi-piece transactions by tracking and enforcing dependencies among concurrent transactions. To control performance overhead and improve multi-core scaling, IC3 only tracks and enforces direct dependencies at runtime. Without static analysis, a transaction T must wait for all its dependent transaction to commit before T can perform any subsequent data access, which precludes most scenarios for safe parallel execution. Static analysis helps IC3 avoid or shorten such costly wait in many circumstances.

Algorithm 1 shows how IC3 executes each piece and Algorithm 2 shows how IC3 executes and commits a multi-piece transaction. Together, they form the pseudo-code of IC3. IC3 uses several data structures to perform direct dependency tracking. First, each transaction T maintains a dependency queue, which contains the list of transactions that T is directly dependent on. Second, the database maintains an accessor list [36], one per record, which contains the set of not-yet-committed transactions that have either read or written this record.

### 3.2 Dependency Tracking and Enforcement

**Piece execution and commit.** The execution of each piece consists of three phases, as shown in Algorithm 1:

- **Wait Phase (lines 3-9).** Once a transaction T has become dependent on another transaction T', how long should T wait before executing its next piece p'? There are three cases, as determined by information from the static analysis. In the first case (lines 3-4), piece p does not have any C-edges and thus is not part of any SC-cycle involving T and T'. This means one cannot violate T' → T by executing p immediately, without constraints. In the second case, piece p is part of an SC-cycle that involves only T and its dependent transaction T'. In other words, p has a C-edge connecting to some piece p' in T'. For case-2, p only needs to wait for p' to finish (line 6-7). The third case is when neither case-1 or case-2 applies (line 8-9), then T has to wait for T' to finish all pieces and commit. The intuition for why p only needs to wait for p' in the second case is subtle; basically, if IC3 ensures that no (direct) dependencies are violated due to the SC-cycle involving only T and T', then no transitive dependencies are violated due to SC-cycles involving T, T' and some other transaction(s). To see why, we refer readers to the proofs (§3.5 and Appendix A). Note that case 2 is actually quite common; SC-cycles are most likely to occur among instances of the same transaction type (Figure 2a shows such an example). These SC-cycles make case 2 applicable.

- **Execution Phase (line 12).** In this phase, IC3 executes user code, and accesses database records. In the database, the value of a record reflects the write of the last committed transaction. In addition, each record also keeps a stashed value, which reflects the write of the last committed piece. A read of the record returns its stashed value, instead of the actual value. This ensures that a transaction T can read the writes of completed pieces in another transaction T' before T' commits. This allows for more interleavings that are not available to 2PL or OCC. All the writes of a piece are simply buffered locally.

- **Commit Phase (lines 15-25).** First, IC3 must check that p has executed atomically w.r.t. other concurrent pieces. We perform the validation according to OCC: IC3 grabs all locks on the piece’s readset and writset (line 15) and checks if any of its reads has been changed by other pieces (line 16, with details ignored). Second, we augment T's dependency queue

<table>
<thead>
<tr>
<th>Algorithm 1: RunPiece(p,T):</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input:</strong> p is a piece of transaction T</td>
</tr>
<tr>
<td><strong>// Wait Phase:</strong></td>
</tr>
<tr>
<td>2 if p does not have any C-edge // case-1</td>
</tr>
<tr>
<td>3 skip to execute phase</td>
</tr>
<tr>
<td>5 foreach T’ in T.dequeue:</td>
</tr>
<tr>
<td>6 if ∃ p’ of T’ and p has a C-edge with p’ // case-2</td>
</tr>
<tr>
<td>7 wait for p’ to commit</td>
</tr>
<tr>
<td>8 else // case-3</td>
</tr>
<tr>
<td>9 wait for T’ to commit</td>
</tr>
<tr>
<td><strong>// Execute Phase</strong></td>
</tr>
<tr>
<td>10 run user code to execute p</td>
</tr>
<tr>
<td><strong>// Commit Phase</strong></td>
</tr>
<tr>
<td>11 lock records in p’s read+writeset (using a sorted order)</td>
</tr>
<tr>
<td>12 validate p’s readset</td>
</tr>
<tr>
<td>14 foreach d in p.readset:</td>
</tr>
<tr>
<td>15 Tw ← last write tx in DB[d.key].acclist</td>
</tr>
<tr>
<td>16 T.dequeue += Tw</td>
</tr>
<tr>
<td>18 DB[d.key].acclist += (T,”reader”)</td>
</tr>
<tr>
<td>20 forw = d.val</td>
</tr>
<tr>
<td>28 return status //whether p has committed or aborted</td>
</tr>
</tbody>
</table>
Algorithm 2: RunTransaction(T):

1  // Execute Phase
2  foreach p in T:
3     RunPiece(p, T)
4     retry p if p is aborted (due to contention)
5
6  // Commit Phase
7  foreach T’ in T.depqueue:
8     wait for T’ to commit
9  foreach d in T.writeset:
10     DB[d.key].value = d.val
11     delete T from DB[d.key].acclist
12
13 return status /whether T has committed or aborted

(T.depqueue) due to any write-read relations that arise from p’s reads. Specifically, for each record in p’s readset, we append to T.depqueue the last writer according to the record’s accessor list (line 18-19). We then add T to the record’s accessor list.

Third, we update T.depqueue and the corresponding accessor lists based on p’s writeset. This update is similar to that done for p’s readset, except we must account for both read-write and write-write relations (lines 22-24). We then update the record’s stashed value with the write value (line 25).

Transaction commit. After all its pieces have finished, transaction T proceeds to commit. First, T must wait for all its dependent transactions to finish their commits (lines 7-8). This is crucial because we must ensure that T’s writes are not overwritten by transactions that are ordered before T in the serialization order. Then, it updates the value of the corresponding record in the database according to its writeset and removes itself from the record’s accessor list (lines 10-11). We note that, unlike 2PL or OCC, the commit phase does not require holding locks across its writeset. This is safe because 1) T explicitly waits for all transactions serialized before it to finish, and 2) conflicting transactions that are to be serialized after T wait for T’s writes explicitly during piece execution (lines 5-9).

Examples. Now we use the examples in Figure 1a and Figure 1b again to see how IC3 works. After merging the deadlock prone SC-cycles shown in Figure 2a into Figure 2b (details in § 3.3), we can enforce the interleaving as follows: after T1 has executed the piece RW1(A), IC3 appends T1 to record A’s accessor list. When T2’s first piece, RW2(A), finishes, IC3 checks A’s accessor list and puts T1 in T2’s dependency queue. When T2 tries to execute its next piece, RW2(B), it will have to wait for RW1(B) to finish because the two pieces are connected by a C-edge and RW1(B)’s transaction (T1) appears in T2’s dependency queue. In Figure 1b, T2 is in T3’s dependency queue when T3 is about to execute W3(C). Since, W3(C) has a C-edge with some transaction but not T2, it has to wait for T2 to finish all pieces and commit. As T2 can only commit after its dependent transaction T1 commits, W3(C) only executes after T1 has finished, thereby ensuring W1(C) → W3(C) and guaranteeing serializability.

3.3 Ensuring Tracked Dependencies are Enforceable

As we discussed earlier, tracked dependencies are not always enforceable at runtime for arbitrary workloads. When this happens, the basic IC3 algorithm encounters deadlocks as pieces enter some cyclic wait pattern. The traditional approach is to run a deadlock detection algorithm and abort all deadlocked transactions. Unlike 2PL, however, in the context of IC3, aborts have a cascading effect: not only must we abort all deadlocked transactions, we must also abort all transactions that have seen the writes of aborted transactions and so forth. A number of concurrency control protocols adopt such an approach [2, 36]. However, as we see in Sec 6, cascading aborts can be devastating for performance when the workload has a moderate amount of contention.

IC3 adopts a different approach to prevent deadlocks. Again, we leverage the static analysis to identify those pieces that can cause potential deadlocks. We combine those pieces (belonging to the same transaction) together into one larger atomic piece. This ensures all tracked dependencies at enforceable at runtime with no risks of deadlocks.

Given a SC-graph, what patterns suggest potential deadlocks? Consider the example in Figure 3a in which T1 accesses table Tab1 before Tab2 and T2 does the opposite. In the underlying SC-graph, this corresponds to an SC-cycle whose conflicting pieces access different tables in an inconsistent order. We refer to this SC-cycle as a deadlock-prone SC-cycle. Deadlock-prone SC-cycles indicate potential runtime deadlocks. Figure 3b gives an example execution that is deadlock: T1 reads record B before T2’s write to B (T1 → T2) while at the same time T2 reads record A before T2’s write to A (T2 → T1). This cyclic dependency will eventually manifest itself as a deadlock when T1 and T2 try to commit. In the example of Figure 3b, the deadlock appears earlier as T1 and T2 wait for each other before they attempt to modify record C. In addition to accessing different tables in an inconsistent order, an SC-cycle is also deadlock-prone if multiple conflicting pieces of a transaction access the same table.

To eliminate deadlock-prone SC-cycles, IC3 combines pieces into a larger atomic piece using the following algorithm. First, we add direction to each S-edge to reflect the chronological execution order of a transaction(Figure 4a). Second, we put all pieces connected by C-edges into a single vertex. The first two steps result in a directed graph whose edges are the original S-edges (Figure 4b). Third, we iteratively merge all the vertexes involved in the same directed cycle into one vertex until the graph is acyclic (Figure 4c).
Last, we combine those pieces of a merged vertex that belong to the same transaction into a single piece. Figure 4d shows the resulting SC-graph of Figure 3a after combining those pieces. Note that there are no longer deadlock-prone SC-cycles in Figure 4d, so IC3 is guaranteed to encounter no deadlocks when enforcing tracked dependencies.

### 3.4 Applicability of IC3

IC3 is not beneficial for all application workloads; it is only effective for contentious workloads that access multiple tables within a single transaction. For these workloads, the static analysis is likely to produce transactions containing multiple pieces, thereby allowing IC3 to exploit the parallelism opportunity overlooked by 2PL/OCC by interleaving the execution of conflicting pieces. For workloads that only access a single table within a transaction, IC3 does not provide any performance gains over traditional concurrency control such as 2PL or OCC. For example, if all transactions only do read and then modify a single database record, then static analysis merges the two accesses so that all transactions consist of a single (merged) piece. As a result, IC3 behaves identically to the traditional concurrency control it uses to ensure the atomicity of a piece.

Workloads that access multiple tables within a transaction are reasonably common in practice. For example, all transactions in the popular TPC-C and TPC-E benchmarks access multiple tables and thus contain multiple pieces (Section 6 gives more details). We have also manually analyzed the 14 most popular Ruby-on-Rails applications on GitHub and found most of them contain transactions accessing multiple tables (Appendix C).

### 3.5 Proof Sketch

Due to space limitations, we only give a proof sketch here. A more rigorous proof is included in the appendix. We are going to prove that IC3 always ensures serializability by only generating acyclic serialization graph.

In a proof by contradiction we assume there is a cycle in the serialization graph, denoted by $T_1 \rightarrow T_2 \rightarrow \ldots \rightarrow T_n \rightarrow T_1$. Treating each piece as a sub-transaction, the cycle can be expanded as $q_1 \rightarrow p_1 \rightarrow q_2 \rightarrow p_2 \rightarrow \ldots \rightarrow q_n \rightarrow p_n \rightarrow q_1$. Because we use OCC to protect the atomicity of each piece, the directed edge in the cycle reflects the chronological commit order of pieces, therefore there must be at least a pair of $q_i$ and $p_i$ such that they are not the same piece. Then this cycle corresponds to an SC-cycle in the SC-graph, which means no piece in the cycle can skip checking direct dependent transactions in Algorithm 1. Moreover, the cycle necessarily implies a deadlock at transaction commit time, so none of the transaction in the cycle can commit.

Consider a fragment $p_i \rightarrow q_i \rightarrow p_j$ in that cycle. For $p_i$, because it can neither skip the checking phase nor successfully wait for $q_i$ that has a C-edge connection to itself. Our static analysis ensures that this $T_i$ to commit ($T_i$ can never commit due to deadlock), $p_i$ can only execute after it waits for the commit of a piece $r_i$ in $T_i$ that has a C-edge connection to itself. Our static analysis ensures that this $r_i$ must be chronologically later than $p_i$, otherwise there will be a non-existent cycle $q_i \rightarrow p_j \rightarrow q_i$ in the SC-graph.

Using the above property, we can inductively “shrink” the cycle until there is no $q_i \rightarrow p_i$ in the cycle. Eventually after $m$ ($m < n$) times iteration, we will get a new cycle, represented as $q_1^m \rightarrow p_1^m \rightarrow q_2^m \rightarrow p_2^m \rightarrow \ldots \rightarrow q_n^m \rightarrow p_n^m \rightarrow q_1^m$, which necessarily implies a directed cycle in the SC-graph we have already eliminated, which is a contradiction to the result of static analysis. Therefore, a cycle in the serialization graph cannot exist, hence IC3’s scheduling is always serializable.

### 4. OPTIMIZATION AND EXTENSIONS

This section introduces several important performance optimizations and extends IC3 to support user-initiated aborts.

#### 4.1 Constraining Pieces Optimistically

(a) Static analysis may constrain piece execution unnecessarily. (b) Constrain piece optimistically by moving the waiting phase to be after piece execution and before its commit.

Figure 5: Constraining the interleaving optimistically to reduce false constraint

Static analysis can cause the runtime to unnecessarily constrain certain safe interleaving. Figure 5a shows an example runtime execution for the SC-graph in Figure 2. $T_1$ and $T_2$
write to the same record A in Tab1 but write to different records (B and B') in Tab2. However, under Algorithm 1, as T2 is dependent on T1 after both write to A, T1 can not execute W2(B') until W1(B) is finished. Such unnecessary constraining sacrifices parallelism.

As each piece is protected by OCC, we can constrain its execution optimistically to unlock more parallelism. The basic idea to constrain each piece’s commit phase instead of its execution phase. This can be done by reordering the wait phase and execution phase in Algorithm 1. For each piece, it first optimistically executes the piece without blocking (execute phase). Then, it waits according to the rules of the wait phase. Last, it will validate and commit the piece.

Figure 5b shows the allowed interleaving of the previous example with optimistic constraining. Unlike before, W2(B') can execute concurrently with W1(B). However, before T2 commits its second piece, it needs to wait for T1's second piece to finish committing. As the commit time of each piece is typically shorter than its execution time, this optimization reduces the size of critical section in which execution needs to be serialized.

### 4.2 Rendezvous Piece

![SC-graph](image)

Figure 6: The SC-graph involving two types of transactions. T2's P2 is the rendezvous piece of T1's P2 and T1's P2.

When executing a piece p in T that is potentially involved in any conflicts (Algorithm 1, line 5-9), IC3 needs to find T's dependent transaction T', and then either 1) wait for a piece in T' that may potentially cause conflicts with p to finish, or 2) wait for the entire T' to commit if no such pieces in T' exist. In the latter case, the wait could be expensive depending on how soon T' will commit. As an optimization to reduce this cost, we introduce a concept named rendezvous piece. For piece p in transaction T, its rendezvous piece in another transaction T' works as a promise that after this rendezvous piece finishes, T' can form no more conflicts with T involving p. More specifically, if we can find a later piece q in T (after p) and another piece r in T', such that q and r are connected by an C-edge in static analysis, r will be a rendezvous piece of p in T'. We then can use r to synchronize T with T'. In this case, IC3 can simply wait for r to finish before committing p, and doing so is sufficient to ensure no undesirable interference could ever happen.

During static analysis, after merging operations, IC3 looks for rendezvous pieces of every piece in other transaction types, and tags the information in the generated SC-graph. Afterwards, IC3 can leverage this information at runtime to cut down waiting time. As an example, Figure 6 shows an SC-graph with two types of transactions T1 and T2. The piece p2 of T1 has no C-edge directly connecting to T2, but a later piece p3 of T1 directly connects the p2 of T2. During static analysis, p2 is identified as the rendezvous piece of p2 of T1. Afterwards, during the execution, before T1 executes p2, it only needs to wait until T2 finishes p2, as shown in Figure 7.

### 4.3 Commutative Operation

Two write pieces commute if different execution orders produce the same database state. Therefore, it may seem unnecessary to constrain the interleaving of commutative pieces. However, this is not correct as write pieces do not commute with read operations that IC3 uses to generate a periodic consistent snapshot in the background. IC3 solves this issue by deferring the execution of commutative operation to the transaction commit phase. In our current implementation, users make commutativity explicitly by using a new data access interface, Update("tableName", key, value, op) where op is user-specified commutative accumulation function such as addition.

### 4.4 Handling User-initiated Aborts

So far, we have presented IC3 on the assumption that transactions are never aborted by users and thus can always be retried until they eventually succeed. We now explain how IC3 handles user-initiated aborts.

In IC3, when a transaction is aborted (by the user), all the transactions that depend on it must also be aborted. IC3 supports this cascading aborts by using an abort bit for each entry in the accessor list. When a transaction aborts, it unlinks its own entry from each accessor list that it has updated and sets the abort bit for all the entries appearing after itself. Before a transaction commits, it checks the abort bits of all its accessor list entries. If any of its entry has the abort bit, then the transaction aborts itself.

### 4.5 Online Analysis

So far, IC3 only handles static workloads where all the types of transactions are known beforehand. To accept a new type of transaction which is not known before, an intuitive way is pausing the system to update the SC-graph. But can we dynamically update the SC-graph without stopping the world?

Adding a transaction type results in a new SC-graph: if IC3 switches the SC-graph without pausing the system, concurrent transactions may use different SC-graphs. When IC3 updates the SC-graph, IC3 may merge conflicting pieces in the old SC-graph to avoid deadlock-prone SC-cycles.

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1IC3 runs read-only transactions separately from read-write transactions by using these snapshots, same as is done in Silo [49].

2Such deferring is always possible because commutative write pieces do not return any values used by later pieces. Otherwise they do not commute.
First, let us consider the simple case that no merging incurs. In this case, the C-edges in the new SC-graph is the superset of the C-edges in the old SC-graph; for the transactions in the old workloads, their instances using the new SC-graph can concurrently execute with the ones using the old SC-graph. As a result, IC3 can process the transactions in old workload until all worker threads use the new SC-graph.

Figure 8 shows an example: the static workload has one transaction (T1) which first updates Tab1 then reads Tab2. A new transaction (T2), issued by user at runtime, updates both tables’ records. To process T2, IC3 needs to update the SC-graph from Figure 8a to Figure 8b. With the above strategy, IC3 should only process T1 during the update. Figure 8c shows a possible execution: as IC3 updates SC-graph when transactions are running, concurrent transactions may use different SC-graphs. But the system is still consistent, because both SC-graphs ensure the atomicity of the first piece.

Now, let us consider another case that the update of the SC-graph requires merging the conflicting pieces. For this case, the above strategy is insufficient to ensure the consistency. Figure 9 gives an example. The new transaction (T2) accesses the tables in the opposite order with the transactions (T1) in the old workload. To avoid deadlock-prone cycle, IC3 needs to merge the conflicting pieces in Figure 9a, and generate the new SC-graph (Figure 9b). Figure 9c gives a possible execution of two instances of T1 at runtime. T1 using the old SC-graph commits the updates separately; T1’ using new SC-graph commits the update in a single piece, and does not enforce the interleaving with T2. As a result, this interleaving introduces a cyclic dependency.

To ensure consistency, IC3 extends the above strategy by introducing transitional SC-graph which is a combination of both the old and new SC-graphs; transactions in the old workload should use the transitional SC-graph until all worker threads begin to use the new SC-graph. The transitional SC-graph allows nested conflicting piece: a conflicting piece includes multiple sub-pieces; sub-pieces from different transactions can be connected with C-edges. The conflicting pieces, which are from the old SC-graph and merged into a single piece, become the sub-pieces in the transitional SC-graph. At runtime, IC3 uses the transitional SC-graph to enforce the sub-piece’s execution and tracks the dependency at the end of each sub-piece. However, IC3 only validates the correctness and commits the updates when the outer piece finishes. Enforcing the sub-piece’s execution ensures the serial order of transactions using transitional SC-graph and old SC-graph. At the same time, as the granularity of validation and commit is the entire piece, IC3 is capable to use Algorithm 1 to ensure the serial order of transactions using transitional SC-graph and the new SC-graph.

Figure 10 is the transitional SC-graph of Figure 9a and Figure 9b. IC3 merges the conflicting pieces in Figure 9a into single piece in Figure 9b, thus each piece in Figure 10 has two sub-pieces accordingly. Figure 11 shows how IC3 enforces transaction’s execution with the transitional SC-graph. IC3 tracks the dependency with T1 after executing the first sub-piece of T1’, then it enforces the second sub-piece’s execution to ensure the consistency. However, IC3 only commits the updates of T1’ at the end of entire piece.

Removing a transaction type also leads to the update of the SC-graph. As removing a transaction type may exclude C-edges from the SC-graph, then some conflicting pieces can be split into multiple pieces. Let us first consider the simple case that no splitting happens, similarly, it is safe to execute the remaining transactions concurrently, as the C-edges in new SC-graph is the subset of the C-edges in old SC-graph. Second, if removing transaction requires splitting some pieces, the SC-graph generated is the old SC-graph when IC3 adds this transaction. As a result, it is safe to use transitional SC-graph to ensure the consistency when updating the SC-graph requires split.

5. IMPLEMENTATION

We have built the IC3 runtime in C++ and implemented the static analyzer using a Python script in a separate pre-processing stage. Our C++ implementation is based on the codebase of Silo [49], a high-performance in-memory database. Silo implements OCC on top of Masstree [31], a concurrent B-tree like data structure. We change the concurrency control protocol to IC3 and reuses Silo’s implementation to support snapshot, durability, and garbage collection.

5.1 Pre-processing and Static Analysis

The static analysis is done by a Python script in the pre-processing stage, before the system is to execute any transaction. Thus, the overhead of static analysis does not affect IC3’s runtime performance. The analyzer parses the stored procedure code (in C++) to determine which table access belongs to which transaction piece and to construct the corresponding SC-graph among transactions. The granularity of the analysis is at the table and column level, i.e. two pieces are connected by a C-edge if both access the same column in the same table and one of the access is a write.

To simplify code analysis, we restrict user code to specify the names of tables and columns accessed via the Get/Put/Scan API as constants. Thus, the analyzer can extract each table access simply, label accesses as individual pieces, and determine which pieces are connected via C-edges. If a table access occurs within an if-else statement, the analyzer represents the corresponding transaction as two separate types (one corresponding to each branch) in the SC-graph. For table accesses within a for-loop, they are grouped into one piece (it is possible to split loops using known compiler tech-
After the analyzer obtains the raw SC-graph by parsing stored procedure code, it applies the algorithm in § 3.3 to merge some pieces if necessary. For each table access, the final output of the analyzer contains its corresponding piece identifier and its C-edge information (i.e., the identifiers for those pieces with a C-edge to it). The IC3 runtime loads the C-edge information based on the analyzer’s output prior to execution. We currently rely on manual annotation to associate the piece identifier with each table access. If a piece contains more than one table access, users must enclose those access within a pair of begin_piece and end_piece statements. As a result of the pre-processing, the IC3 runtime has sufficient information to implement line 3 and 6 in Algorithm 1.

5.2 Runtime Implementation

IC3 uses a tuple to represent each table record and its meta-data. Among others, the meta-data includes the record’s accessor list (implemented as a linked list), the stashed value and a version number for ensuring piece atomicity using OCC.

IC3 uses n worker threads to execute transactions, where n is the number of cores in the machine. We implement MCS lock [32], a type of spinlock that scales well to many cores [9]. Each tuple is associated with a separate MCS lock which protects the atomicity of operations on the tuple.

Each running transaction is associated with a data structure, referred to as its context, that holds information such as the transaction ID, its dependency queue, the current piece being executed, and the status of the transaction. The context data structure has a fixed size and is reused for a new transaction.

**Piece Execution and Commit** (Lines 11–26, Algorithm 1). IC3 uses OCC to ensure the atomicity of each piece. During piece execution, IC3 buffers writes in the piece’s write-set and copies the version number of each record being read in the piece’s read-set. To commit piece p, IC3 first acquires the MCS locks for all tuples corresponding to p’s read- and write-set. Then, IC3 checks whether the version numbers in the read-set differ from those currently stored in the tuples. Suppose validation succeeds for piece p of transaction T. Then, for each record accessed by p, IC3 adds the piece’s transaction ID (T) to the tuple’s accessor list, updates the tuple’s stash value if the corresponding access is a write, and copies the transaction ID of the last conflicting entry in the tuple’s accessor list to T’s dependency queue (lines 17–25, Algorithm 1). Last, IC3 releases the MCS locks.

**Piece wait** (lines 2–9, Algorithm 1). There are three cases for how long a piece should wait before execution. The IC3 runtime can determine which case applies to piece p by examining p’s C-edge information. This information is calculated by the static analyzer during pre-processing and loaded in the runtime’s memory prior to execution.

By default, the worker thread waits by spinning. If piece p needs to wait for its dependent transaction T’ to commit (line 8, Algorithm 1), the worker thread continuously reads several pieces of information in T’ s context and checks 1) whether the status of T’ becomes “committed” 2) whether the transaction ID stored in the context of T’ has been changed; this occurs when T’ finishes and its context data structure is re-used by other transactions. If piece p needs to wait for a specific piece p’ in T’ to commit (line 6–7, Algorithm 1), the worker thread also additionally spins to check whether the current piece being executed by T’ is after p’. If so, piece p can proceed to execution without waiting for T’ to commit. Each read of the spin variables (i.e., transaction status, transaction ID, or current piece identifier) is done without locking because the underlying memory instructions involving no more than 8-bytes are atomic. IC3 adds a memory barrier whenever a spin variable is modified.

Apart from the default spin-wait strategy, we also explored a suspend-wait strategy in which a worker thread suspends a blocked transaction to execute others. The implementation of suspend-wait is done using C++ co-routines. If a piece needs to wait, the worker thread puts the current transaction in the thread’s pending queue and switches
to execute other runnable transactions (that the worker has previously suspended) or a new one. We implement the pending queue as a lock-free queue so that suspending a transaction will not block other worker threads.

We choose spin-wait as the default strategy because it leads to better performance in our experiments. For example, when running TPC-C new-order transactions with 64 worker threads accessing one warehouse, the spin-wait strategy has 2.14X throughput than the suspend-wait strategy (340K TPS vs. 155K TPS). This is because the overhead of the context switching and lock-free queue manipulation out-weights the overhead of spin-wait for short waits which are the case in TPC-C. Suspend-wait may be beneficial for workloads involving long waits.

5.3 Secondary Index Implementation

IC3 supports secondary indexes similarly as Silo [49] and Calvin [16]. Each secondary index corresponds to a separate table that maps secondary keys to the records’ primary keys. When modifying a table with a secondary index, the user transaction needs to explicitly update the record in the secondary index table indexed by the attribute.

6. EVALUATION

This section measures the performance and scalability of IC3. We first compare IC3 with traditional approaches (OCC and 2PL) under varying levels of contention. We use the OCC implementation of Silo [49]. We implement 2PL ourselves by associating each record with a scalable read-write lock. Our implementation of 2PL eliminates the chance of deadlock by sorting the locks in a consistent order. Then, we present the comparison with other alternatives with contended workloads. Last, we analyze the effect of different optimization methods.

6.1 Experiment Setup

Hardware. Our experiments are conducted on a 64-core AMD machine with 8 NUMA nodes. Each node has 8 cores (Opteron-6474). Each core has a private 16KB L1 cache and every two cores share a 2MB L2 cache. Each NUMA node has a 8MB L3 cache and 16GB local memory (128GB in total). The machine runs a 64-bit 4.0.5 Linux kernel.

Workloads and metrics. This evaluation includes three benchmarks, a micro benchmark which does simple random updates, the widely-used TPC-C [44] benchmark and a more complex TPC-E benchmark [45]. We will primarily use TPC-C to demonstrate the performance measurements of IC3 and the alternatives.

For each benchmark, we first evaluate the performance of IC3 with increasing contention rate. Then, we study system scalability under high contention. Further more, we also evaluate the online analysis mechanism and the amount of transitive dependencies at runtime. Last, we study if the real-world applications can potentially benefit from IC3.

Throughput is the primary metric in this evaluation. Every trial is run for a fixed duration (i.e. 30 seconds) to record a sustainable throughput. We manually pin each thread to a single core, and ensure that the number of worker threads equals to the number of cores. When disk logging is enabled, IC3 can only scale up to 16 cores due to the limitation of I/O bandwidth (two disks) in our test machine; thus, we disable logging by default.

6.2 Microbenchmark

We begin our evaluation with a simple microbenchmark involving one type of transaction. Each transaction executes a controllable number of pieces and each different piece accesses a different table. Each piece randomly updates 4 distinct records from the same table. Each piece is protected using 2PL. To avoid deadlock, the records are sorted when each piece starts. Each table has 1M records. Each record has a 100-byte value and a 64-bit primary key.

For each piece, the contention rate is controlled by varying the selection scope of its first operation between 10 and 1M. When a piece selects a record out of 10, it has 10% contention rate. Figure 12(a) shows the performance of workloads with each transaction with moderate size (10 pieces). When the selecting scope is 1,000,000 (contention rate is nearly 0), IC3’s throughput is about 15% lower than that of 2PL and OCC (167K vs. 196K vs. 189K TPS). This extra cost is mainly from manipulating the linked list for dependency tracking. When the contention rate increases to 1% with 100 records to select from, the performance of IC3 remains unchanged (167K TPS), while 2PL and OCC have 23% and 52% performance slowdown accordingly (149K vs. 196K and 93K vs.189K TPS). OCC’s performance drops greater than 2PL because the 1% contention rate among pieces can cause 65% transaction aborts in OCC. When the contention rate is greater than 1%, IC3’s performance degrades more gracefully. With 10% contention rate, IC3 has 45% performance loss, (90K vs. 167K TPS), while the throughput of 2PL and OCC drops 86% and 90% respectively (27K vs. 196K and 18K vs. 189K TPS).

We also evaluate IC3’s performance speedup with concurrent execution under highly contended workload. Figure 12(b) shows the throughput improvement under highly contended workload (10% abort rate) with an increasing number of worker threads. The throughput of IC3 keeps growing to 64 worker threads, while 2PL and OCC can only scale to 16 cores. With 64 worker threads, IC3 outperforms its single thread version by 9X (90K vs. 9.9K TPS), while 2PL gets 3X speedup (29K vs. 10K TPS) and OCC only gets 1.5X speedup (16K vs. 10K TPS).

We also analyze the effect of transaction length on performance. For the workload with short transactions having only 2 pieces, it has 70% performance degradation when the contention rate is increased from 0 to 10% (1350K vs. 410K TPS). Under high contention level with 10% abort rate, IC3 achieves 10X speedup with 62 worker threads compared with the performance with only 1 thread (43K TPS vs. 410K TPS). For the workload with the longer transaction containing 64 pieces, it has 37% performance degradation when the contention rate is increased from 0 to 10% (23K vs. 15K TPS). For highly contended workloads with 10% abort rate, IC3 achieves 15X speedup (1K vs. 15K TPS) over a single thread. IC3 can improve the workloads’ performance for workload under high contention regardless of the number of pieces in the transaction. However, IC3 achieves more speedup for longer transactions.

6.3 TPC-C

In the TPC-C benchmark, three out of five transactions are read-write transactions that are included in the static analysis and processed by IC3’s main protocol. Figure 14 shows the SC-graph. The other two are read-only transactions and are supported by the same snapshot mechanism in
Silo [49]. In TPC-C, we decrease the number of warehouses from 64 to 1 to increase the contention rate. When there are 64 warehouses, each worker thread is assigned with a local warehouse, so each thread will make most of the orders using its local warehouse. Only a small fraction of transactions will access remote warehouses. When there is only one warehouse, all worker threads make orders from this global shared warehouse, suggesting a high contention rate.

Under high contention rate, IC3 performs much better than 2PL and OCC. As the number of warehouses decreases to 1, the throughput of IC3 only drops by 32% (435K vs. 643K TPS). In contrast, the performance of 2PL and OCC degrades dramatically when the total number of warehouses is less than 16. OCC suffers 64% throughput degradation at 8 warehouses with 63% abort rate. When there are only 4 or less warehouses, OCC has only a few hundreds of TPS (e.g., 341 TPS for 4 warehouses) as the abort rate is more than 99%. For 2PL, its performance degrades 59% with 8 warehouses and 93% with 1 warehouse.

Figure 13(b) shows the scalability of IC3 when sharing a global warehouse. IC3 can scale to 64 threads with 22X speedup over one thread (435K vs. 19K TPS). However, the performance is only improved by 27% from 32 cores to 64 cores. The major reason is that all payment transactions update the same warehouse record and contend on the same cache line. This can be further optimized by distributing the record, such as phase reconciliation [34]. One may find that IC3’s scalability with TPC-C is better than in our microbenchmarks. This is because not all pieces’ execution in TPC-C will be constraint (i.e., commutative pieces, read-only pieces and read-only transactions). Such pieces can be concurrently executed with the conflicting pieces, which increases the concurrency. Both OCC and 2PL can only scale to 4 cores, with 49K TPS and 43K TPS accordingly. After 4 threads, the performance of 2PL does not change notably, but the performance of OCC degrades drastically because conflicting transactions are frequently aborted.

6.4 Comparison with Alternative Approaches

This subsection continues to use TPC-C to compare IC3 with four important alternative approaches under highly contended workloads.

Transaction chopping: We first apply transaction chopping [41] to TPC-C and merge pieces to eliminate SC-cycles. Each merged piece is protected using 2PL or OCC. We also exclude C-edges between any commutative operations. Figure 15a shows the performance when all worker threads share a global warehouse. Transaction chopping with 2PL only gets marginal benefit compared to 2PL: it cannot scale beyond 8 threads, as most operations of new-order and delivery transaction need to be merged. After 8 threads, IC3 scales better than transaction chopping and its performance is 4X under 64 threads (435K vs. 100K TPS). When using OCC to protect the merged piece (Chopping-OCC in Figure 15a), it has similar performance as chopping-2PL when the number of threads is less than 8. With 8 worker threads, its performance is worse than chopping-2PL (75K vs. 99K TPS) due to piece aborts and retries. As con-

Figure 12: Microbenchmark

Figure 13: TPC-C Benchmark

Figure 14: The SC-graph of 3 Read Write Transactions in TPC-C
tension further increases with more than 8 worker threads, the throughput of chopping-OCC degrades significantly.

Deterministic database with lazy evaluation: We also compare against the deterministic database with lazy evaluation [16]. Deterministic database divides each transaction into two phases: new phase and later phase. The system needs to execute all transactions’ new phases sequentially to generate a global serialized order and analyze the dependency of their later phases. Then the later phases can be executed deterministically according to the dependency graph generated in the new phase. Execute high conflicting operations in the new phase can improve the temporal locality and increase the concurrency of later phases.

We use the implementation released with the paper. Figure 15b shows the scaling performance of deterministic database under one global TPC-C warehouse. We use one extra worker thread to run all the transaction’s now phases and use the same number of worker threads with IC3 to run the later phase concurrently. We tune the setting such that the number of transaction can be buffered in the new phase and choose the threshold (i.e., 100) with the highest throughput. We issue 1M transactions to the system for processing to get the throughput result.

With a single thread, lazy evaluation is better than IC3 (38K vs. 19K TPS). This is because: 1) One extra thread is used to execute all highly contended operations which parallelise the execution and achieve good cache locality; 2) Some operations are deferred and even never executed; 3) Different code base for both benchmark and system implementation also contribute the performance difference. When the size of transaction batch is 100, their system achieves highest throughput under 16 worker threads (318K). However, its performance degrades after 16 threads and IC3 can even achieve better performance after 32 threads.

Using OCC to ensure serializability across pieces. We evaluate another strategy, called Nested OCC, that chops each transaction into pieces and uses OCC to ensure atomicity within and across pieces. At the end of each piece, it validates the records read by the piece and retries the piece if validation fails. At the end of the transaction, it validates the records read in all pieces. Similar to IC3, commutative operations are not included in the conflicting pieces.

Figure 15c shows performance of Nested OCC for TPC-C under high contention. Since the contention within a piece only causes the re-execution of the piece instead of the whole transaction, Nested OCC has slower abort rate than OCC with 4 worker threads (15% vs. 42%). As a result, its performance is 62% better than OCC and 30% better than IC3 with 4 worker threads. With an increasing number of threads, the throughput of Nested OCC drops significantly like OCC due to dramatically increased abort rate. With 64 worker threads, its abort rate is 98% which is the same as OCC. This is because, with more worker threads, pieces are more likely to interleave in a non-serializable manner, thereby causing aborts. By contrast, as IC3 enforces the execution order among the concurrent conflicting pieces, thereby avoiding aborts and achieving good scalability with many threads.

Dependency-aware transactional memory (DATM) [36] is the last compared algorithm. Under DATM, a transaction can observe the update of conflicting uncommitted transactions. All conflicting transactions will commit successfully, if the interleaving of the conflicting operations are safe. However, this method also allows unsafe interleaving which will incur cascading abort.

We port DATM by modifying OCC to be dependency aware. However, since original algorithm targets software transaction memory, we make slightly optimized choices for our implementation of DATM. Each record keeps an accessor list to track the accessed transactions. However, our implementation only keeps the memory pointers of the received or written value. We can check if a read is stale by checking the memory pointer, which saves the cost from memory compare. Like [36], we use timeout for deadlock prevention.

As DATM is designed for software transactional memory, it doesn’t support range query and deletion. Thus we only evaluate it with new-order transactions in TPC-C under high contention: all workers share the same warehouse. After profiling with different timeout thresholds, we found the best performance can be achieved when the timeout threshold is set to 0.45 ms on our 2.2GHz CPU. Figure 15d shows the performance. We also include OCC and 2PL as reference. Since DATM can manage dependency among uncommitted conflicting transactions, DATM scales to 8 threads with 125K TPS, which is better than all others. With 8 threads, IC3 gets 95K TPS while 2PL and OCC achieve 105K TPS and 1K TPS accordingly. However, the performance of DATM degrades with the increasing number of cores, mainly due to more cascading aborts and an increased cost per abort. With 16 threads, the abort rate is 81% and the abort rate increases to 99% (with 92% for observing an aborted transaction’s update).

6.5 Factor Analysis

To understand the overhead and the benefit of each optimization, we show an analysis with TPC-C (Figure 16) when all threads share one warehouse (high contention).
Figure 16: Analysis the effect of each optimization method. Optimization is applied from bottom to top for each group.

Figure 16a shows the analysis result. “Basic” is the performance of the basic algorithm (§ 3.2). Enforcing the interleaving optimistically (“+Optimistic Constraint”) improves the performance by 32% with 64 threads (224K vs. 296K TPS). The performance is improved by 40% (296K vs. 435K) if we run the commutative operations without constraints.

Optimization with rendezvous piece.

We introduce a new transaction (last-order-status) to demonstrate the performance effect of the rendezvous piece optimization. This transaction checks the status of latest order made by new-order transaction. It reads the next_o_id from a random district. Then, it uses this order id to read records from tables of ORDER and ORDERLINE. We configure a benchmark with 50% new-order and 50% last-order-status. Figure 17 shows the according SC-graph. Figure 16b shows the evaluation result. Compared with the basic protocol, the performance can be improved by 23% with rendezvous piece with 64 cores (289K vs. 235K TPS).

6.6 Impact of Durability

This section shows the impact of durability on latency and throughput. Due to the limitation of I/O bandwidth in our test machine (two hard disks), we evaluate the systems with at most 16 cores. We choose TPC-C benchmark and still use the low and high contention configurations.

Figure 18a shows the impact of supporting durability on throughput under low contention. All three systems can scale to 16 cores with durability support. The durability introduces around 5.50% overhead for IC3.

Figure 18b shows the impact on throughput under high contention. For OCC, the transaction abort becomes the performance killer and both versions of OCC cannot scale beyond 4 threads. In contrast, durability has insignificant influence on the throughput of IC3 and 2PL.

Figure 19a and Figure 19b illustrate the latency of OCC, 2PL and IC3 with durability support. The latency of a transaction is evaluated by measuring the time from which a transaction is issued to the time it is durable on the disks. The latency of Silo is a little different from their original paper [49], because there was a bug in their code and that is now fixed in the current version. Under high contention, the latency of OCC increases notably due to frequent aborts and retries. Like the throughput, the latency of IC3 is stable with the increasing number of cores.

6.7 Impact of User Initiated Abort

In IC3, if a transaction T is explicitly aborted by user code, all transactions that have read the stash values of T’s committed pieces should abort. We evaluate the impact of cascading aborts (caused by user initiated aborts) using same micro-benchmark in § 6.2. In the experiments, each transaction aborts after committing a piece with varied probabilities.

Figure 20(a) shows the throughput of IC3 under different user abort rates with 64 worker threads. As expected, the throughput decreases as user abort rate increases. For workloads with no conflict, the performance drop is only due to user aborts. With 10% user initiated abort rate, IC3 has around 4% performance degradation (102K vs. 89K TPS). If the workload has 5% conflict rate, 10% user initiated abort rate causes 20% performance loss. This is because the cascading aborts result in 37% transaction abort rate. When the conflict rate increases to 10%, 10% user aborts causes 30% performance loss (105K vs. 75K TPS), as cascading abort causes 55% transaction abort rate.

Figure 20(b) shows the throughput of IC3 as the number of worker threads increases for workloads with 10% conflict rate. When the number of worker threads is less than 8, IC3 has similar throughputs for different user abort rates. This is
because there is little cascading abort caused by user aborts: 10% user abort only incurs 2% cascading abort. Beyond 8 worker threads, higher user initiated abort rate leads to more throughput decrease due to the cascading abort. With 64 worker threads, 5% user abort rate incurs 37% transaction abort rate (resulting in 15% less throughput) while 10% user abort rate incurs 55% transaction abort rate (resulting in 30% less throughput).

### 6.8 TPC-E Benchmark

We also implement the TPC-E benchmark to evaluate the performance of IC3 in a more complex OLTP setting. In TPC-E, 4 out of 10 transactions are read-write transactions and need to be included in the static analysis. We only compare IC3 with OCC in the TPC-E evaluation because our implementation of 2PL does not do deadlock detection. Unlike TPC-C, we cannot guarantee user transactions access records in a common order, therefore, we cannot use 2PL without deadlock detection. We evaluate IC3 and OCC using read-write transactions and vary the contention rate by changing the access range in the security table.

Figure 21(a) shows the performance of 64 worker threads with the increasing contention rate. When the conflict rate increases to 70% (this occurs when all worker threads share a security record), IC3 only has 14% slowdown compared with no contention. In contrast, the performance of OCC degrades dramatically from 14K TPS to 2K TPS due to high abort rate (95%). Figure 21(b) shows the scalability of these two protocols with 70% conflict rate, the performance of IC3 increases with the number of worker threads from 8K TPS to 123K TPS and achieves the highest throughput with 32 worker threads, while the performance of OCC degrades after 8 worker threads. IC3 does not scale beyond 32 threads; this is likely because we did not implement the initialization of table data on multiple NUMA nodes due to time constraints (we implemented this optimization for all other benchmarks). As a result, all memory accesses end up on a single NUMA node, limiting scalability.

### 6.9 Online Analysis

To evaluate the effect of online analysis, we use the TPC-C benchmark with 64 worker threads. All worker threads share a single warehouse. At the beginning, we only run three types of transactions: New-Order, Order-Status and Stock-Level. Then, we add Payment transaction at the 10 seconds and Delivery transaction at the 20 seconds. To compare the performance of different schemes, we also implement other two offline analysis schemes. The first one is analyzing all the transactions before the system starts (Analysis at beginning). The second one is stopping the system when updating the SC-graph (Stop the world). Figure 22 shows the comparison result, we calculate the throughput per 0.1 seconds. X-axis is the time line, while Y-axis is the throughput. At beginning, “Analysis at beginning” is worse than the other two schemes. This is because some commutative pieces of new-order becomes conflicting pieces after involving Payment and Delivery transactions. When add payment/delivery transactions, the “stop the world” scheme’s performance degrades seriously. This is because we set a barrier to stop the system when update the SC-graph. However, dynamic update the SC-graph with our algorithm can keep the performance when update the SC-graph.

### 6.10 Transitive Dependencies

We use the new-order transaction to study the relationship between the amount of transitive dependencies and the number of cores. All transactions access 10 DISTRICT tables under one warehouse and a single STOCK table. At runtime, we record each transaction’s direct dependent transactions with an in-memory log; we analyze the transitive dependencies with the log after the program finishes. We calculate the average number of direct/transitive dependencies per transaction. Table Table 1 shows the analysis result. For the direct transitive dependency, its amount increases with the number of cores; with 64 cores, on average, each transaction directly depends on 6 transactions as they access the same DISTRICT. For the transitive dependencies, its amount increases linearly with the number of cores. With 32 cores, each transaction transitively depends on 1 transactions on average; but, with 64 cores, the number increases to 9. However, at runtime, each transaction only needs to tracks 1 transaction (w.r.t., last direct dependent transactions) on average.

### 6.11 Web Applications Study

To determine if real-world applications can potentially benefit from IC3, we analyze 14 most popular ruby-on-rails web applications on GitHub according to their GitHub stars.
### 7. RELATED WORK

One purpose of concurrency control is constraining inter-leavings among transactions to preserve some serial order, using various approaches like two-phase locking [1, 26, 8, 14], timestamp ordering [10, 5, 29] and commit ordering [37, 38].

**Table 1**: The average number of direct/transitive dependencies with TPCC neworder transaction.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Direct Dependencies</th>
<th>Transitive Dependencies</th>
</tr>
</thead>
<tbody>
<tr>
<td>Canvas LMS</td>
<td>Education</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Discourse</td>
<td>Community discussion</td>
<td>0.2</td>
<td>0.002</td>
</tr>
<tr>
<td>Spree</td>
<td>eCommerce</td>
<td>0.6</td>
<td>0.018</td>
</tr>
<tr>
<td>Diaspora</td>
<td>Social network</td>
<td>0.8</td>
<td>0.13</td>
</tr>
<tr>
<td>Redmine</td>
<td>Project management</td>
<td>2.8</td>
<td>0.97</td>
</tr>
<tr>
<td>OneBody</td>
<td>Church portal</td>
<td>6.3</td>
<td>9.5</td>
</tr>
<tr>
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<td>Social networking</td>
<td>16,019</td>
<td>1,560</td>
</tr>
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<td>Blogging</td>
<td></td>
<td>1,117</td>
</tr>
<tr>
<td>Browser CMS</td>
<td>Content management</td>
<td></td>
<td>1,229</td>
</tr>
<tr>
<td>GitLab</td>
<td>Code management</td>
<td></td>
<td>1,200</td>
</tr>
<tr>
<td>Inosshi</td>
<td>Social network</td>
<td></td>
<td>1,147</td>
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<tr>
<td>Teambox</td>
<td>Project management</td>
<td></td>
<td>1,173</td>
</tr>
<tr>
<td>Radiant</td>
<td>Content management</td>
<td></td>
<td>1,609</td>
</tr>
<tr>
<td>GitLab CI</td>
<td>Continuous integration</td>
<td></td>
<td>1,420</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Total</th>
<th>Mul-Tables</th>
<th>D-SC</th>
<th>IC3-SC</th>
<th>GitHub Stars</th>
</tr>
</thead>
<tbody>
<tr>
<td>Canvas LMS</td>
<td>Education</td>
<td>46</td>
<td>30</td>
<td>12</td>
<td>20</td>
<td>1,542</td>
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<td>36</td>
<td>28</td>
<td>3</td>
<td>26</td>
<td>16,019</td>
</tr>
<tr>
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<td>3</td>
<td>-</td>
<td>3</td>
<td>6,802</td>
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<tr>
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<td>10,331</td>
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<tr>
<td>Redmine</td>
<td>Project management</td>
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<td>8</td>
<td>-</td>
<td>8</td>
<td>1,560</td>
</tr>
<tr>
<td>OneBody</td>
<td>Church portal</td>
<td>2</td>
<td>1</td>
<td>-</td>
<td>1</td>
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<tr>
<td>Community Engine</td>
<td>Social networking</td>
<td>2</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1,117</td>
</tr>
<tr>
<td>Publify</td>
<td>Blogging</td>
<td>5</td>
<td>1</td>
<td>-</td>
<td>1</td>
<td>1,497</td>
</tr>
<tr>
<td>Browser CMS</td>
<td>Content management</td>
<td>4</td>
<td>3</td>
<td>-</td>
<td>3</td>
<td>1,200</td>
</tr>
<tr>
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<td>8</td>
<td>5</td>
<td>-</td>
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<td>16,523</td>
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<tr>
<td>Inosshi</td>
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<td>-</td>
<td>-</td>
<td>1,585</td>
</tr>
<tr>
<td>Teambox</td>
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<td>4</td>
<td>1</td>
<td>-</td>
<td>1</td>
<td>1,873</td>
</tr>
<tr>
<td>Radiant</td>
<td>Content management</td>
<td>2</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1,609</td>
</tr>
<tr>
<td>GitLab CI</td>
<td>Continuous integration</td>
<td>2</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1,420</td>
</tr>
</tbody>
</table>

**Table 2**: Ruby-on-rails applications used in analysis (Total: the total number of user defined transactions in the workload.

**Mul-Tables**: the number of transactions which access more than one table. D-SC: The number of transactions which are involved in a deadlock prone SC-Cycle. IC3-SC: The number of transactions which have more than one conflicting piece and are involved in a compatible SC-Cycle). GitHub starts record the number of stars on GitHub as of October 2015.

As most applications use active record interface instead of SQL, thus we only analyze the user defined transactions manually. Table 2 shows the analysis result. 11 out of 14 applications have transaction types that access more than one table only four of them have extremely simple transactions which access only one table and can potentially benefit from IC3. As a further analysis, we construct their SC-graph and identify the deadlock prone SC-cycles. Results show that all of the 11 applications can take the advantage of IC3. This is because their SC-graphs have IC3 compatible SC-cycles, and therefore IC3 can ensure the serializability by enforcing the interleaving among conflicting pieces. For example, for the most complex workload Canvas LMS which has 46 user defined transactions, 30 out of 46 transactions access more than one table and each transaction accesses 2.8 tables on average. In these 30 transactions, 12 transactions are involved in a deadlock-prone SC-cycle. After merging the deadlock prone SC-cycles into atomic pieces, there are still 20 transactions which have more than one conflicting piece. All of them can benefit from IC3.

One type of concurrency control is constraining inter-leavings among transactions to preserve some serial order, using various approaches like two-phase locking [1, 26, 8, 14], timestamp ordering [10, 5, 29] and commit ordering [37, 38].

One main difference with prior approaches is that IC3 dynamically constrains interleaving of transaction pieces to preserve serializability, which may lead to more concurrency. Others have proposed decomposing transactions into pieces [18, 4, 13, 41]. To preserve serializability after chopping, Garcia-Molina [17] shows that if all pieces of a decomposed transaction commute, then a safe interleaving exists. This, however, is a strong condition and many OLTP workloads do not suffice. Shasha et al. [41] show that serializability can be preserved if there is no SC-cycle in an SC-graph. Zhang et al. [53] further extends this theory to lower latency in distributed systems. In contrast, IC3 tracks dependency at runtime and constrain the interleaving with SC-graph. Cheung et al. [11] also use static analysis to optimize database applications. However they target the code quality of the database applications which are running on application servers.

There exist some approaches [36, 2] that try to improve performance by being aware of dependencies. Ordered sharing lock [2] allows transactions to hold locks concurrently. It ensures serializability by enforcing order protected operation and lock releasing must obey the lock acquired order. Ramadan et al. [36] developed a dependency aware software transactional memory. They avoid false aborts by tracking dependency. However, both permit unsafe interleaving which cause cascading aborts. IC3 only permits safe interleaving during the execution. Callas [52] is a piece of work done concurrently with ours that also constrains the interleaving of transaction pieces to ensure serializability. Although the basic algorithms of Callas and IC3 are similar, they are designed for different settings (distributed vs. multicore). Furthermore, the details of the algorithms are different, e.g. Callas does not support dynamic workloads.
and does not include the technique of Sec. 1.

Deterministic database [48, 47, 46] leverages a sequencing layer to pre-assign a deterministic lock ordering to eliminate a commit protocol for distributed transactions. Faleiro et al. [16] proposes a deterministic database with lazy evaluation on multicore settings. However, they only allow concurrency after the system knows exactly the data accessed information [40]. Thus, the sequencing layer can become a performance bottleneck with large number of cores.

Recently, there has been work to re-schedule or reconcile conflicting transactions to preserve serializability. For example, Mu et al. [33] reduces conflicts by reordering conflicting pieces of contended transactions to achieve serializability. However, they require the entire dependency graph is generated before to reordering. This approach is not practicable on multicore settings. Narula et al. [34] utilize commutativity of special transaction pieces to mitigate centralized contention during data updating. Compared to this work, IC3 is more general and can be applied to general transactions.

Researchers have also applied other techniques to reduce or even eliminate concurrency control [24, 12, 3]. H-store and its relatives [42, 24, 20, 50] treat each partition as a standalone database and thus local transactions can run to completion without any concurrency control. Cross-partition transactions can then be executed using a global lock. Hence, performance highly depends on whether the partition of database fits the workload and the performance would degrade noticeably when cross-partition transactions increase [49]. Granola [12] requires no locking overhead for a special type of distributed transactions called independent transactions.

IC3 continues this line of research by optimizing transaction processing in modern multicore and in-memory databases [35, 25, 27, 28, 15, 49, 30, 54]. Recently, some databases have started to improve multicore scalability by eliminating centralized locks and latches [22, 23, 39, 21] for databases implemented using 2PL. However, the inherent limitation of 2PL such as read locking constrains its performance under in-memory settings. Several recent systems instead use OCC [1, 26] to provide speedy OLTP transactions, using fine-grained locking [49] or hardware transaction memory to protect the commit phase [29, 51]. As shown in this paper, IC3 notably outperforms both OCC and OLTP under contention.

Subasu et al. [43] describe a hybrid design by using several replicated database engines, each running on a subset of cores, where a primary handles normal requests and other synchronized replicas handle read-only requests. In this case, IC3 could be used to accelerate the primary copy. Dora [35] uses a thread-to-data assignment policy to run each piece accessing a partition to reduce contention on the centralized lock manager. Though it also decomposes the execution of a transaction into pieces, each piece still uses locks to ensure an execution as a whole, while each piece in IC3 executes concurrently with others rather than respecting the synchronization constraints.

8. CONCLUSION

Multi-core in-memory databases demand its concurrency control mechanism to extract maximum parallelism to utilize abundant CPU cores. This paper described IC3, a new concurrency control scheme that constrains interleavings of transaction pieces to preserve serializability while allowing parallel execution under contention. The key idea of IC3 is to combine static analysis with runtime techniques to track and enforce dependencies among concurrent transactions. To demonstrate its effectiveness, we have implemented IC3 and evaluations on a 64-core machine using TPC-C showed that IC3 has better and more scalable performance than OCC, 2PL, and other recently proposed concurrent control mechanisms under moderate or high levels of contention.

Acknowledgements

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References


Appendix: Proof

Definition: Let each S-edge in an SC-graph become directed following the chronological order of pieces. Also, repeatedly merge vertexes (pieces) connected by C-edges to a single vertex. Afterwards, a cycle in the graph is defined as an x-cycle. Similarly, a path is defined as an x-path.

Fact 1. The offline static analysis ensures there is no x-cycle.

We use the concept of serialization graph as a tool to prove serializability. A schedule is serializable iff the serialization graph is acyclic. Because we use OCC to protect the execution of each piece, if we consider each piece as a (sub-)transaction, we have the following property.
**FACT 2.** The serialization graph of pieces is acyclic.

If two pieces $p_i$ and $p_j$ from two different transactions are connected as $p_i \rightarrow p_j$ in the serialization graph, they have a chronological commit order as $t_c(p_i) < t_c(p_j)$, and $p_i, p_j$ should be also connected by a C-edge in the SC-graph. We can denote the chronological commit order as $p_i \rightarrow p_j$.

If two pieces $q_i$ and $p_j$ are connected by an S-edge in the SC-graph, and $q_i$ is ahead of $p_i$ in chronological order, we denote this as $q_i \rightarrow p_j$.

**FACT 3.** IC3 tracks per-record longest path in the serialization graph.

If $T_i \rightarrow T_j$ (expanded as $p_i \rightarrow p_j$) is a longest path in the serialization graph, after $p_i$ is committed, $T_i$ will appear in $T_j$’s depqueue. This also suggests that $T_j$ will only enter its commit phase after $T_i$ commits.

Theorem 1. The schedule of IC3 is serializable as it always generates acyclic serialization graph.

Now we are going to prove IC3 is serializable by proving the serialization graph is acyclic. Assume there is a cycle in the serialization graph, let it be $T_1 \rightarrow T_2 \rightarrow ... \rightarrow T_n \rightarrow T_1$. We are going to prove that the cycle necessarily plays a role in the SC-graph, which leads to a contradiction to Fact 1.

Expand each transaction in the cycle $T_1 \rightarrow T_2 \rightarrow ... \rightarrow T_n \rightarrow T_1$ to pieces, as

$q_1 \rightarrow p_1 \rightarrow q_2 \rightarrow p_2 \rightarrow ... \rightarrow q_n \rightarrow p_n \rightarrow q_1$

The symbol $\rightarrow$ above (between a pair of $q_i \rightarrow p_i$) represents following three possible cases:

1. $q_i$ and $p_i$ are the same piece, i.e. $q_i = p_i$.
2. $q_i$ and $p_i$ are different pieces, they are connected by an S-edge, and $q_i$ is chronologically ahead of $p_i$, denoted by $q_i \rightarrow p_i$.
3. $q_i$ and $p_i$ are different pieces, they are connected by an S-edge, and $q_i$ is chronologically behind $p_i$, denoted by $q_i \leftarrow p_i$.

To simplify without loss of accuracy, we use the symbol $\rightarrow i$ to represent the combination of the first and second cases; $\leftarrow i$ to represent the first and third cases.

**Lemma 1. No transaction in cycle can commit.**

According to Fact 3, the cycle $T_1 \rightarrow T_2 \rightarrow ... \rightarrow T_n \rightarrow T_1$ necessarily implies an acyclic cycle in the commit order, i.e. $t_c(T_1) < t_c(T_2) < ... < t_c(T_n) < t_c(T_1)$, which is not possible. According to IC3’s protocol, a cycle in the serialization graph will necessarily cause a deadlock in transaction commit phase, which means no transaction is able to commit. Actually, such deadlock can never form in the first place. The following part explains that.

**Lemma 2.** $\exists i : q_i \rightarrow p_i$

Assume for every pair of $q_i$ and $p_i$, they are the same piece. Then the cycle leads a contradiction: the cycle should not exist according to Fact 2.

**Lemma 3.** $\exists i, j : q_i \rightarrow p_i$ and $p_j \rightarrow q_j$

Proof by contradiction. Without loss of generality, assume $\forall i : q_i \rightarrow p_i$. Then the cycle will necessarily imply an x-cycle in static analysis, which contradicts with Fact 1.

**Lemma 4.** For a fragment $p_i \rightarrow q_j \rightarrow p_j$, there will be a piece $r_i$ in $T_i$, such that $p_i \rightarrow r_i \rightarrow q_j$.

$q_j \rightarrow p_j$ refers to that before $p_j$ executes, $q_j$ already commits, leaving $T_i$ in $T_j$’s depqueue. Therefore, when $p_j$ commits, it shall either wait $T_i$ commits, or it waits until all pieces in $T_i$ that has C-connection to itself commits. According to Lemma 1 it has to be the latter case. Assume the last piece in $T_i$ that has C-connection to $p_j$ is $r_i$. $r_i$ cannot be neither be $p_i$ or any piece before $p_i$. Otherwise, $r_i \rightarrow p_i \rightarrow q_j \rightarrow p_j \rightarrow r_i$ will form a x-cycle, which contradicts with Fact 1.

With Lemma 4, we can inductively prove the cycle in a serialization graph will necessarily implies an x-cycle in static analysis.

In the cycle:

$q_1 \rightarrow p_1 \rightarrow q_2 \rightarrow p_2 \rightarrow ... \rightarrow q_n \rightarrow p_n \rightarrow q_1$

If there exists $j$ that $j \rightarrow p_j$, without loss of generosity, we can safely assume $j = n$. We can shrink the cycle following Lemma 4, then the cycle becomes as follows.

$q_1 \rightarrow p_1 \rightarrow q_2 \rightarrow p_2 \rightarrow ... \rightarrow q_{n-1} \rightarrow p_{n-1} \rightarrow r_{n-1} \rightarrow q_1$

Transform the above cycle into:

$q_1 \rightarrow p_1 \rightarrow q_2 \rightarrow p_2 \rightarrow ... \rightarrow q_{n-1} \rightarrow p_{n-1} \rightarrow q_1$

Repeatedly reduce the cycle following Lemma 4, for $m$ times ($m < n$), until we have:

$q_1 \rightarrow p_1 \rightarrow q_2 \rightarrow p_2 \rightarrow ... \rightarrow q_{n-1} \rightarrow p_{n-1} \rightarrow q_1$

Consider each pair of $q_i \rightarrow p_i$ in the above cycle, there exists at least one pair of $q_i \rightarrow p_i$ such that $q_i \rightarrow p_i$. Otherwise, we will have $q_1 \rightarrow q_2 \rightarrow ... \rightarrow q_i \rightarrow q_1$, which is not possible. Then means the above cycle necessarily implies an x-cycle in the SC-graph, which is a contradiction to the result of static analysis.

Q.E.D.