

Lecture 2

Homework 1 is out

- Due on Mon 25th Feb
- Also start looking at ideas for projects
- Suggestions are welcome!

Overview of today



- Physics of color
- Human encoding of color
- Color spaces
- Camera sensor & color
- Demosaicing
- White balancing

Overview of today

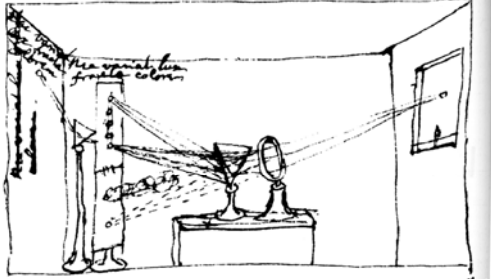
- **Physics of color**
- Human encoding of color
- Color spaces
- Camera sensor & color
- Demosaicing
- White balancing

Why is color useful

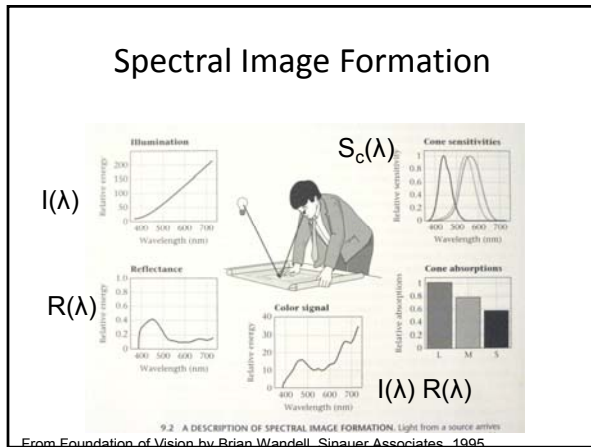
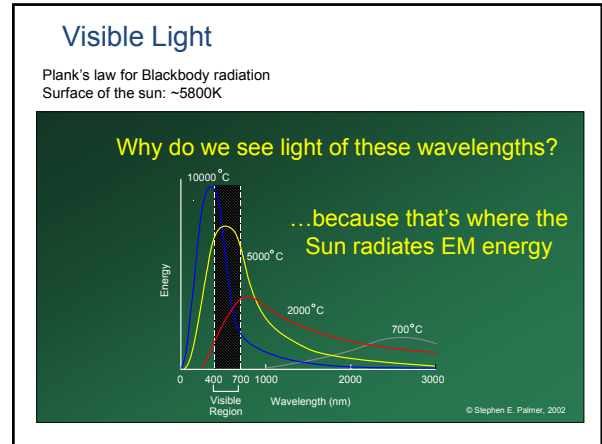
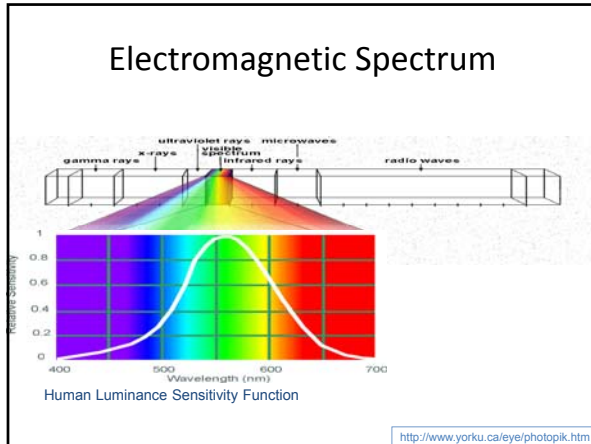
- Find things to eat
- Spot dangerous things

Color



4.1 NEWTON'S SUMMARY DRAWING of his experiments with light. Using a point source of light and a prism, Newton separated sunlight into its fundamental components. By reconverging the rays, he also showed that the decomposition is reversible.
From Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995



Spectral Image Formation

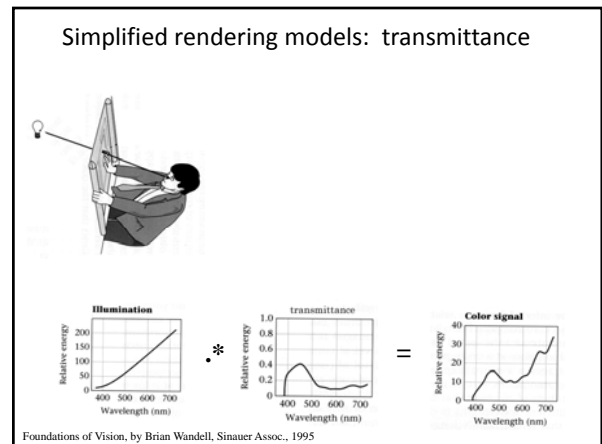
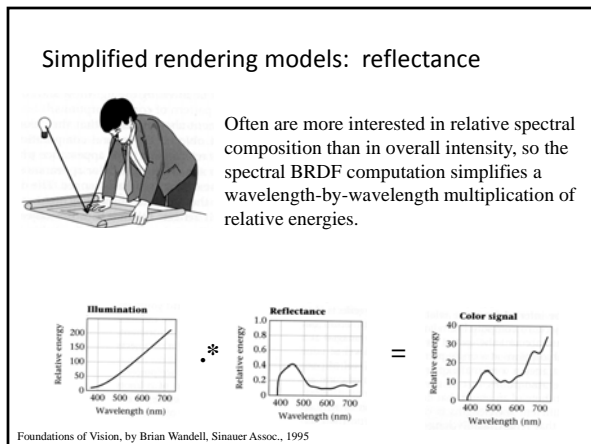
$$p_c = \int I(\lambda) S_c(\lambda) R(\lambda) d\lambda$$

$I(\lambda)$ – Illumination Spectrum

$S_c(\lambda)$ - Spectral sensitivity of channel c

$R(\lambda)$ - Surface reflectance/transmission

Pixel value / Perceived color depends on all 3 terms!
→ Problem of color constancy



How measure those spectra: Spectrophotometer

(just like Newton's diagram...)

(A) Source Lens Prism Lens Movable slit Sensor

Wavelength (nm)	Color (viewed in isolation)
700	Red
610	Orange
580	Yellow
540	Green
480	Blue
400	Violet

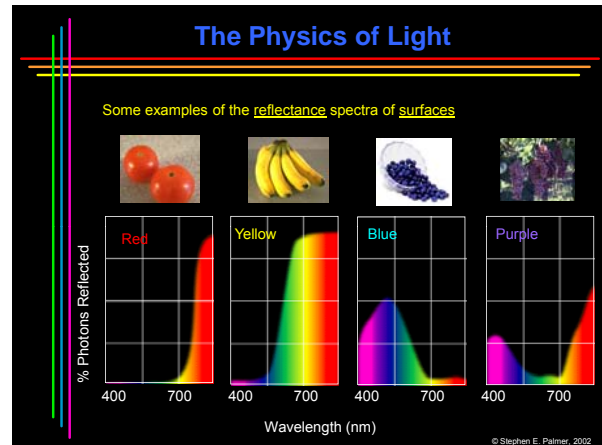
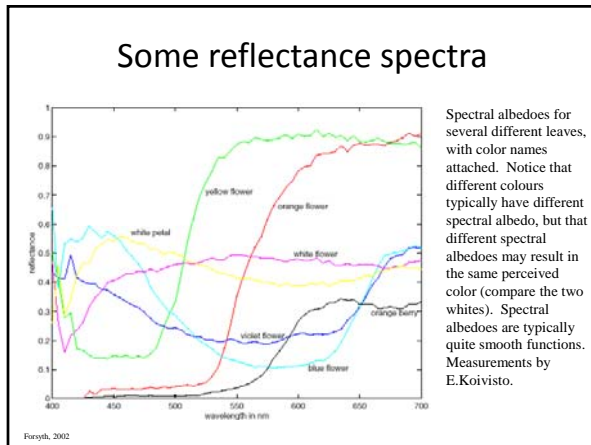
(B)

4.2 A SPECTRORADIOMETER is used to measure the spectral power distribution of light. (A) A schematic design of a spectroradiometer includes a means for separating the input light into its different wavelengths and a detector for measuring the energy at each of the separate wavelengths. (B) The color names associated with the appearance of lights at a variety of wavelengths are shown. After Wyszecki and Stiles, 1982.

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Spectrometer Demo

- Lights
- Bulb
- LEDs



Transmission Demo

- Gels
- Glasses

Spectra are smooth

- Physical process involved with transmission/reflection means that spectra are similar at nearby wavelengths
- Can model spectra in low dimensional space
 - Principal Components Analysis (PCA)

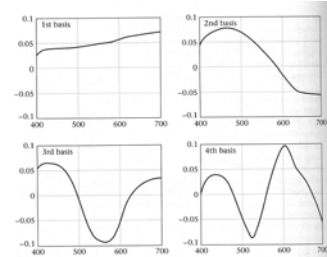
Low-dimensional models for color spectra - PCA

$$e(\lambda) = \begin{pmatrix} \vdots \\ \vdots \\ \vdots \end{pmatrix} = \begin{pmatrix} E_1(\lambda) & E_2(\lambda) & E_3(\lambda) \\ \vdots & \vdots & \vdots \end{pmatrix} \begin{pmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \end{pmatrix}$$

How to find a linear model for color spectra:
 --form a matrix, D, of measured spectra, 1 spectrum per column.
 --[u, s, v] = svd(D) satisfies D = u*s*v'
 --the first n columns of u give the best (least-squares optimal) n-dimensional linear bases for the data, D:
 $D \approx u(:,1:n) * s(1:n,1:n) * v(1:n,:)$

Slide credit:
W. Freeman

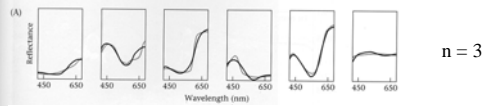
Basis functions for Macbeth color checker



9.9 BASIS FUNCTIONS OF THE LINEAR MODEL FOR THE MACBETH COLORCHECKER. The surface-reflection functions in the collection vary smoothly with wavelength, as do the basis functions. The first basis function is all positive and explains the most variance in the surface-reflection functions. The basis functions are ordered in terms of their relative significance for reducing the error in the linear-model approximation to the surfaces.

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

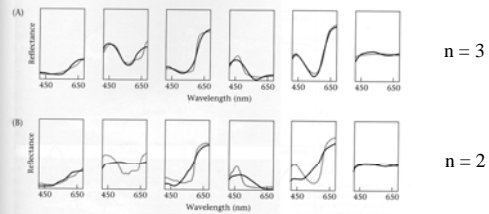
n-dimensional linear models for color spectra



9.8 A LINEAR MODEL TO APPROXIMATE THE SURFACE REFLECTANCES IN THE MACBETH COLORCHECKER. The panels in each row of this figure show the surface-reflection functions of six colored surfaces (shaded lines) and the approximation to these functions using a linear model (solid lines). The approximations using linear models with (A) three, (B) two, and (C) one dimension are shown.

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

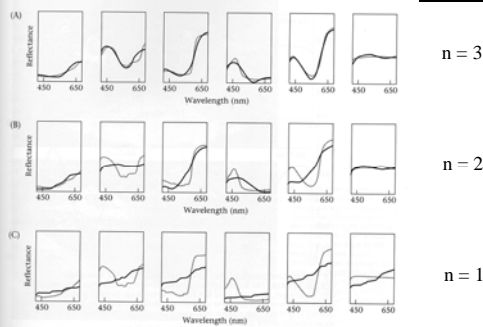
n-dimensional linear models for color spectra



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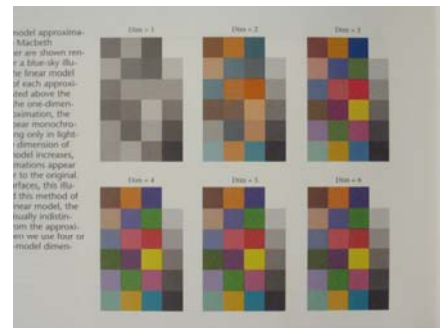
n-dimensional linear models for color spectra



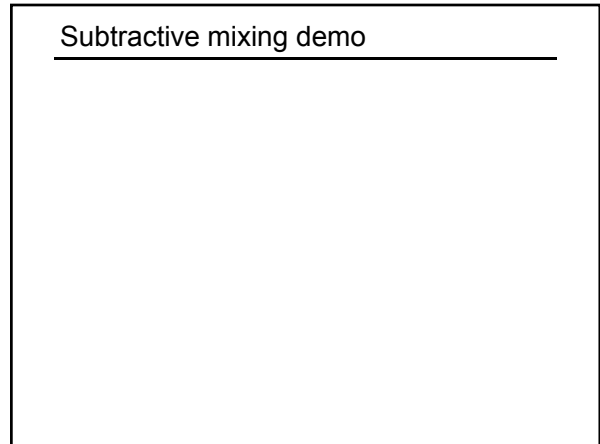
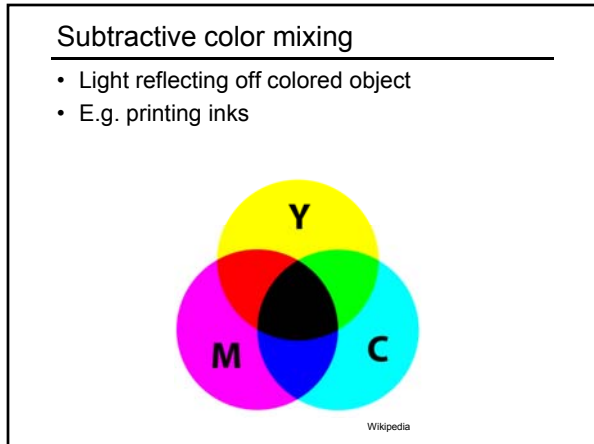
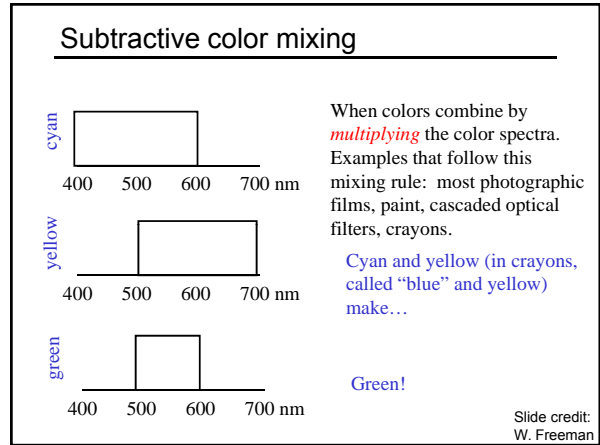
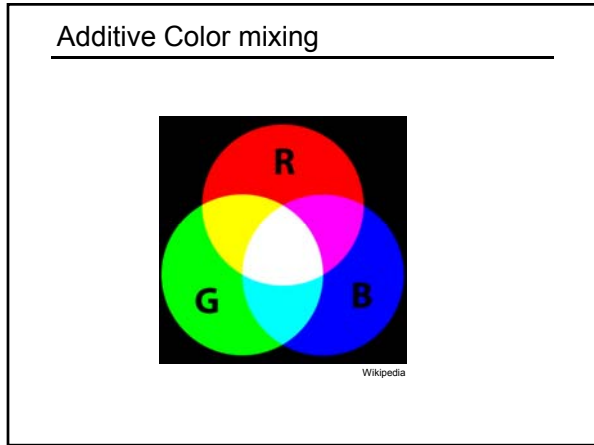
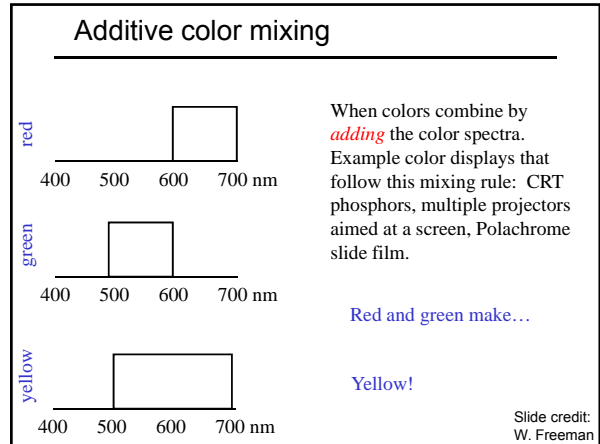
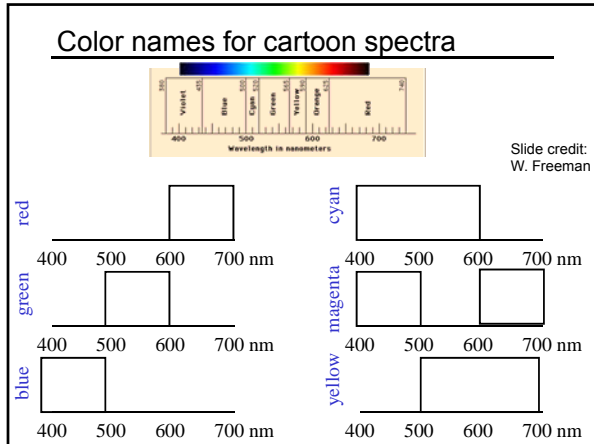
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Reconstruction of MacBeth color chart



From Foundation of Vision by Brian Wandell, Sinauer Associates, 1995



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- Color spaces
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The Eye

The human eye is a camera!

- **Iris** - colored annulus with radial muscles
- **Pupil** - the hole (aperture) whose size is controlled by the iris
- What's the "film"?
 - photoreceptor cells (rods and cones) in the **retina**

Slide by Steve Seitz

The Retina

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Retina up-close

Two types of light-sensitive receptors

Cones
cone-shaped
less sensitive
operate in high light
color vision

cone
rod

Rods
rod-shaped
highly sensitive
operate at night
gray-scale vision

Human Photoreceptors

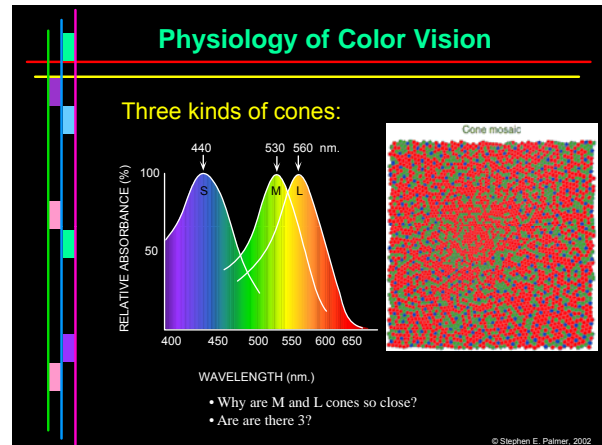
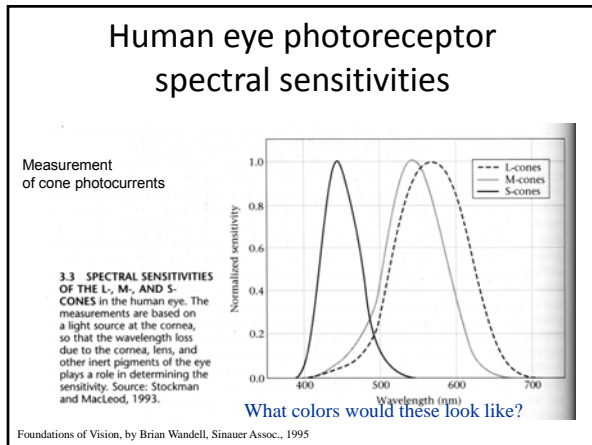
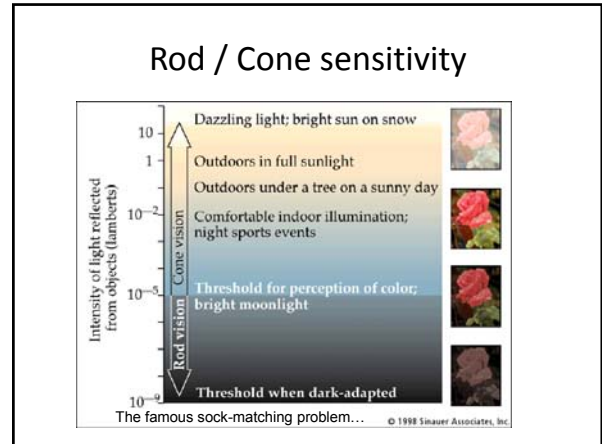
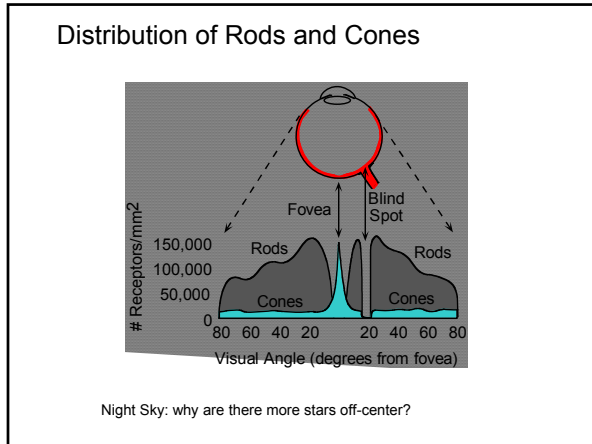
(A)

(B)

(C)

3.4 THE SPATIAL MOSAIC OF THE HUMAN CONES. Cross sections of the human retina at the level of the inner segments showing (A) cones in the fovea, and (B) cones in the periphery. Note the size difference (scale bar = 10 μ m), and that, as the separation between cones grows, the rod receptors fill in the spaces. (C) Cone density plotted as a function of distance from the center of the fovea for seven human retinas; cone density decreases with distance from the fovea. Source: Curcio et al., 1990.

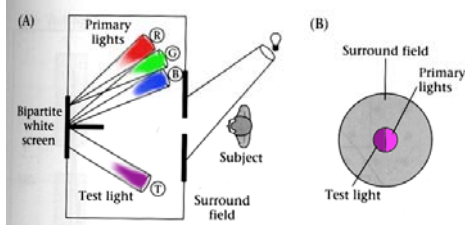
(From Foundations of Vision, by Brian Wandell, Sinauer Assoc.)



- ### Why specify color numerically?
- Accurate color reproduction is commercially valuable
 - Many products are identified by color ("golden" arches);
 - Few color names are widely recognized by English speakers -
 - About 10; other languages have fewer/more, but not many more.
 - It's common to disagree on appropriate color names.
 - Color reproduction problems increased by prevalence of digital imaging - eg. digital libraries of art.
 - How do we ensure that everyone sees the same color?
- Forsyth & Ponce

- ### An assumption that sneaks in here
- For now we will assume that the spectrum of the light arriving at your eye completely determines the perceived color.
 - But we know color appearance really depends on:
 - The illumination
 - Your eye's adaptation level
 - The colors and scene interpretation surrounding the observed color.
- Slide credit: W. Freeman

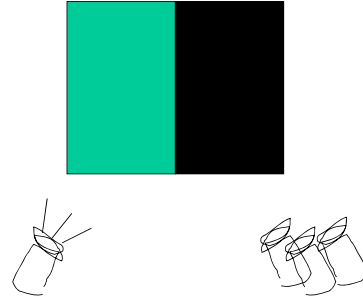
Color matching experiment



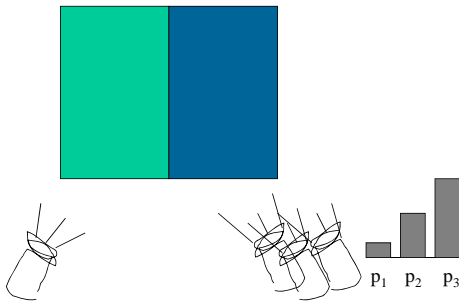
4.10 THE COLOR-MATCHING EXPERIMENT. The observer views a bipartite field and adjusts the intensities of the three primary lights to match the appearance of the test light. After Judd and Wyszecki, 1975.

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

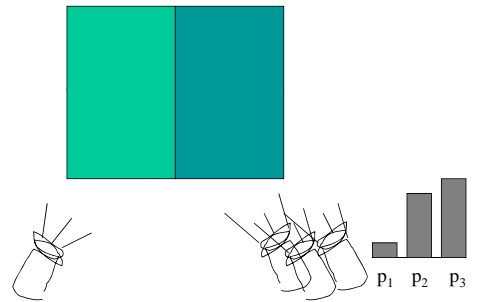
Color matching experiment 1



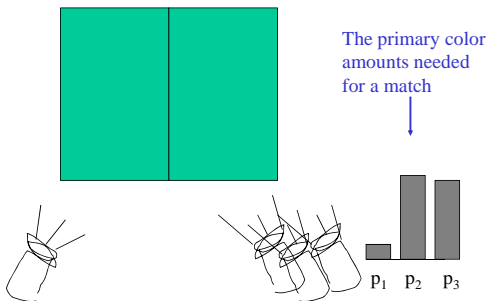
Color matching experiment 1



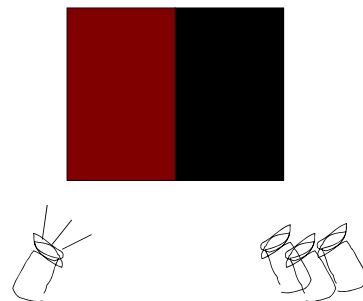
Color matching experiment 1

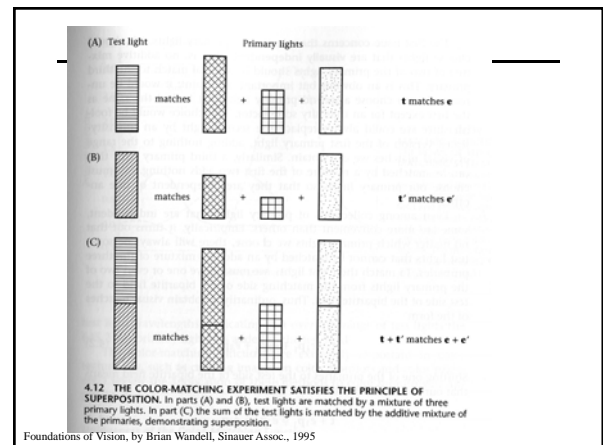
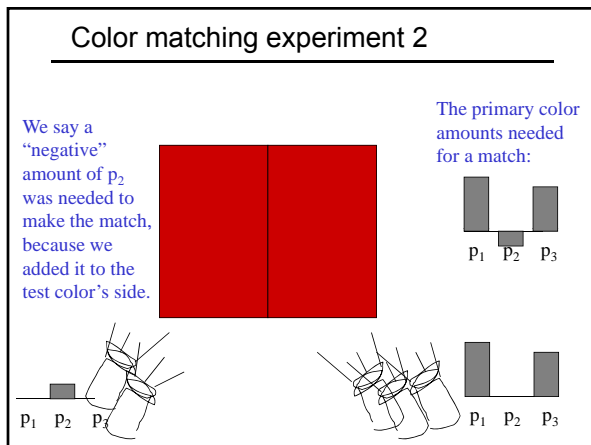
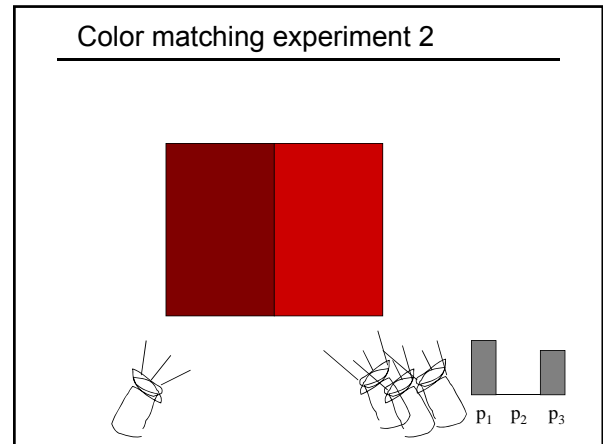
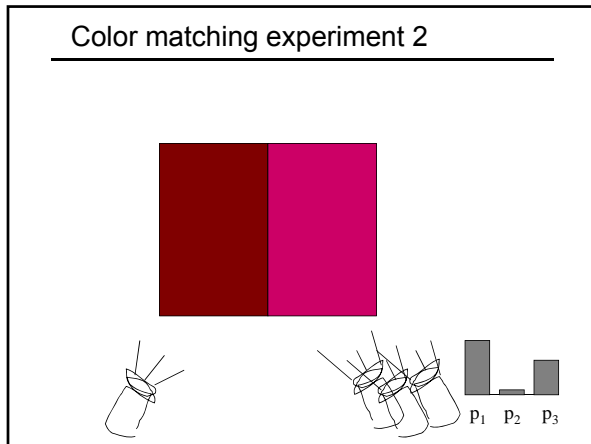


Color matching experiment 1



Color matching experiment 2





Grassman's Laws

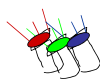
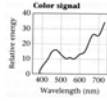
- For color matches:
 - symmetry: $U=V \Leftrightarrow V=U$
 - transitivity: $U=V$ and $V=W \Rightarrow U=W$
 - proportionality: $U=V \Leftrightarrow tU=tV$
 - additivity: if any two (or more) of the statements $U=V$, $W=X$, $(U+W)=(V+X)$ are true, then so is the third
- These statements are as true as any biological law. They mean that additive color matching is linear.

Forsyth & Ponce

Measure color by color-matching paradigm

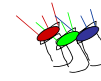
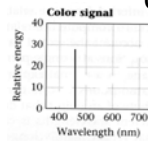
- Pick a set of 3 primary color lights.
- Find the amounts of each primary, e_1, e_2, e_3 , needed to match some spectral signal, t .
- Those amounts, e_1, e_2, e_3 , describe the color of t . If you have some other spectral signal, s , and s matches t perceptually, then e_1, e_2, e_3 will also match s , by Grassman's laws.
- Why this is useful—it lets us:
 - Predict the color of a new spectral signal
 - Translate to representations using other primary lights.

Goal: compute the color match for any color signal for any set of primary colors



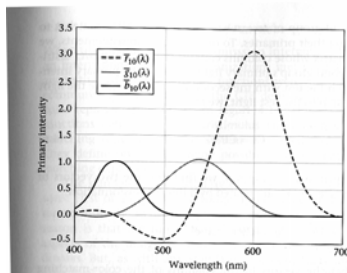
- Examples of why you'd want to do that:
 - Want to paint a carton of Kodak film with the Kodak yellow color.
 - Want to match skin color of a person in a photograph printed on an ink jet printer to their true skin color.
 - Want the colors in the world, on a monitor, and in a print format to all look the same.

How to compute the color match for any color signal for any set of primary colors



- Pick a set of primaries, $p_1(\lambda), p_2(\lambda), p_3(\lambda)$
- Measure the amount of each primary, $c_1(\lambda), c_2(\lambda), c_3(\lambda)$ needed to match a monochromatic light, $t(\lambda)$ at each spectral wavelength λ (pick some spectral step size). These are called the color matching functions.

Color matching functions for a particular set of monochromatic primaries



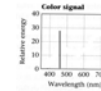
- $p_1 = 645.2$ nm
- $p_2 = 525.3$ nm
- $p_3 = 444.4$ nm

4.13 THE COLOR-MATCHING FUNCTIONS ARE THE ROWS OF THE COLOR-MATCHING SYSTEM MATRIX. The functions measured by Stiles and Burch (1959) using a 10-degree bipartite field and primary lights at the wavelengths 645.2 nm, 525.3 nm, and 444.4 nm with unit radiant power are shown. The three functions in this figure are called $P_{10}(\lambda)$, $B_{10}(\lambda)$, and $G_{10}(\lambda)$.

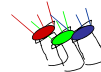
Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Using the color matching functions to predict the primary match to a new spectral signal

We know that a monochromatic light of wavelength will be matched by the amounts $c_1(\lambda_i), c_2(\lambda_i), c_3(\lambda_i)$

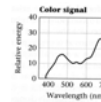


of each primary.



And any spectral signal can be thought of as a linear combination of very many monochromatic lights, with the linear coefficient given by the spectral power at each wavelength.

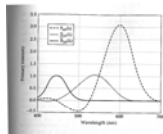
$$\vec{t} = \begin{pmatrix} t(\lambda_1) \\ \vdots \\ t(\lambda_N) \end{pmatrix}$$



Using the color matching functions to predict the primary match to a new spectral signal

Store the color matching functions in the rows of the matrix, C

$$C = \begin{pmatrix} c_1(\lambda_1) & \cdots & c_1(\lambda_N) \\ c_2(\lambda_1) & \cdots & c_2(\lambda_N) \\ c_3(\lambda_1) & \cdots & c_3(\lambda_N) \end{pmatrix}$$



Let the new spectral signal be described by the vector t.

$$\vec{t} = \begin{pmatrix} t(\lambda_1) \\ \vdots \\ t(\lambda_N) \end{pmatrix}$$

Then the amounts of each primary needed to match t are: $C\vec{t}$

Switching between matching functions

- Color matching functions are not unique
- Depend on set of primaries!
- Map between coordinates in two bases using 3x3 matrix

How do you translate colors between different systems of primaries?

■ $p_1 = (0\ 0\ 0\ 0\ 0 \dots\ 0\ 1\ 0)^T$	■ $p'_1 = (0\ 0.2\ 0.3\ 4.5\ 7 \dots\ 2.1)^T$
■ $p_2 = (0\ 0 \dots\ 0\ 1\ 0 \dots\ 0\ 0)^T$	■ $p'_2 = (0.1\ 0.44\ 2.1 \dots\ 0.3\ 0)^T$
■ $p_3 = (0\ 1\ 0\ 0 \dots\ 0\ 0\ 0\ 0)^T$	■ $p'_3 = (1.2\ 1.7\ 1.6 \dots\ 0\ 0)^T$

Primary spectra, P Primary spectra, P'

Color matching functions, C Color matching functions, C'

The amount of each primary in P needed to match the color with spectrum t. The color of that match to t, described by the primaries, P.

Any input spectrum, t

The amount of each P' primary needed to match t

The spectrum of a perceptual match to t, made using the primaries P'

So, how to translate from the color in one set of primaries to that in another:

The values of the 3 primaries, in the unprimed system

The values of the 3 primaries, in the primed system

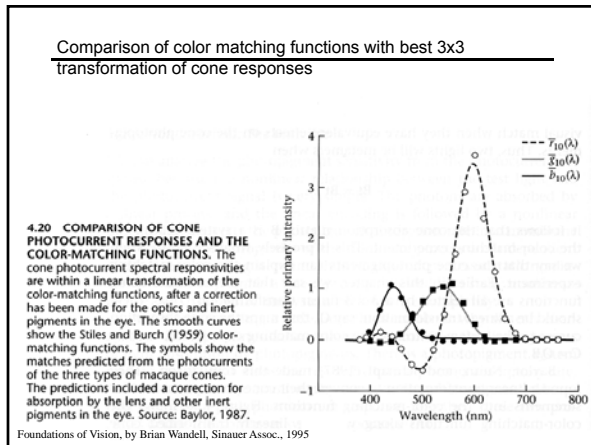
$$e = CP'e'$$

a 3x3 matrix

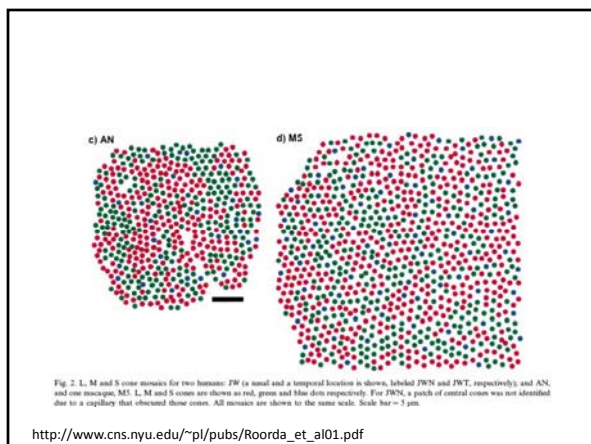
C

P'

P' are the old primaries
C are the new primaries' color matching functions



- Summary so far
- Set of non-unique color matching functions that can be used to describe color in 3-coordinate system
 - Can describe physiology experiments that directly electrical signals from cone cell
 - Mapping between matching functions takes form of 3x3 matrix
 - Let's now look at the various color spaces used to describe color



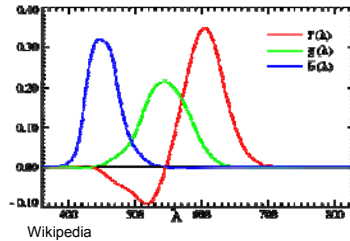
- Overview of today
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Basic issues

- How to represent a continuous spectrum in a three coordinate system
- Cover wide range of colors
- Limited dynamic range (8bits/channel)
- Preferably be intuitive

CIE Standard Observer Color matching functions

- 3-D coordinate space
- Difficult to visualize in 2-D



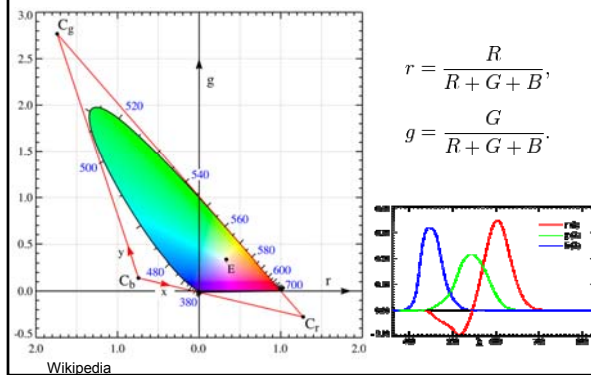
Define:

$$r = \frac{R}{R + G + B},$$

$$g = \frac{G}{R + G + B}.$$

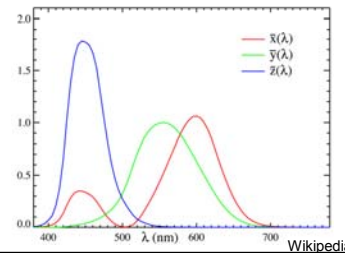
Constant brightness

CIE rg Chromaticity space

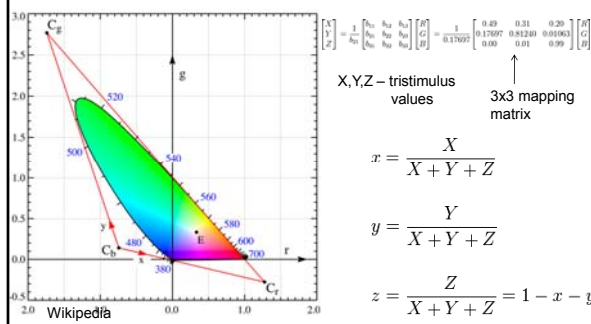


CIE XYZ color-matching functions (1931)

- No negative light
- Green matches luminosity (overall brightness)
- Primaries not physically realizable
- Not an intuitive representation

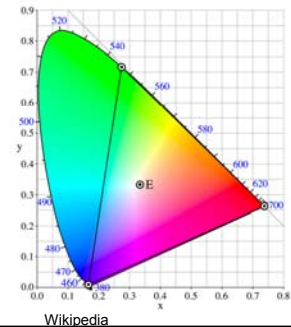


Mapping to CIE XYZ (1931)



CIE XYZ Chromaticity space

- 2-D slice of inherently 3-D space
- Many other spaces but are derivatives of this
- Used to show range of colors obtainable, known as the gamut



sRGB color space

- Standard space used for 8-bit/channel color display
- Representation implicit for most images/application.
- Limited gamut (other spaces exist with larger gamut)
- Incorporates non-linearities inherent in display devices (1/)
- Mapping from CIE XYZ to sRGB has two parts:
 - $$\begin{bmatrix} R_{linear} \\ G_{linear} \\ B_{linear} \end{bmatrix} = \begin{bmatrix} 3.2410 & -1.5374 & -0.4986 \\ -0.9692 & 1.8760 & 0.0416 \\ 0.0556 & -0.2040 & 1.0570 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$
 - $$C_{comp} = \begin{cases} 12.92C_{linear}, & C_{linear} \leq 0.0031308 \\ (1 + a)C_{linear}^{2.4} - a, & C_{linear} > 0.0031308 \end{cases}$$

Wikipedia

Gamma correction

- Tone response curve

Wikipedia

Typical CMYK color space

http://www.tasi.ac.uk/images/cie_gamut.jpg

Intuitive color space

- Hue, Saturation, Brightness
- Very similar to Hue, Saturation, Value

The Psychophysical Correspondence

There is no simple functional description for the perceived color of all lights under all viewing conditions, but

A helpful constraint:
Consider only physical spectra with normal distributions

Photons

Wavelength (nm.)

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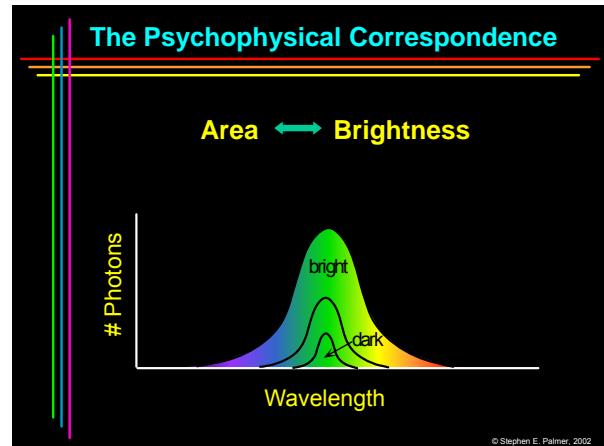
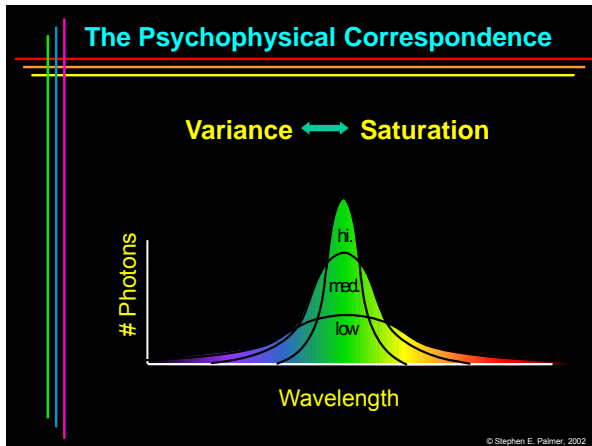
The Psychophysical Correspondence

Mean ↔ Hue

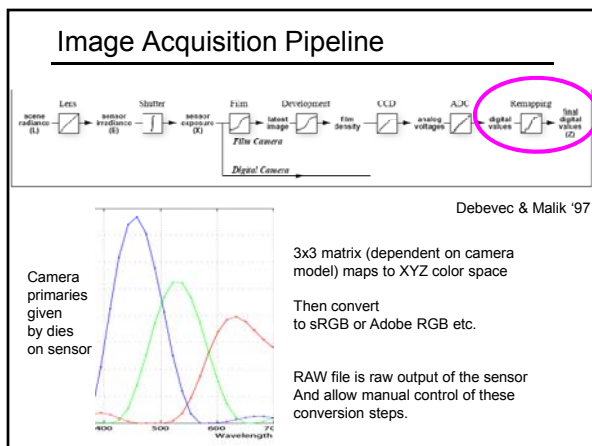
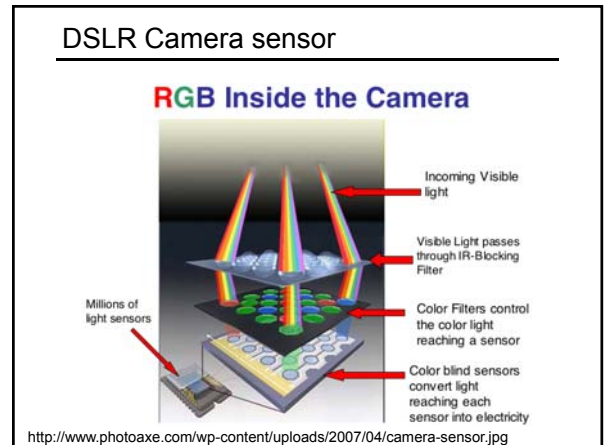
Photons

Wavelength

© Stephen E. Palmer, 2002



- ### Overview of today
- Physics of color
 - Human encoding of color
 - Color spaces
 - Camera sensor & color
 - Demosaicing
 - White balancing



Sensitivity (ISO)

- Third variable for exposure
- Linear effect (200 ISO needs half the light as 100 ISO)

Kodachrome 25 ASA Ektachrome 64 ASA Fujichrome 160 ASA Ektachrome 320 ASA

Nikon D2X ISO 100	Nikon D2X ISO 200	Nikon D2X ISO 400	Nikon D2X ISO 800	Nikon D2X ISO 1600	Nikon D2X ISO 3200

From dpreview.com

CCD color sampling

- Problem: a photosite can record only one number
- We need 3 numbers for color

What are some approaches to sensing color images?

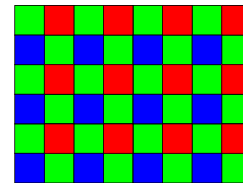
- Scan 3 times (temporal multiplexing)
- Use 3 detectors (3-ccd camera)
- Use offset color samples (spatial multiplexing)
- Multiplex in the depth of the sensor (Foveon)

Some approaches to color sensing

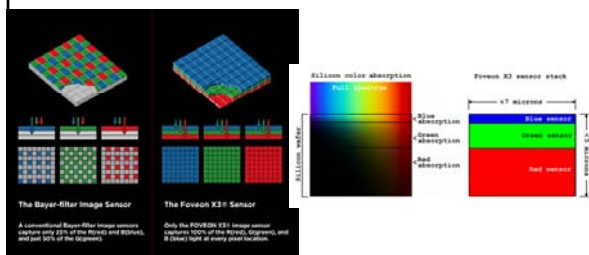
- Scan 3 times (temporal multiplexing)
 - Drum scanners
 - Flat-bed scanners
 - Russian photographs from 1800's
- Use 3 detectors
 - High-end 3-tube or 3-ccd video cameras
- Use spatially offset color samples (spatial multiplexing)
 - Single-chip CCD color cameras
 - Human eye
- Multiplex in the depth of the sensor
 - Foveon

Bayer RGB mosaic

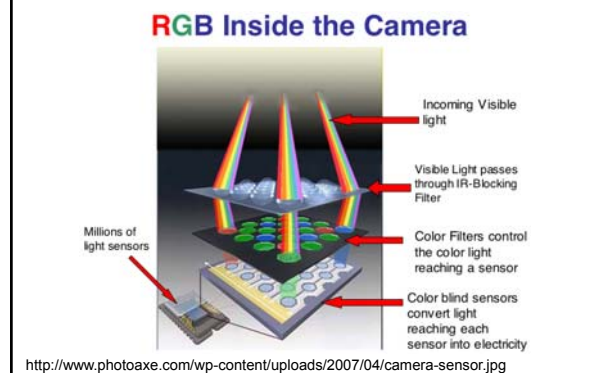
- Why more green?
 - We have 3 channels and square lattice don't like odd numbers
 - It's the spectrum "in the middle"
 - More important to human perception of brightness

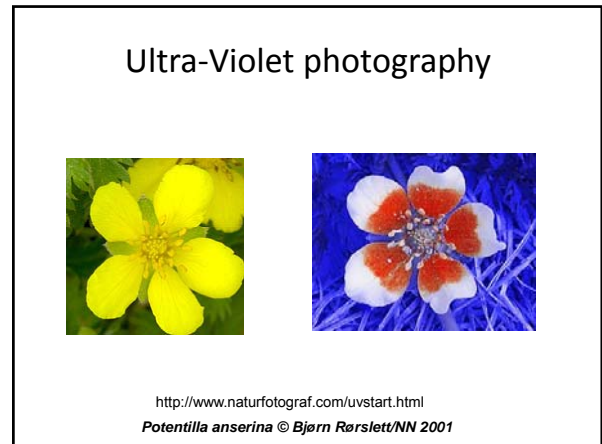
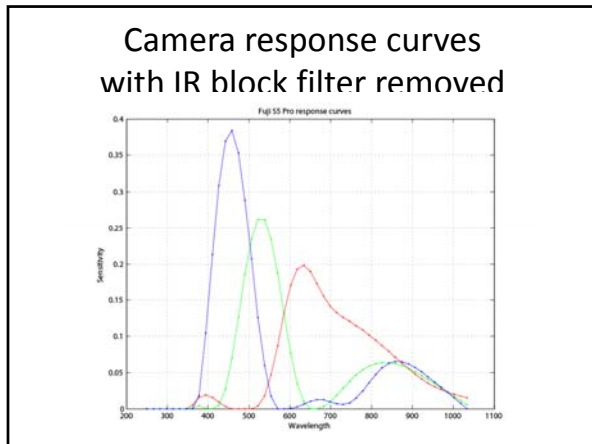


Foveon image sensor

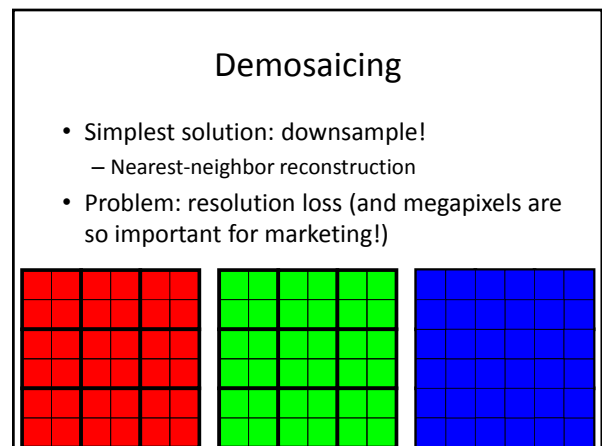
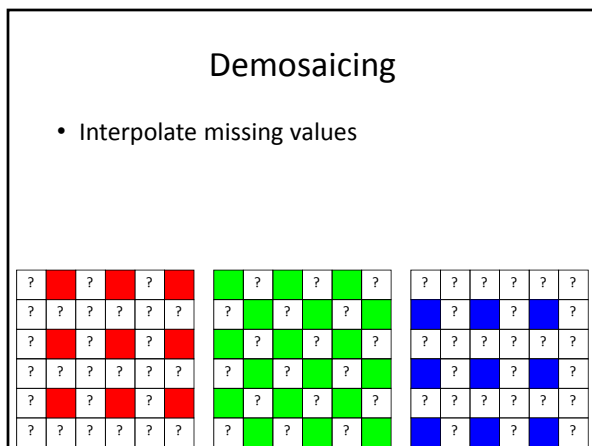


DSLR Camera sensor



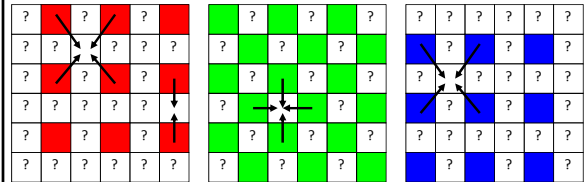


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 - White balancing

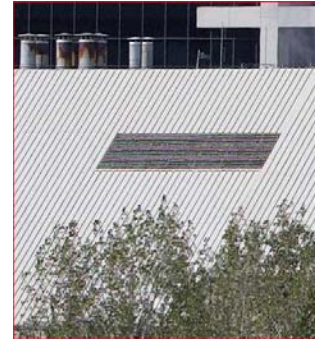


Linear interpolation

- Average of the 4 or 2 nearest neighbors
 - Linear (tent) kernel
- Smoother kernels can also be used (e.g. bicubic) but need wider support

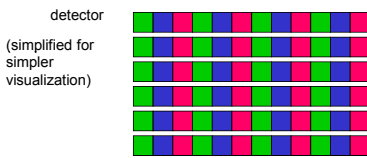


Color Moire patterns



<http://forums.dpreview.com/forums/read.asp?forum=1034&message=8115658>

CCD color filter pattern



Slide credit: F. Durand

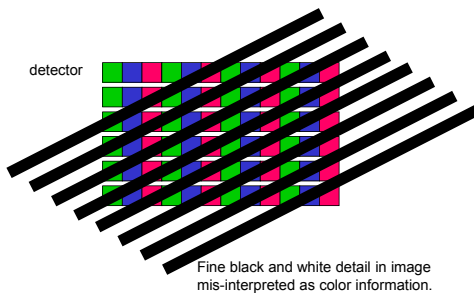
Typical color moire patterns



Blow-up of electronic camera image. Notice spurious colors in the regions of fine detail in the plants.

Slide credit: F. Durand

The cause of color moire



Slide credit: F. Durand

Motivation for median filter interpolation



The color fringe artifacts are obvious; we can point to them. Goal: can we characterize the color fringe artifacts mathematically? Perhaps that would lead to a way to remove them...

Slide credit: F. Durand

Median filter

Replace each pixel by the median over N pixels (5 pixels, for these examples). Generalizes to "rank order" filters.

In:

5-pixel neighborhood

Out:

Spike noise is removed

In:

Out:

Monotonic edges remain unchanged

Slide credit: F. Durand

Recombining the median filtered colors

Linear interpolation
Median filter interpolation

Slide credit: F. Durand

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White balance problem

- Spectrum of light source affects color of objects in scene
- We need to discount the color of the light source
- We often don't notice since we adapt to the illuminant of the room, not that of the scene in the picture

Von Kries adaptation

- Multiply each channel by a gain factor
- Note that the light source could have a more complex effect
 - Arbitrary 3x3 matrix
 - More complex spectrum transformation

Slide credit: F. Durand

Best way to do white balance

- Grey card:
- Take a picture of a neutral object (white or gray)
- Deduce the weight of each channel
- If the object is recoded as r_w, g_w, b_w use weights $1/r_w, 1/g_w, 1/b_w$

Slide credit: F. Durand

Grey world assumption

- The average color in the image is grey
- Use weights

$$\frac{1}{\int_{image} r}, \frac{1}{\int_{image} g}, \frac{1}{\int_{image} b}$$

- Note that this also sets the exposure/brightness
- Usually assumes 18% grey

Slide credit: F. Durand

Brightest pixel assumption

- Highlights usually have the color of the light source
 - At least for dielectric materials
- Do white balance by using the brightest pixels
 - Plus potentially a bunch of heuristics
 - In particular use a pixel that is not saturated/clipped

Slide credit: F. Durand

End

Sensitivity to blur

